

# Neutron EDM and Dressed Spin

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# Outline

- History of neutron EDM search
- Review of neutron EDM technique
- Neutron EDM experiment at SNS at ORNL
- Measurement of dressed spin
- Theory of dressed spin
- Simulation of dressed spin and neutron EDM experiment

# Neutron electric dipole moment

$$\vec{d}_n = \int dx^3 \rho \vec{x} = d_n \hat{S}$$



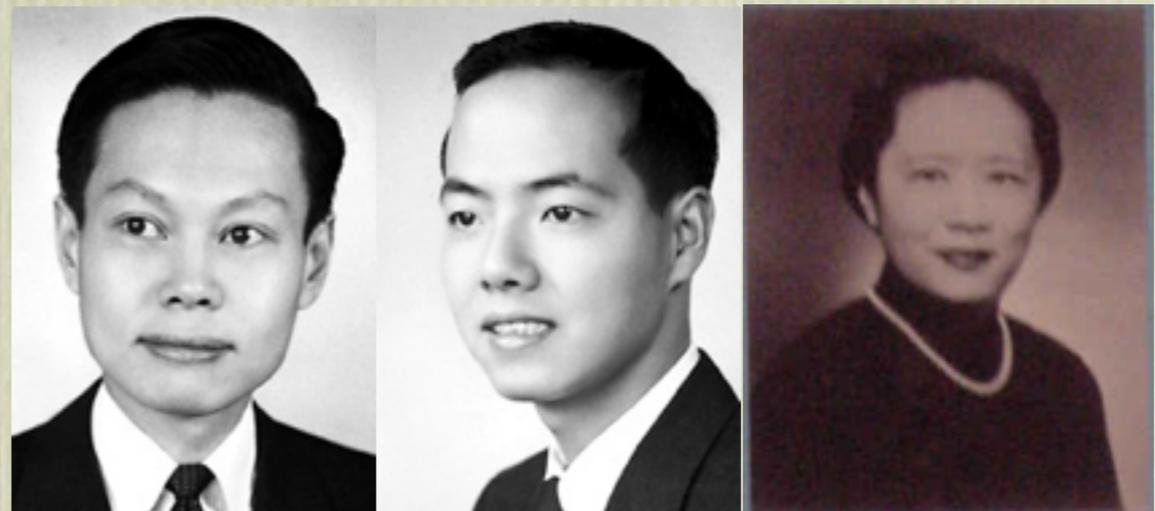
- Electric dipole moment (EDM) is the first moment of the charge distribution ( $\rho$ ).
- The EDM (**vector**) is parallel to the **Spin (axial vector)** direction.
- A non-zero neutron EDM violates the parity symmetry.

# Pioneers of neutron electric dipole moment



**Purcell Ramsey**

- Purcell and Ramsey emphasized the possibility of a non-zero neutron EDM and the need to check it experimentally.
- They set an upper limit of  $3 \times 10^{-18}$  e cm from the neutron-nucleus scattering data (1950).
- They carried out a pioneering measurement of the upper limit of  $5 \times 10^{-20}$  e cm by using the separated oscillatory field at Oak Ridge (1950) (later slides).
- The parity violation was suggested by Lee and Yang (1956) and discovered by Wu, et al. (1957).
- Still no neutron EDM was observed.

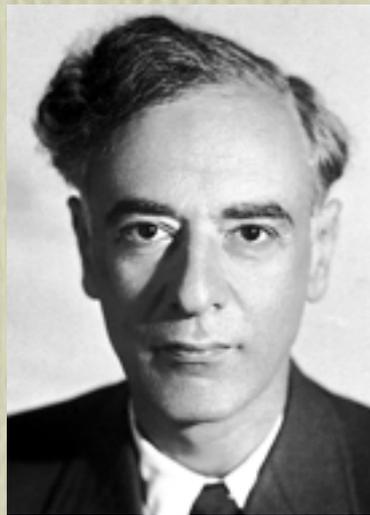


**Yang**

**Lee**

**Wu**

# EDM and CP violation



Landau

$$\vec{d}_n = \int dx^3 \rho \vec{x} = d_n \hat{S}$$



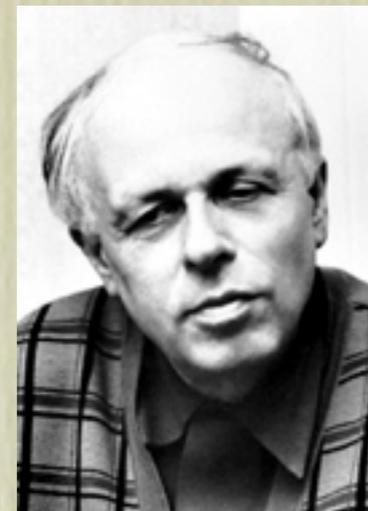
Cronin

Fitch

- Landau showed that particles cannot possess EDM from time-reversal invariance (1957).
- T violation implies **CP violation** if CPT holds.
- No neutron EDM experiments during 1957-1964.
- CP violation was discovered in **neutral Kaons decay** by Cronin and Fitch(1964).

# Baryon asymmetry of Universe and CP violation

- Baryon asymmetry of universe (BAU) : baryon/photon $\sim 10^{-10}$ .
- Sakharov proposed CP violation as one of necessary ingredients(1967).
- CP violation has only been observed in **Kaon and B meson decays**, which can be explained by **Kobayashi-Maskawa mechanism** (CKM matrix) in SM(baryon/photon $\sim 10^{-18}$ ).
- Require CP violation beyond the SM.



**Sakharov**



**Kobayashi**

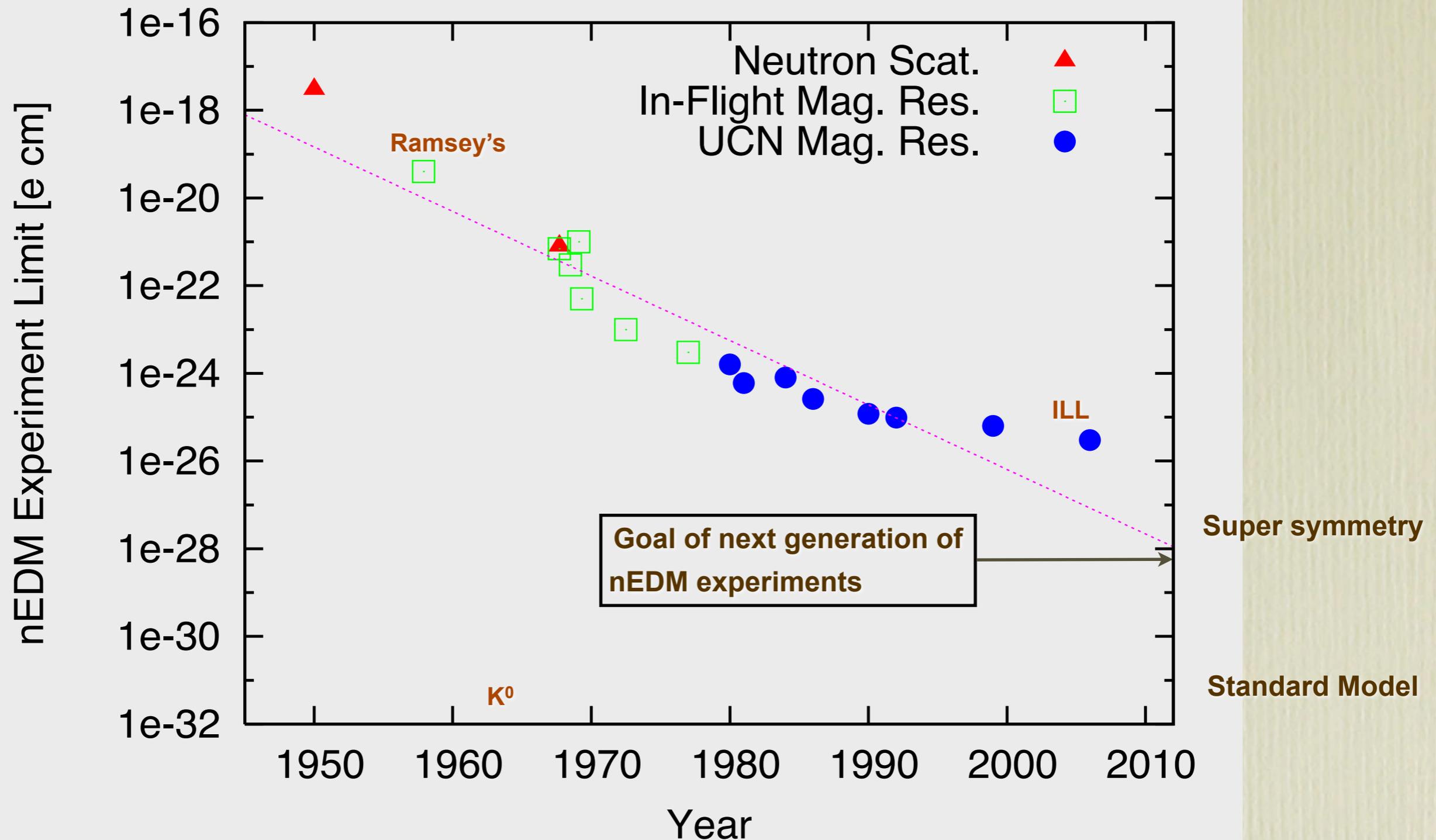


**Maskawa**

# Neutron EDM in Standard Model

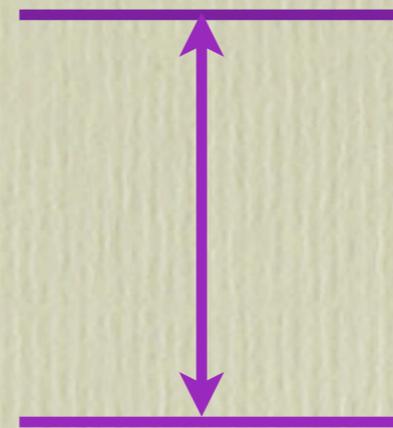
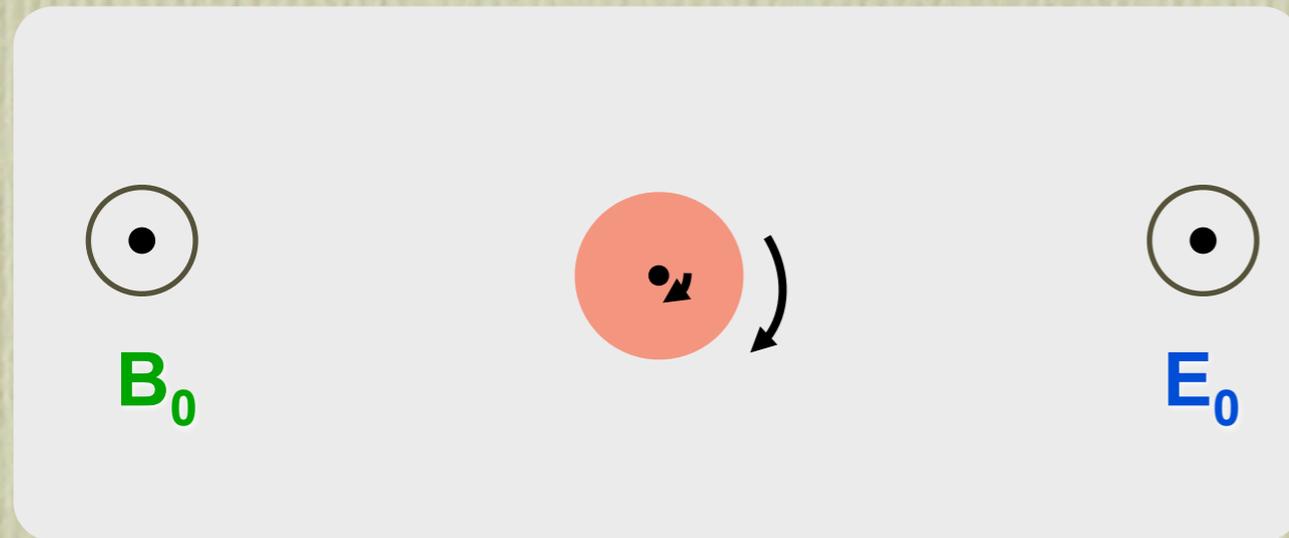
- Upper limit of neutron EDM ( $d_n$ )  $\sim 3 \times 10^{-26}$  e cm.
- Neutron EDM in Standard Model
  - **Strong interaction:**  $d_n \sim \theta \times 10^{-15}$  e cm, where  $\theta$  specifies the magnitude of CP violation in the QCD Lagrangian ( $\theta < 10^{-10}$ ).
  - **Weak interaction:** Phase in CKM matrix:  $d_n \sim 10^{-31}$  e cm
- Neutron EDM provides a strong constraint for new theories predicting CP violation.
- The neutron EDM searches can explore physics beyond SM complementary to LHC.

# History of neutron EDM search



- Current neutron EDM upper limit:  $< 2.9 \times 10^{-26}$  e cm (90% C.L.)
- Still no evidence for neutron EDM.

# How to measure neutron EDM?



$$B_0 \uparrow E_0 \uparrow$$

$$\hbar\omega = 2(\mu_n B_0 + d_n E_0)$$

- Measure the **precession frequency** of neutron in  $B_0$  and  $E_0$ .
- **Flip  $E_0$** , get nEDM from precession frequency difference.

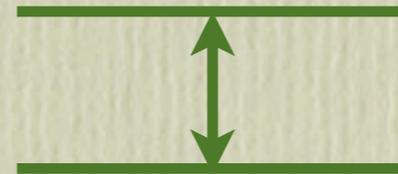
$$H = -(\vec{\mu}_n \cdot \vec{B}_0 + \vec{d}_n \cdot \vec{E}_0)$$

$$\vec{\mu}_n = \gamma_n \vec{S}, \quad \vec{d}_n = d_n \hat{S}$$

$$\rightarrow \omega = \gamma_n B_0 \pm 2d_n E_0 / \hbar$$

$$\rightarrow \Delta\omega = 4d_n E_0 / \hbar$$

# How to measure neutron EDM?



$$B_0 \uparrow \quad E_0 \downarrow$$

$$\hbar\omega = 2(\mu_n B_0 - d_n E_0)$$

- Measure the **precession frequency** of neutron in  $B_0$  and  $E_0$ .
- **Flip  $E_0$** , get nEDM from precession frequency difference.

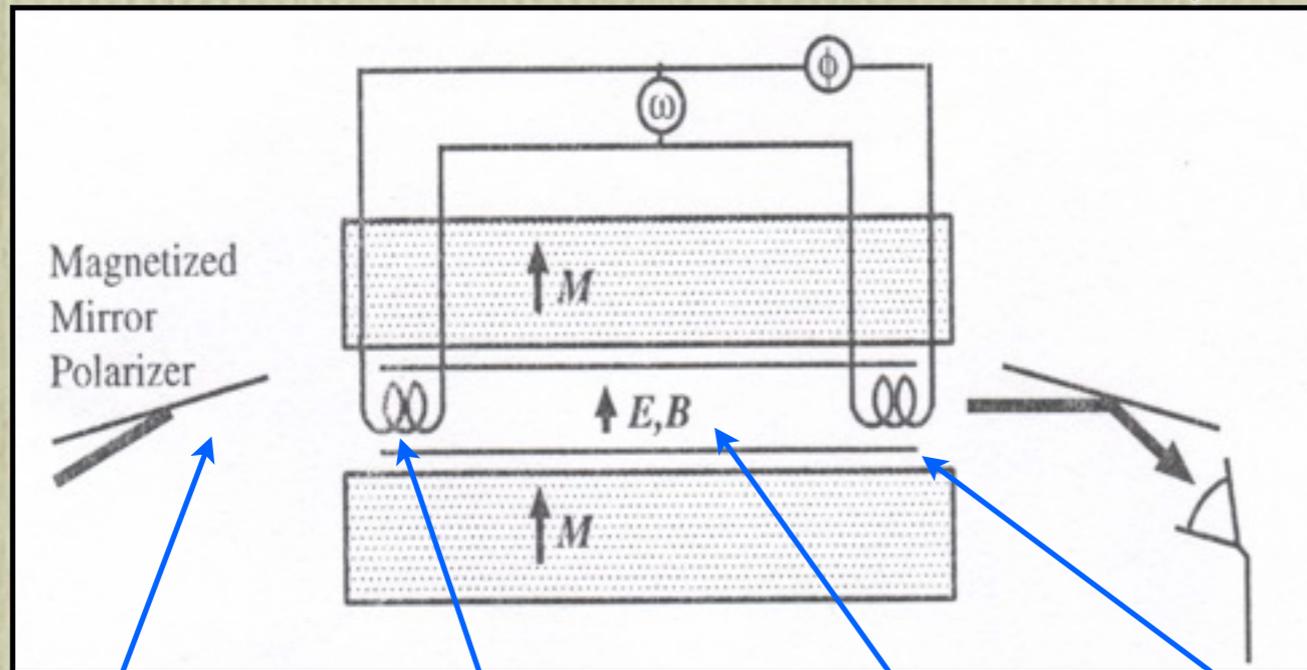
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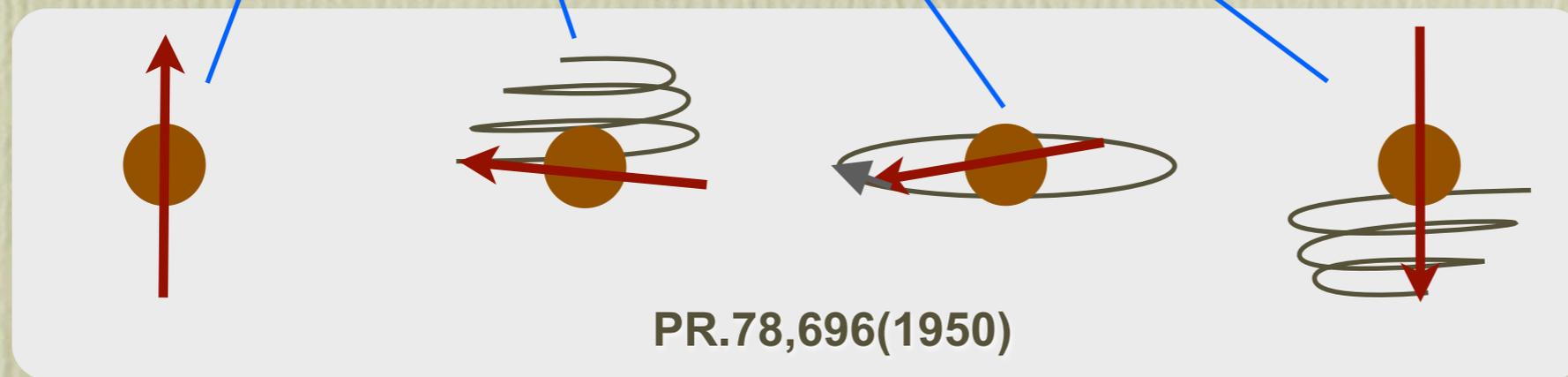
# Purcell and Ramsey's experiment



- Table-size experiment using **separated oscillatory fields method**.

- PR.108,120(1957):

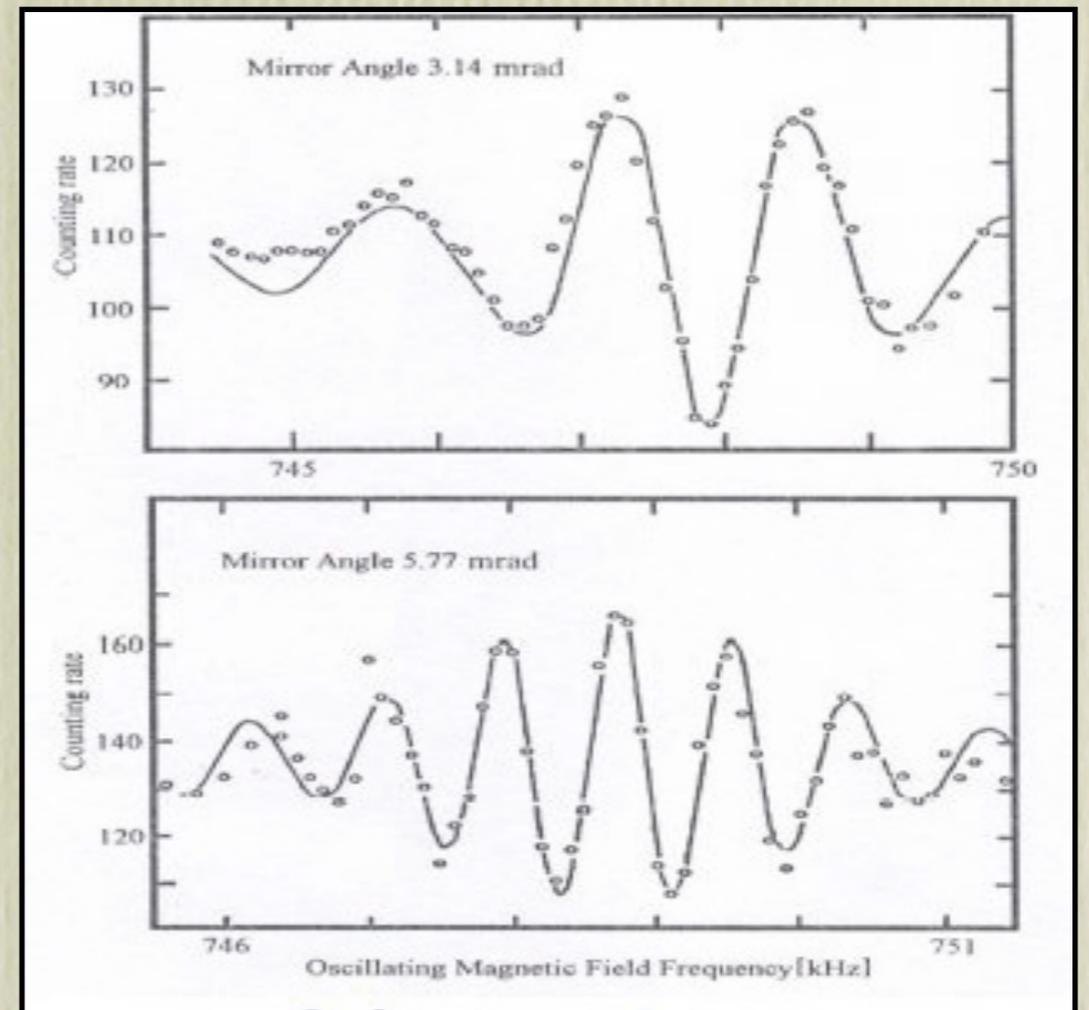
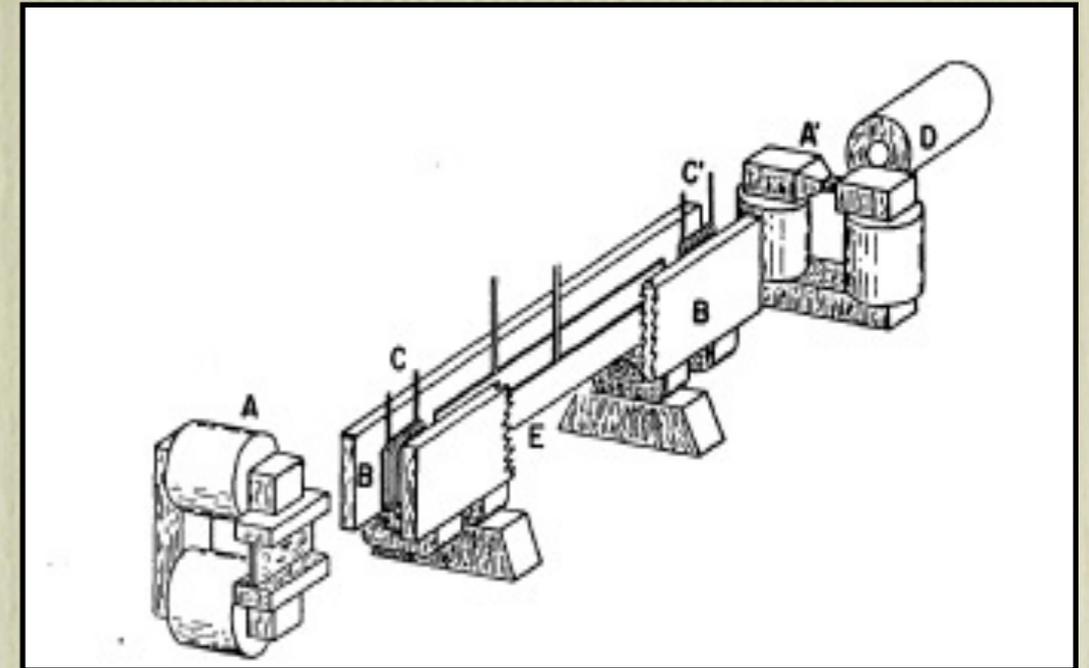
$$d_n < 5 \times 10^{-20} \text{ e cm}$$



RF	off	on	off	on
	neutron spin is parallel to holding field	first $\pi/2$ pulse is applied; spin is rotated to be perpendicular to holding field	neutrons precess in B and E	second $\pi/2$ pulse is applied; spin is rotated to be anti-parallel to holding field

# Purcell and Ramsey's experiment

- The peak location determines the precession frequency.
- Limitations:
  1. **Short duration** for observing the precession ( $\sim 1$  ms) due to short transit time of cold neutron beam in this region
  2. Systematic error due to **motional magnetic field** ( $\mathbf{v} \times \mathbf{E}$ )
- Both can be improved by using **ultracold neutrons (UCN)** due to their slow velocities ( $\sim 5$  m/s)



# Ultracold neutron (UCN)



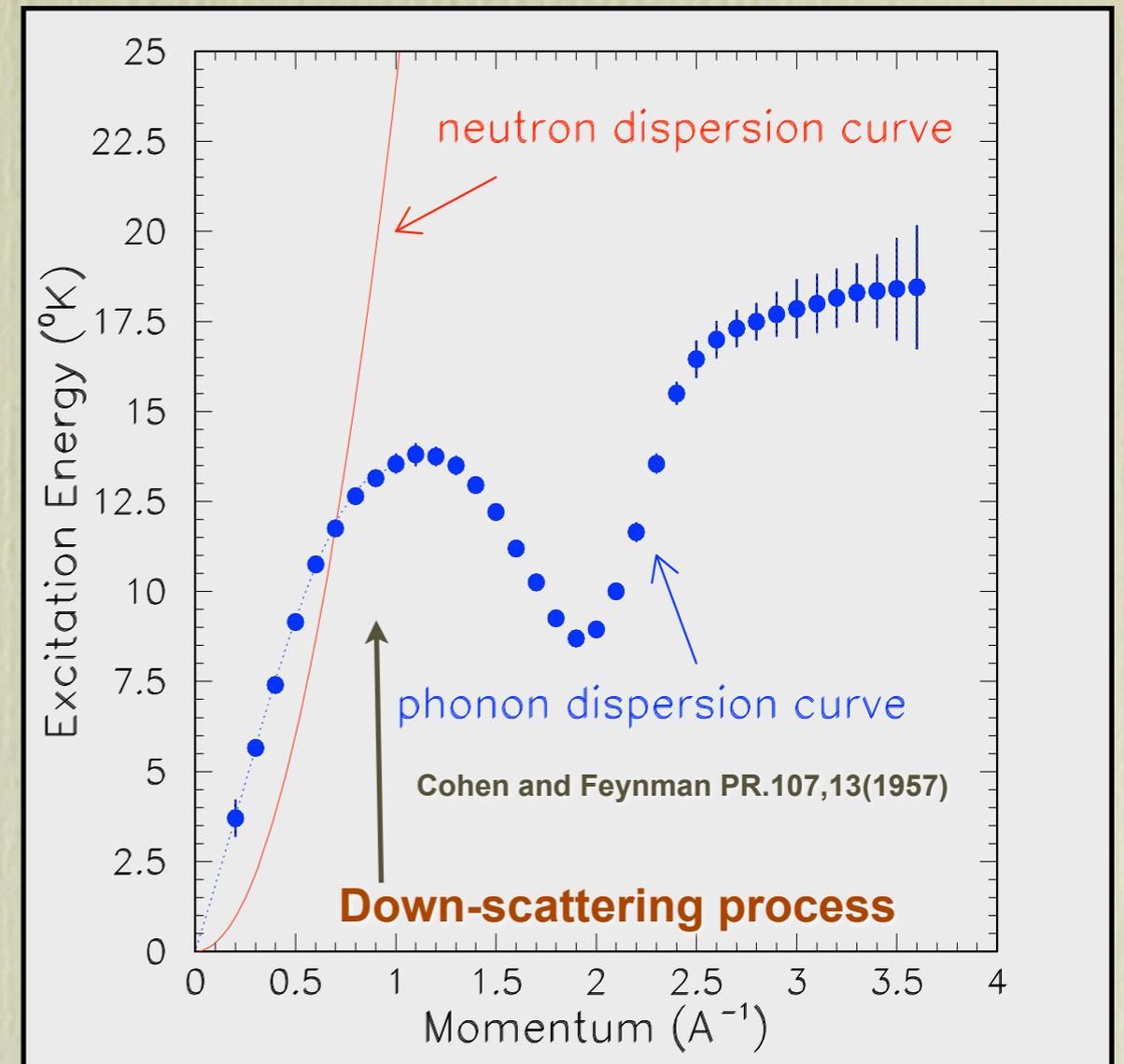
Fermi

- Fermi suggested that neutrons with very low energy can be stored in a bottle(1936).
- Many materials provide repulsive **Fermi potential  $U_F$**  around order of **200 neV** for neutrons.
- If neutron energy is *less* than the Fermi potential  $U_F$ , neutrons can be stored in a bottle.
- $U_F \sim 200$  neV, UCNs have velocities of order of 5 m/sec, wavelengths of order 500 °A and an effective temperature of order 2 mK.
- **Long storage time, low velocity.**
- Many experiments with UCN, like neutron life time measurement, **neutron EDM**, gravitational interactions of neutrons,etc.

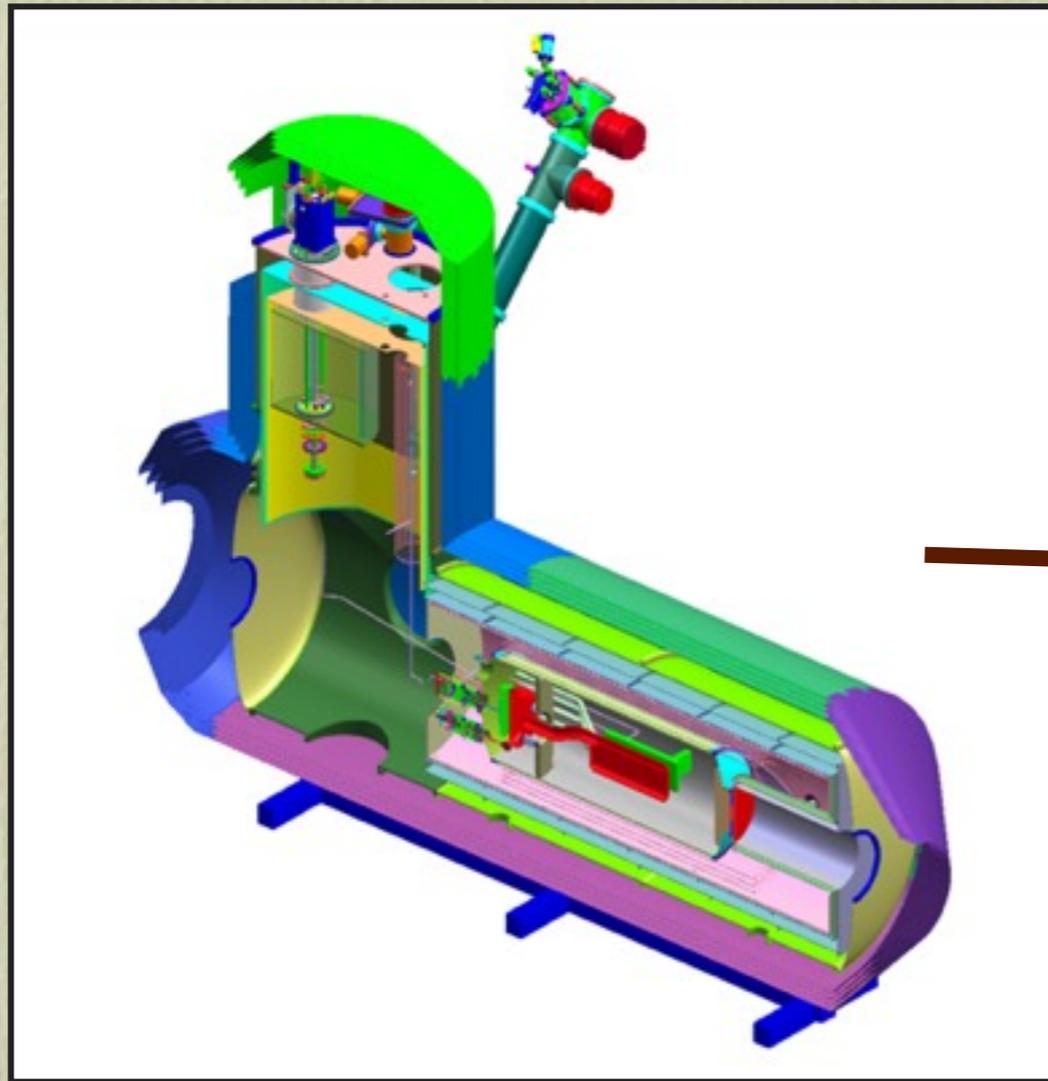
# UCN production in superfluid $^4\text{He}$

- UCN was extracted from the **low-energy tail** of the Maxwell-Boltzmann distribution of cold neutrons ( $\sim 5 \text{ UCN/cm}^3$ ).
- A method was suggested by Golub and Pendlebury. Cold neutron with momentum of  $0.7 \text{ \AA}^{-1}$  ( $10^{-3} \text{ eV}$ ) can excite a phonon in superfluid  $^4\text{He}$  and become an UCN via **down-scattering process**.

**=> Much larger UCN density than conventional UCN sources**



# The new neutron EDM experiment (based on UCN production in superfluid $^4\text{He}$ )



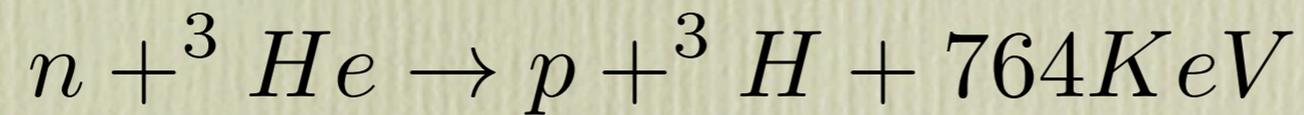
( Based on the idea originated by R. Golub and S. Lamoreaux in 1994 )

Collaboration:

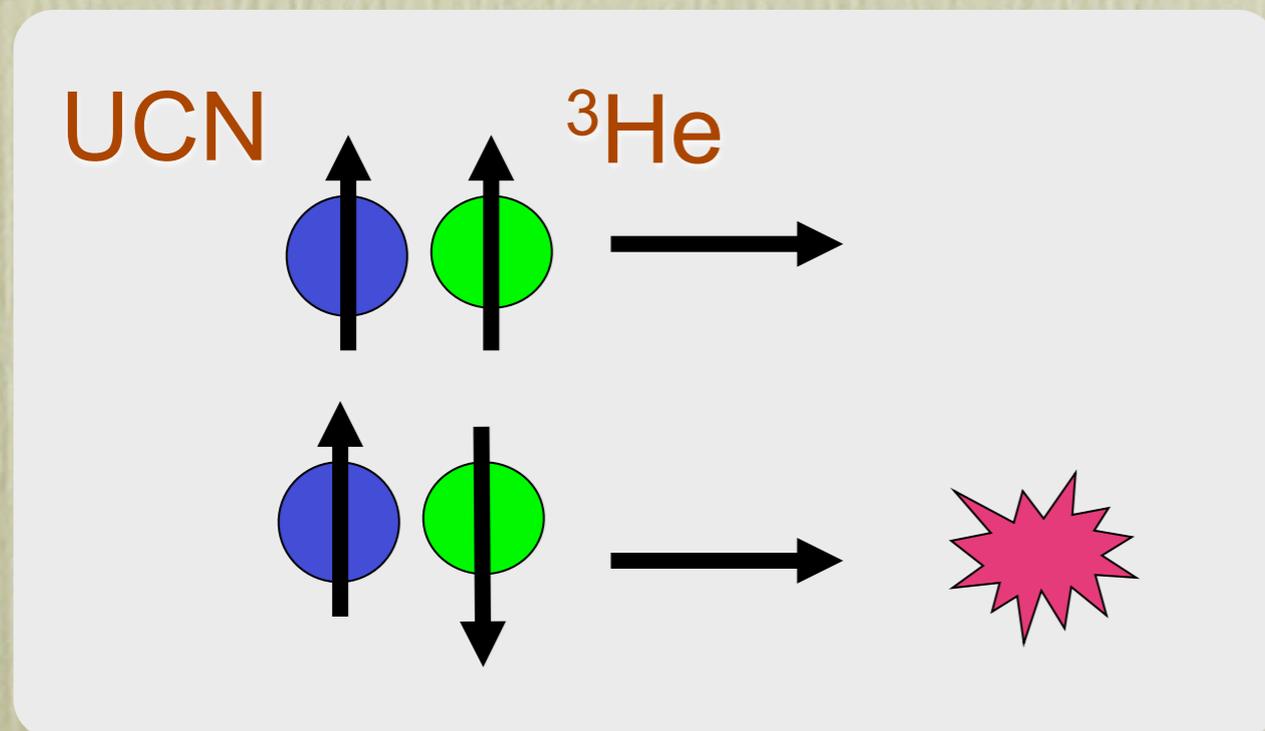
Arizona State, Berkeley, Brown, Boston, Caltech, Duke, Indiana, Illinois, Kentucky, LANL, Maryland, MIT, Mississippi State, NCSU, ORNL, Simon-Fraser, Tennessee, Virginia, Valparaiso, Yale

# How to measure the precession of UCN in superfluid $^4\text{He}$ ?

- Use polarized  $^3\text{He}$  in the bottle as a spin analyzer.



- n –  $^3\text{He}$  absorption is strongly spin-dependent.

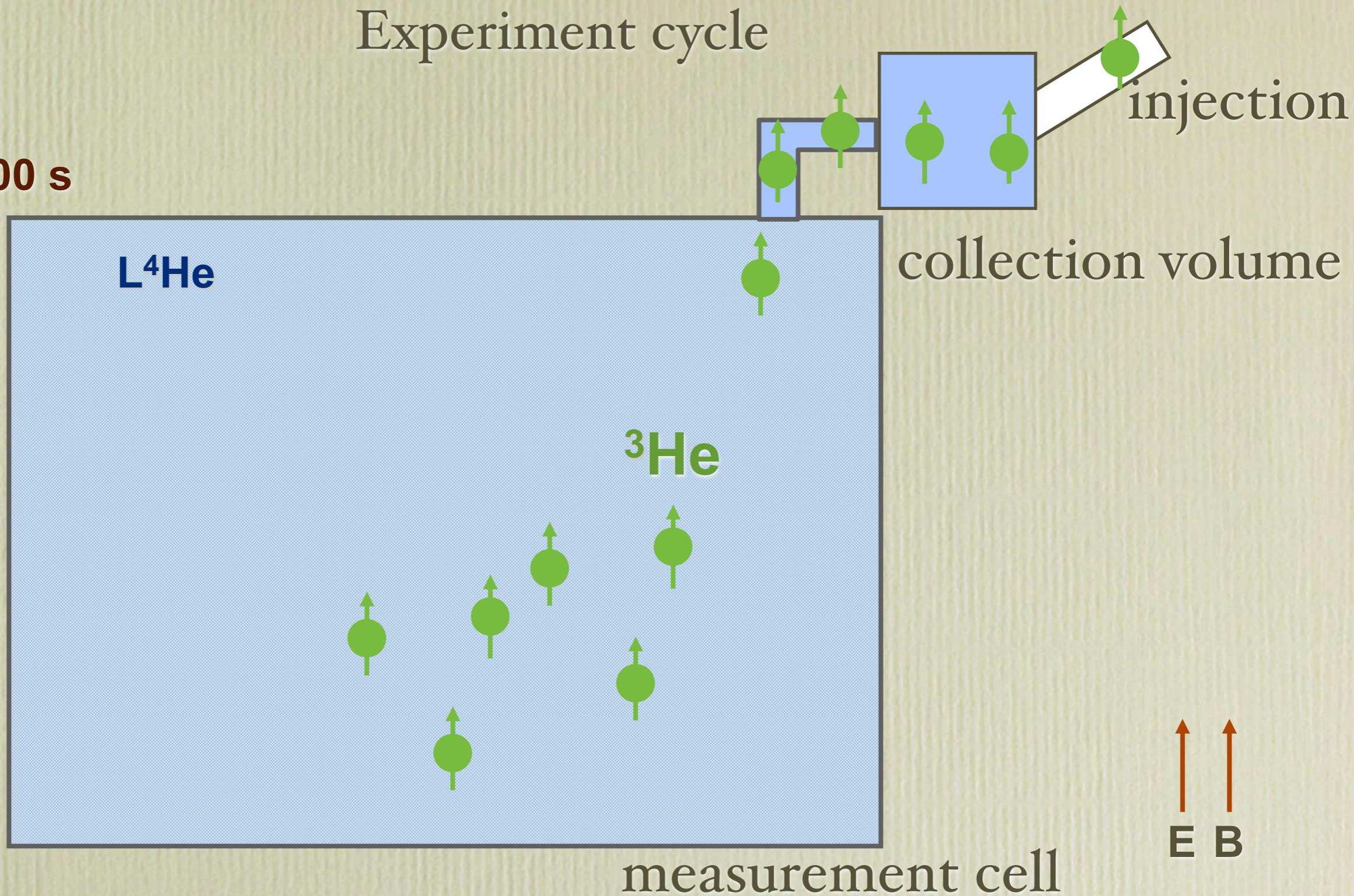


$$J=1, \sigma \sim 0$$

$$J=0, \sigma_{\text{abs}} \sim 4.8 \times 10^6 \text{ barns for } v=5 \text{ m/s}$$

# Experiment cycle

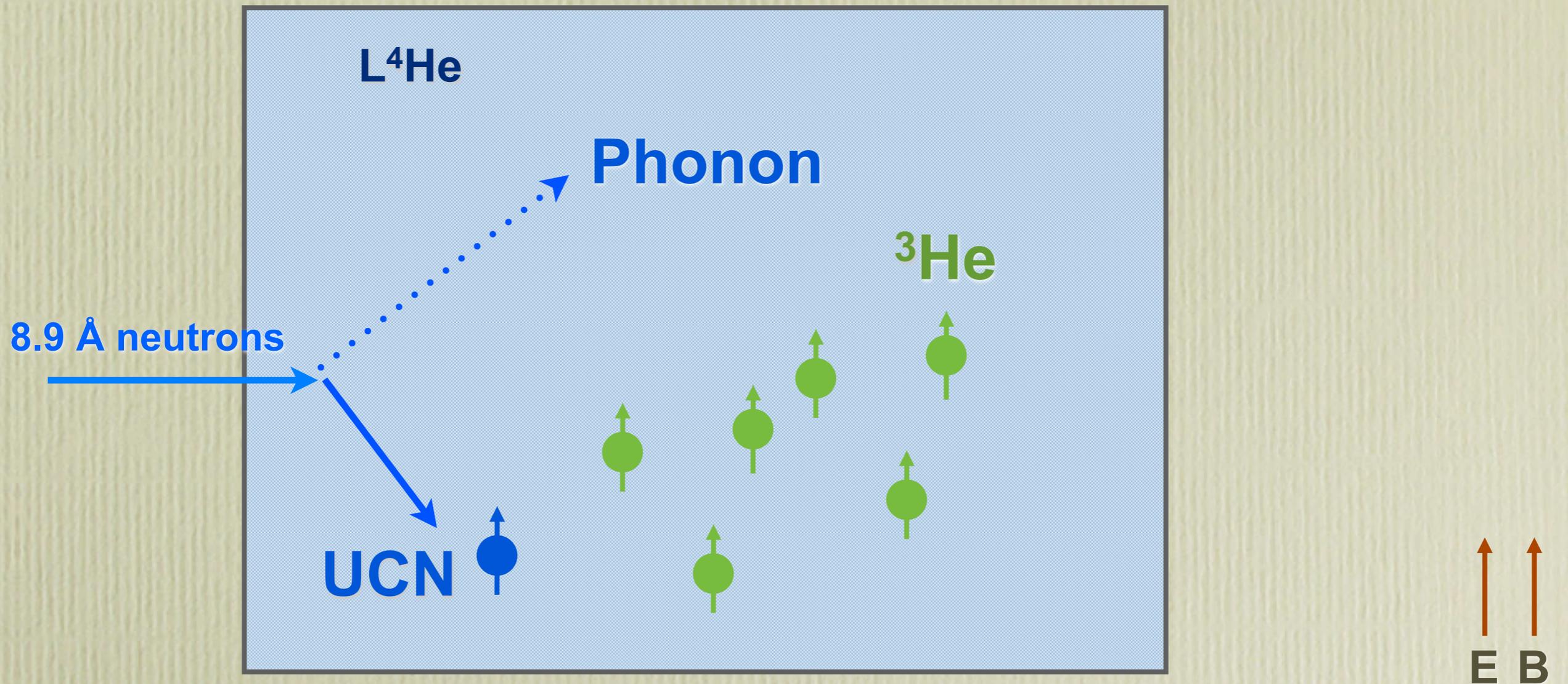
$T = 0 - 100 \text{ s}$



Fill  $L^4\text{He}$  with polarized  $^3\text{He}$

# Experiment cycle

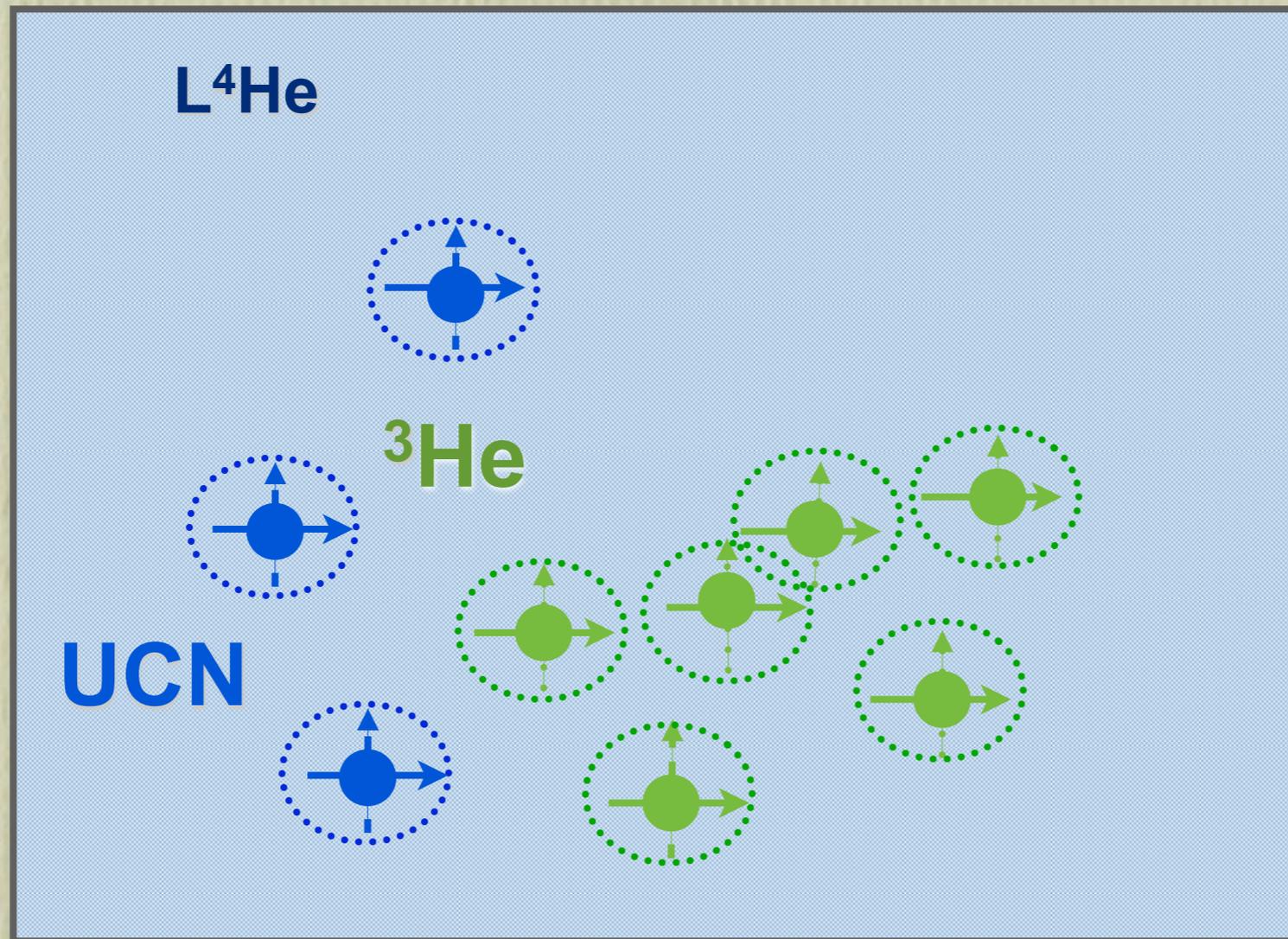
$T = 100 - 1100 \text{ s}$



Produce polarized UCNs with polarized cold neutron beam

# Experiment cycle

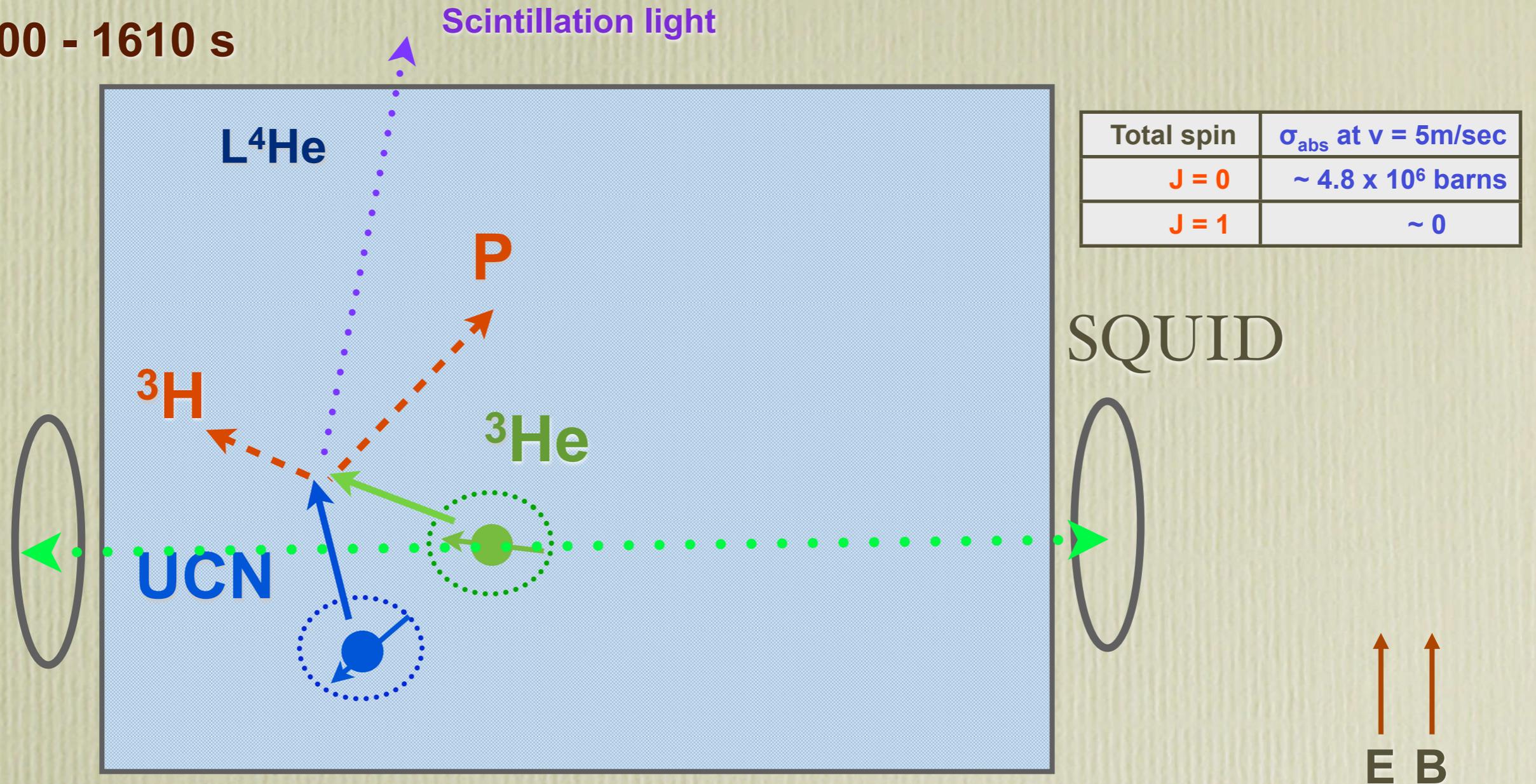
**T = 1100 s**



Flip neutron and <sup>3</sup>He spins by a  $\pi/2$  RF coil

# Experiment cycle

$T = 1100 - 1610 \text{ s}$



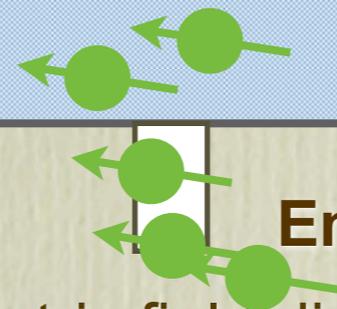
- UCN and  $^3\text{He}$  precess in a uniform B field ( $\sim 10\text{mG}$ ) and a strong E field ( $\sim 50\text{KV/cm}$ ). Measure the precession of  $^3\text{He}$  by using SQUID.
- Detect **scintillation light** from the reaction  $n + ^3\text{He} \rightarrow p + t$  (and from other sources, including neutron beta decays)

•  $\theta_{n3}$  is the relative angle between neutron and  $^3\text{He}$ .

$$\frac{d\phi(t)}{dt} = N_0 e^{-\Gamma_{\text{tot}} t} \left[ \frac{1}{\tau_\beta} + \frac{1}{\tau_3} (1 - P_3 P_n \cos(\theta_{n3})) \right]$$

# Experiment cycle

**T = 1610 - 1710 s**



**Empty Line**

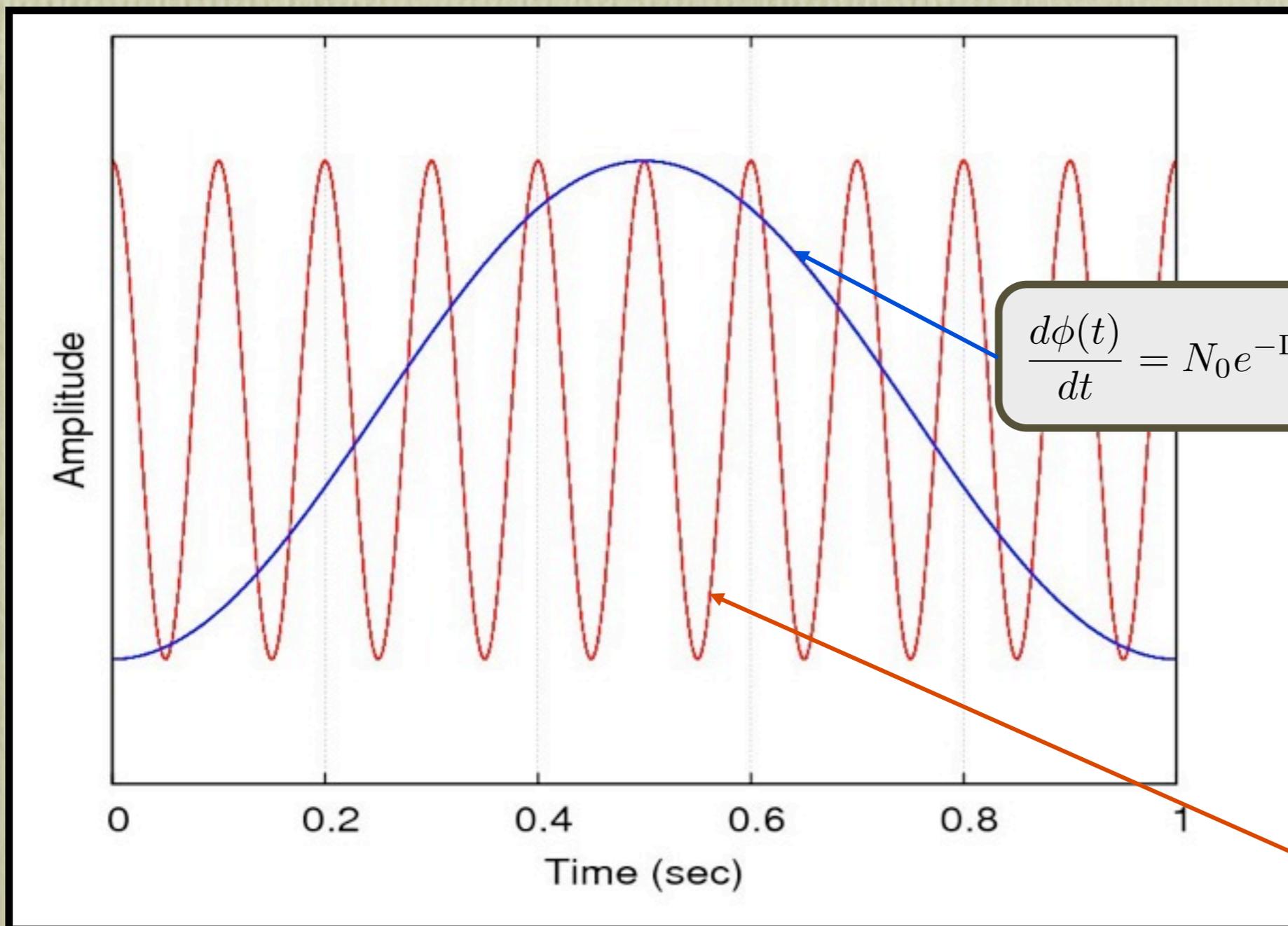


Empty the  $^3\text{He}$  by using heat flush, change the electric field direction periodically and repeat the measurement

# Two oscillatory signals

- Scintillation light from  $n + {}^3\text{He} \rightarrow p + t$  with  $\omega_\gamma = (\gamma_n - \gamma_3)B_0 \pm 2d_n E_0/\hbar$  where the relative angle  $\theta_{n3} = \omega_\gamma t$ .
- SQUID signal from the precession of  ${}^3\text{He}$  with  $\omega_3 = \gamma_3 B_0$ .
- Thus, the precession of neutron can be known well.

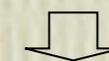
**comagnetometer:**  
reduce the error caused by  $B_0$   
instability between measurements



**Scintillation signal**

$$\frac{d\phi(t)}{dt} = N_0 e^{-\Gamma_{tot} t} \left[ \frac{1}{\tau_\beta} + \frac{1}{\tau_3} (1 - P_3 P_n \cos(\theta_{n3})) \right]$$

$$\gamma_3 \approx 1.1 \gamma_n$$

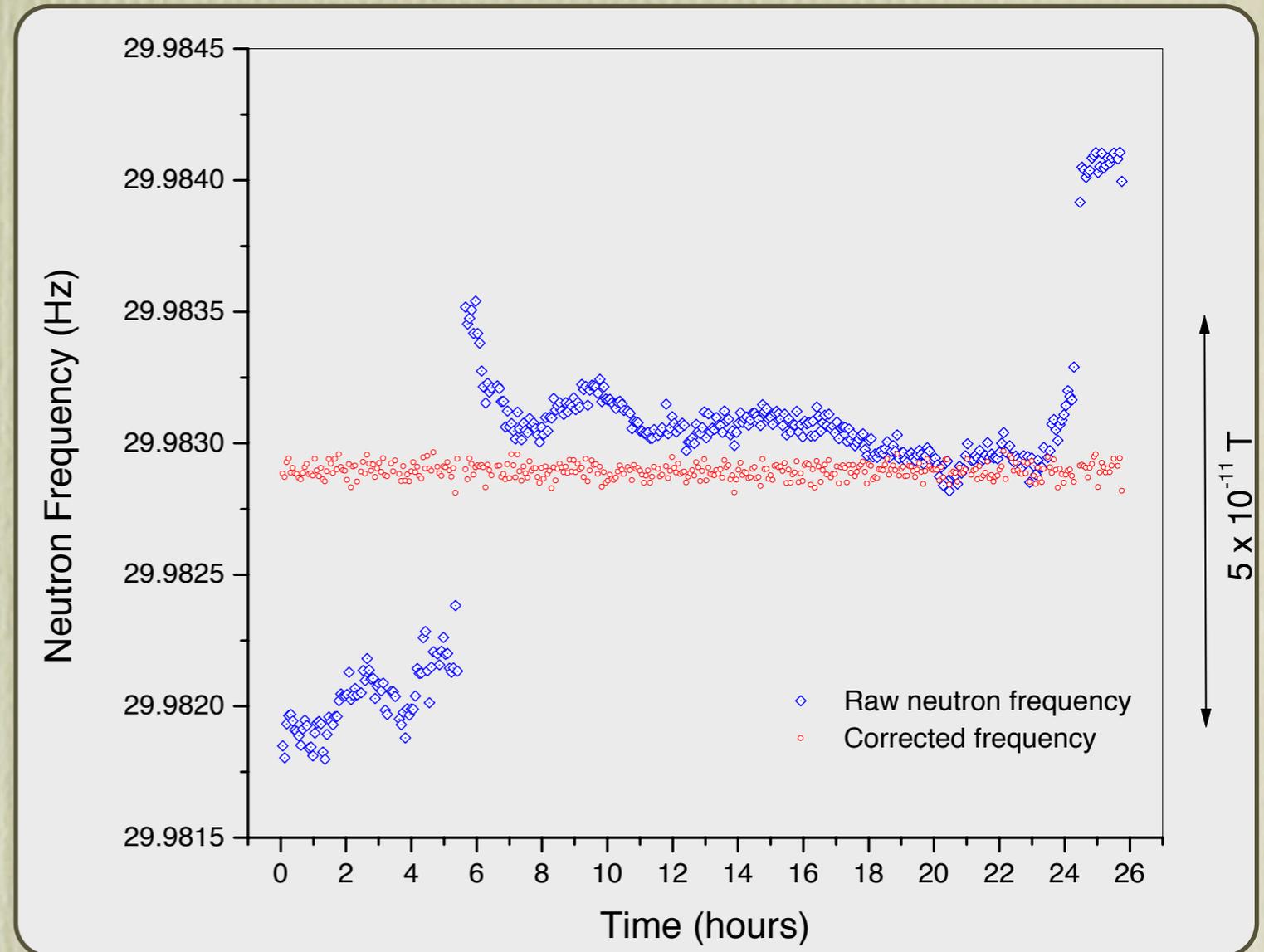


SQUID frequency is ~10  
times higher than  
scintillation frequency

**SQUID signal**

# Application of comagnetometer

- The idea is to add a **polarized atomic species** to precess with neutrons.
- **The drift of the holding field** can be monitored by measuring the precession of the comagnetometer.
- $^{199}\text{Hg}$  was applied as a comagnetometer in ILL experiment (Phys.Rev.Lett. 97 (2006) 131801:  $d_n < 2.9 \times 10^{-26}$  e cm). But it *cannot* be used in liquid  $^4\text{He}$ .
- $^3\text{He}$  will be used for the new neutron EDM experiment in liquid  $^4\text{He}$  at the SNS.



# Dressed spin in nEDM

- Neutrons and  $^3\text{He}$  naturally precess at different frequencies (different g factors)
- Applying a RF field (dressing field),  $B_d \cos(\omega_d t)$ , perpendicular to the constant  $B_0$  field, the effective g factors of neutrons and  $^3\text{He}$  will be **modified** (dressed spin effect)
- At a **critical dressing field**, the effective g factors of neutrons and  $^3\text{He}$  can be made **identical!**

$$\omega_\gamma = (\gamma_n - \gamma_3)B_0 \pm 2d_n E_0 / \hbar \rightarrow \pm 2d_n E_0 / \hbar$$

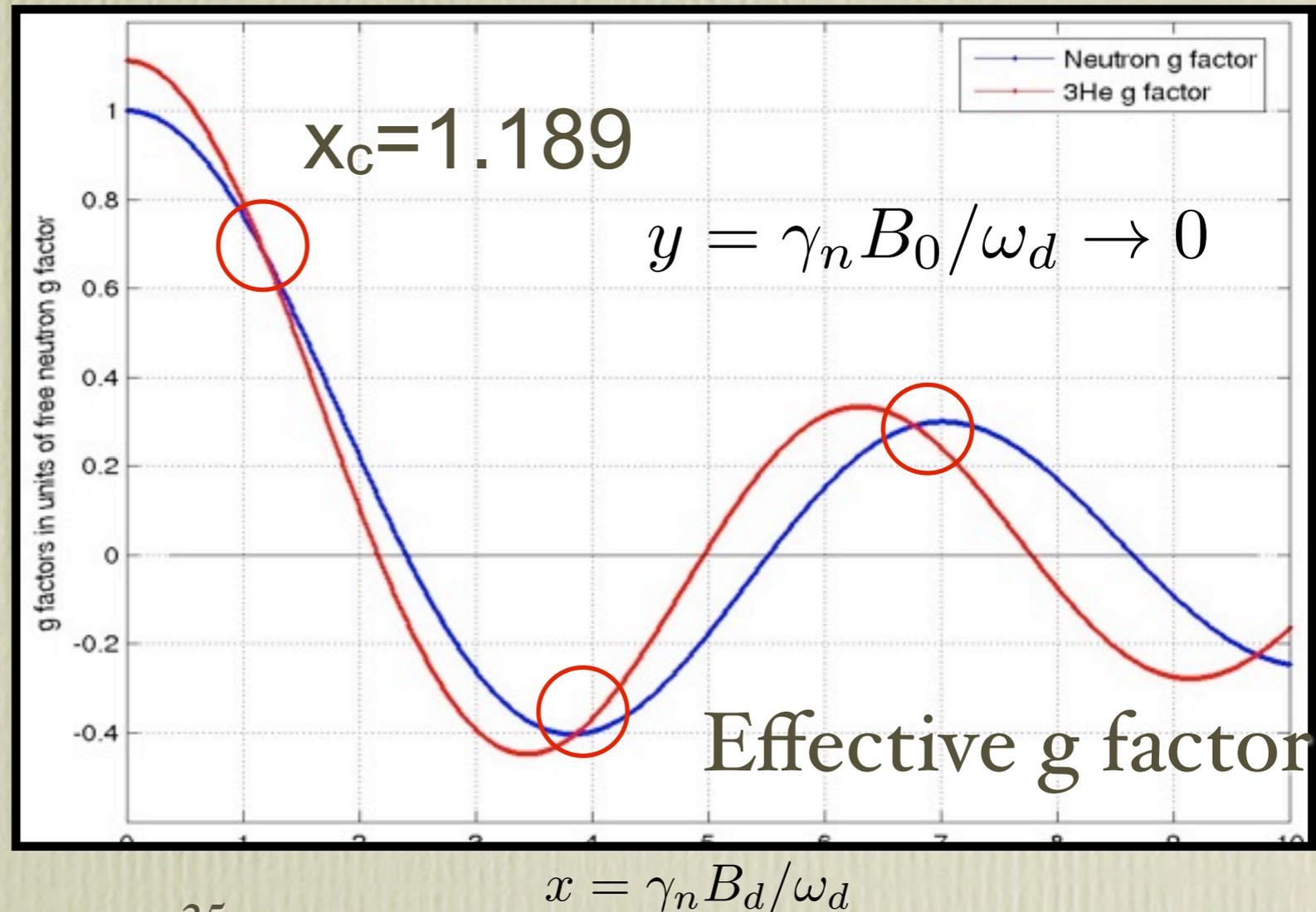
# Critical dressing of neutron and $^3\text{He}$

- The Larmor frequency is given as  $\omega_{Larmor} = \omega_0 = \gamma B_0$
- $\gamma$  is modified by the dressing field at the high frequency limit as  $\gamma' = \gamma J_0(x)$
- The critical dressing is  $\gamma'_n = \gamma'_3$
- Thus  $J_0(x_c) = a J_0(ax_c)$
- $a = \gamma_3/\gamma_n \approx 1.1$
- The proposal value is  $B_0 = 10 \text{ mG}$ ,  
 $x = 1.189$ ,  
 $y = 0.01$ .

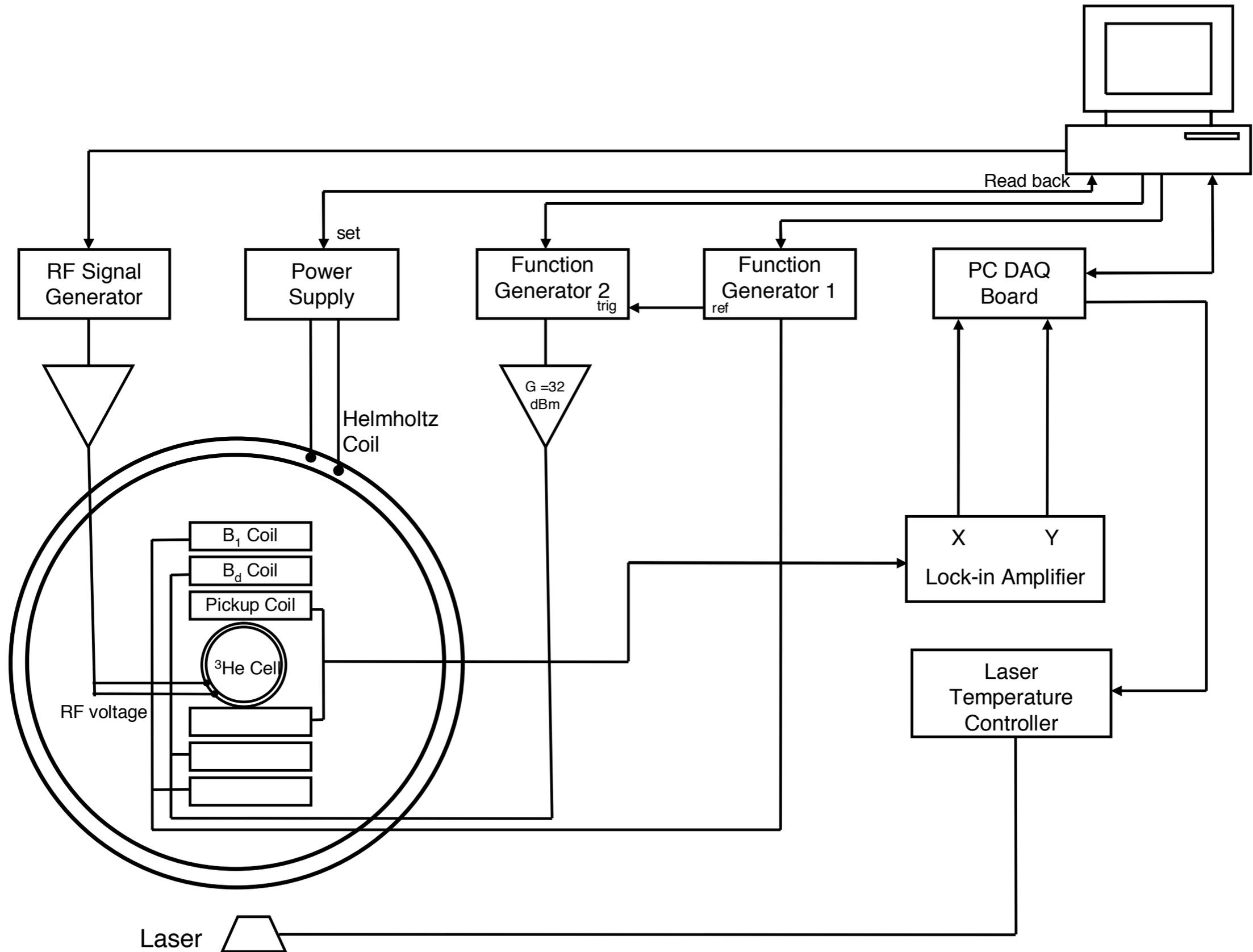
$$x \equiv \frac{\gamma_n B_d}{\omega_d}$$

$$y \equiv \frac{\gamma_n B_0}{\omega_d}$$

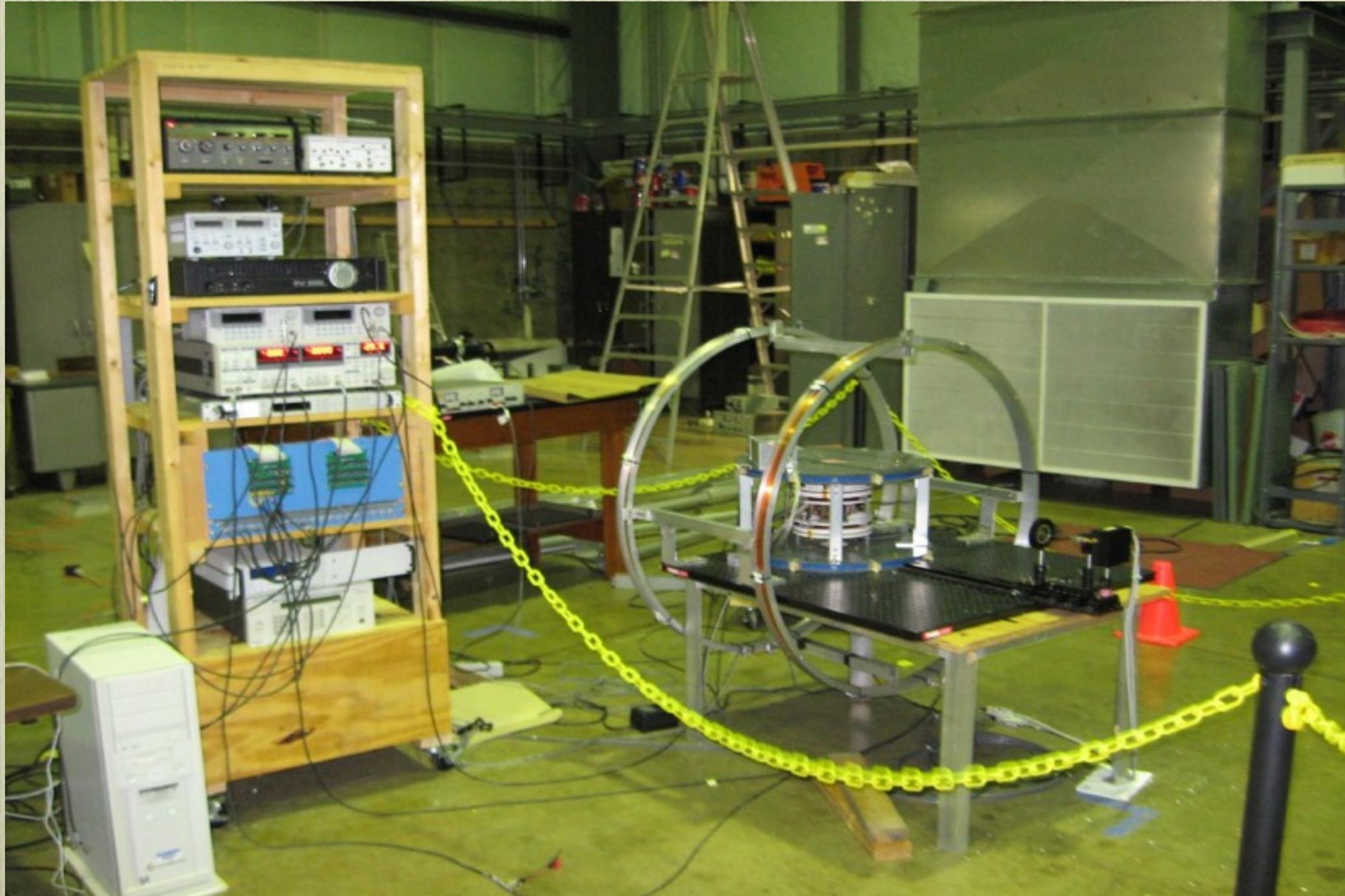
The goal of the UIUC measurement is to explore the dressed spin effect of polarized  $^3\text{He}$  as a function of  $B_0$ ,  $B_d$  and  $\omega_d$  in a cell.



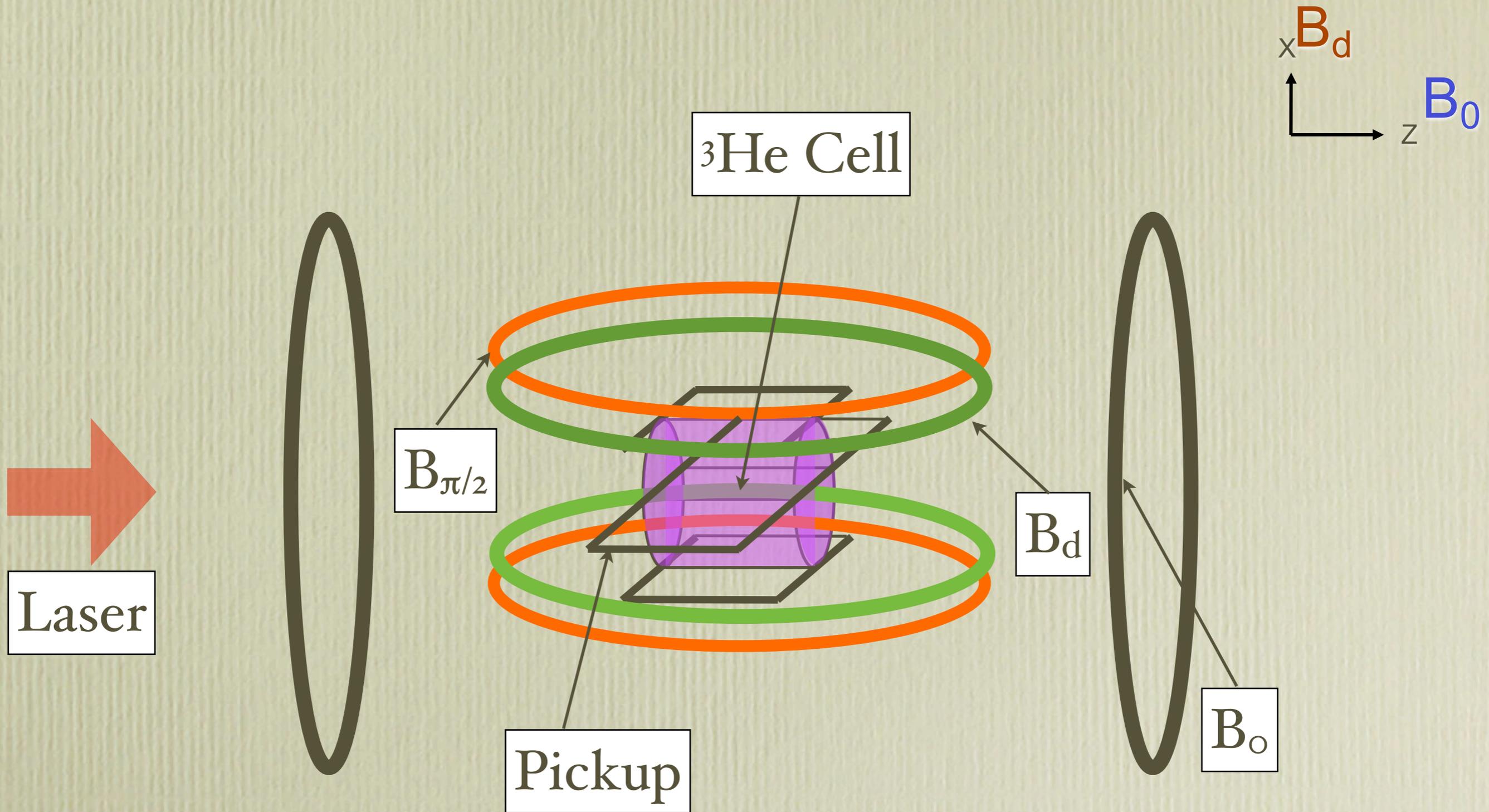
# Experimental setup



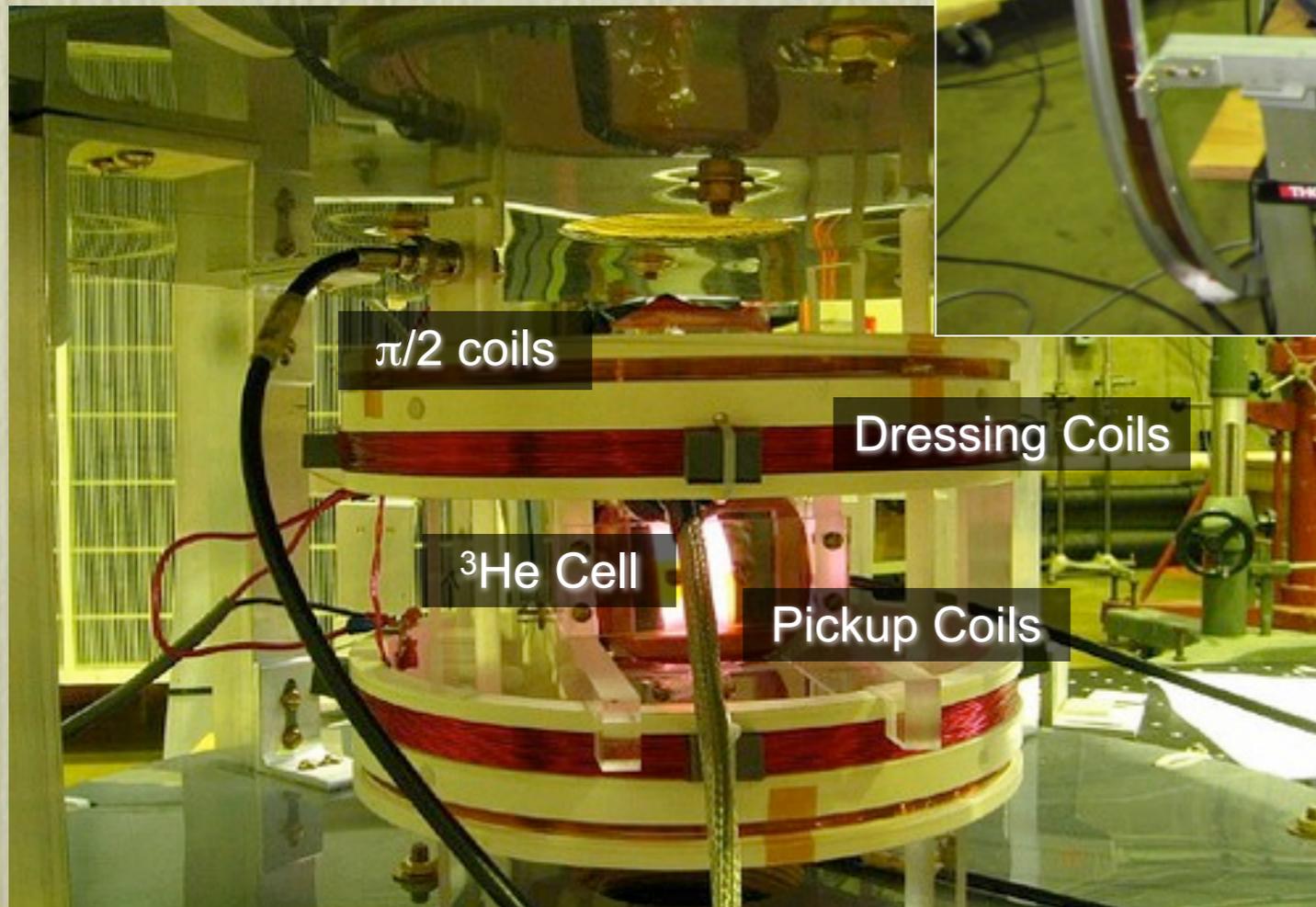
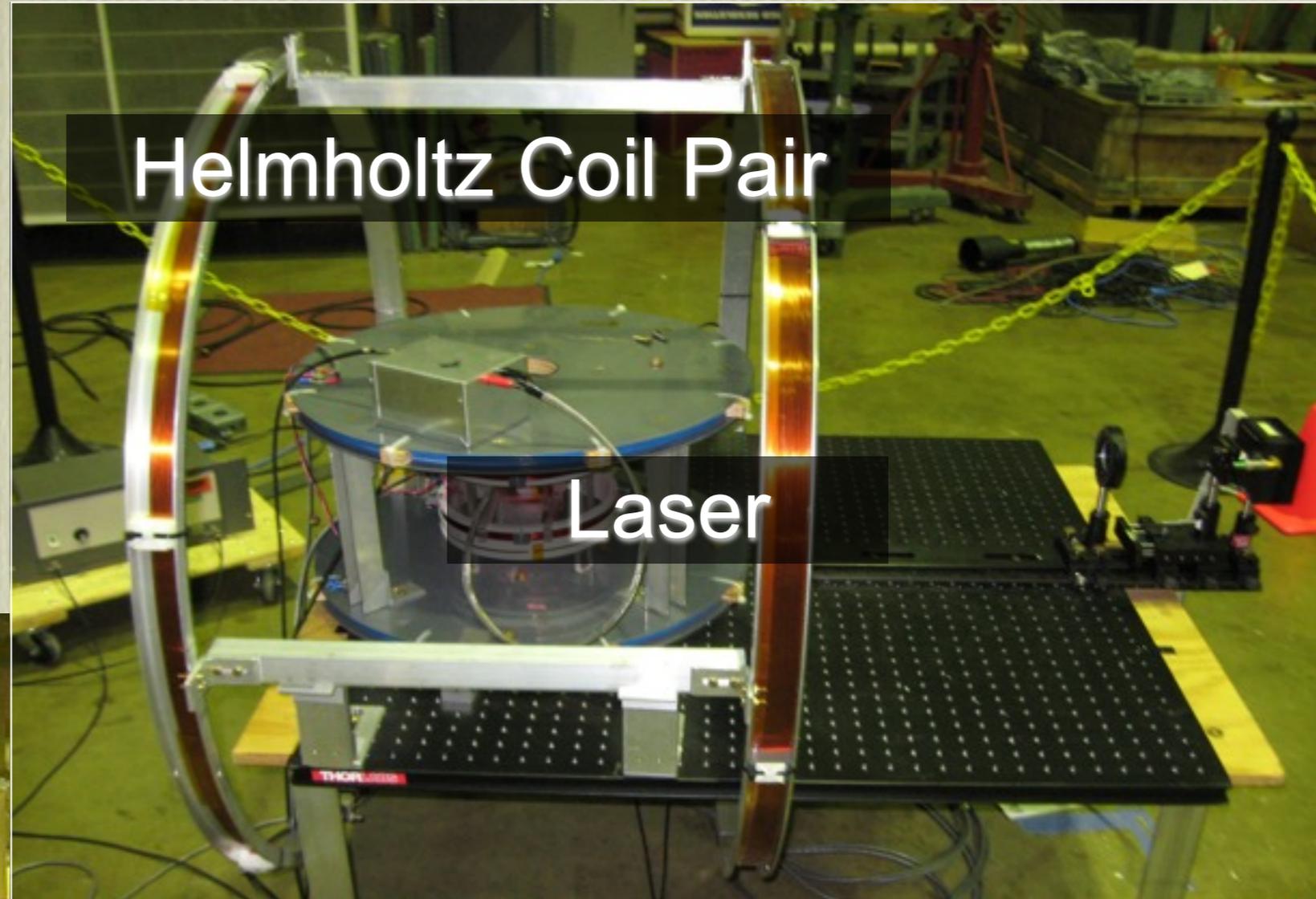
# Experimental setup



# Experimental setup

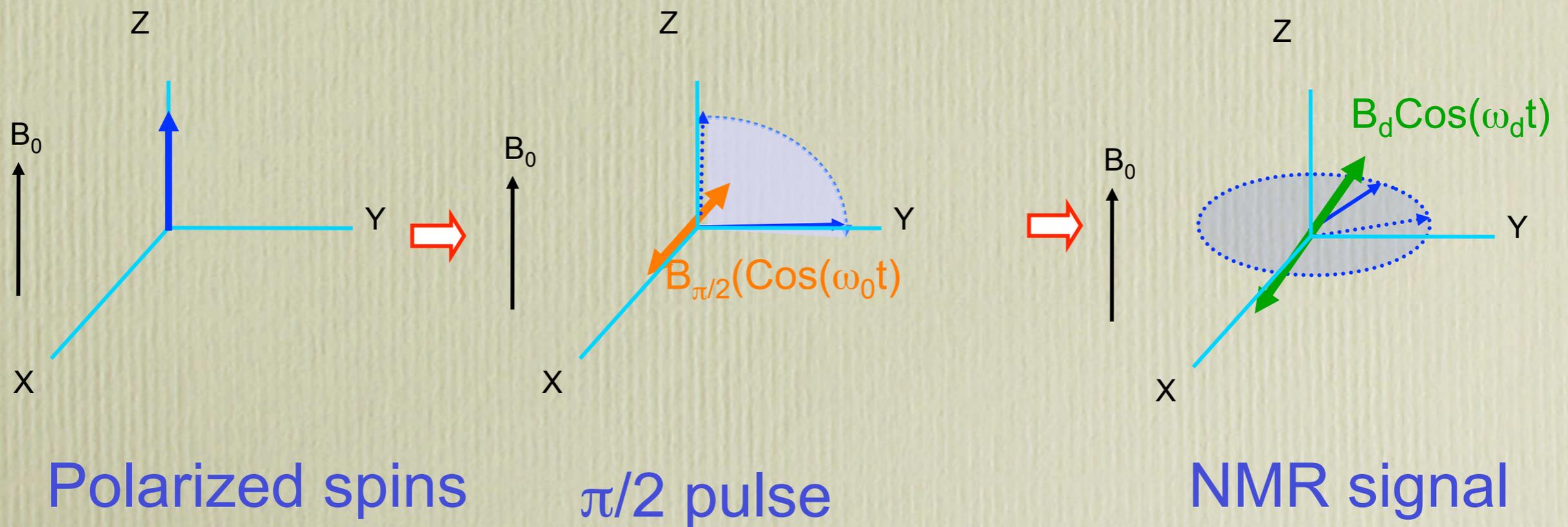


# Experimental setup



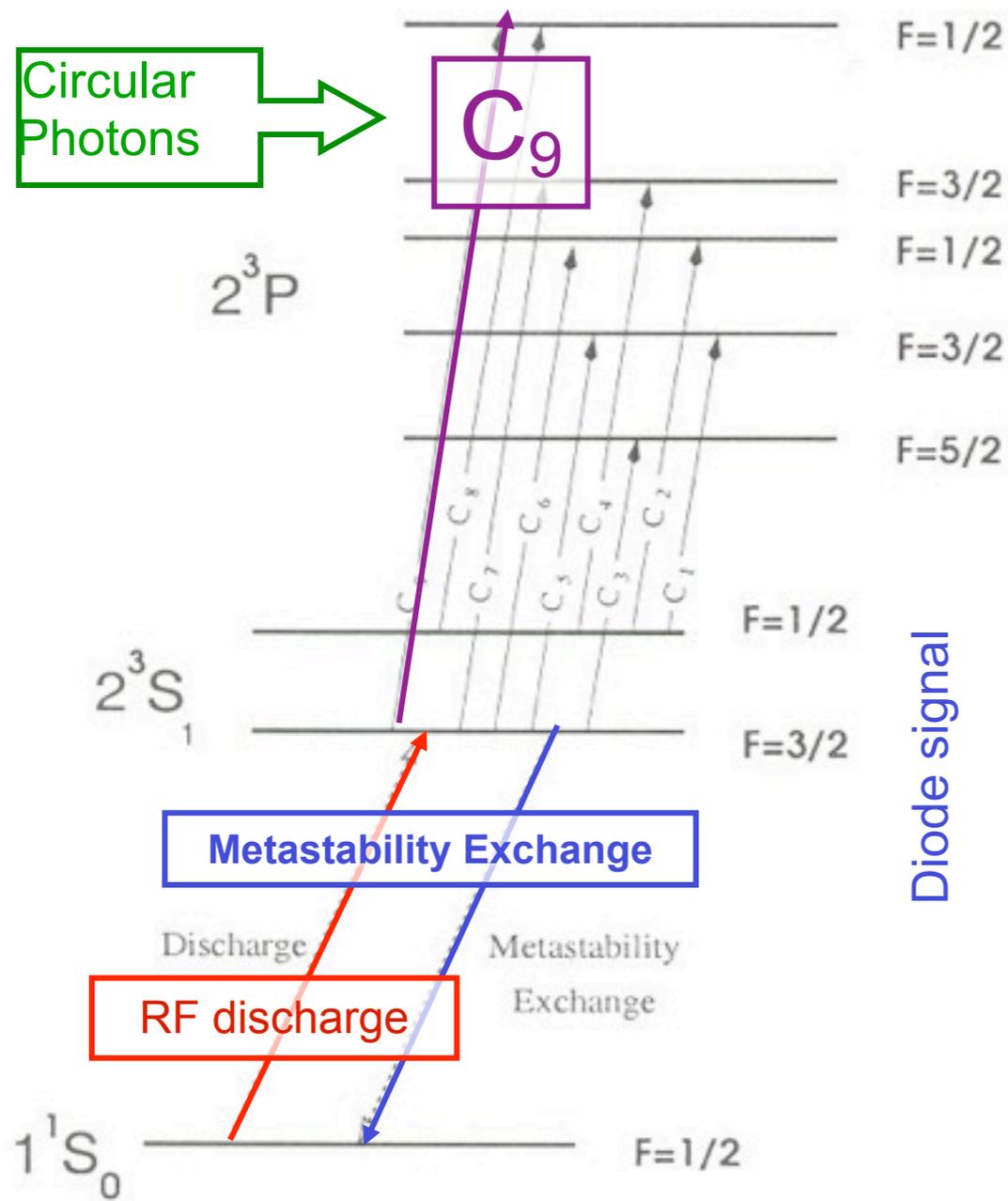
# Experimental steps

- Polarize  $^3\text{He}$  nuclear spins. (Metastability exchange with optical pumping) (by **Laser** and  $\mathbf{B}_0$ )
- $\pi/2$  pulse to rotate the spin to x-y plane. (by  $\mathbf{B}_{\pi/2}\mathbf{Cos}(\omega_0 t)$ )
- Apply a dressing field,  $\mathbf{B}_d\mathbf{Cos}(\omega_d t)$ , and measure precession frequency by the **pickup coils** and **Lock-in amplifier**.

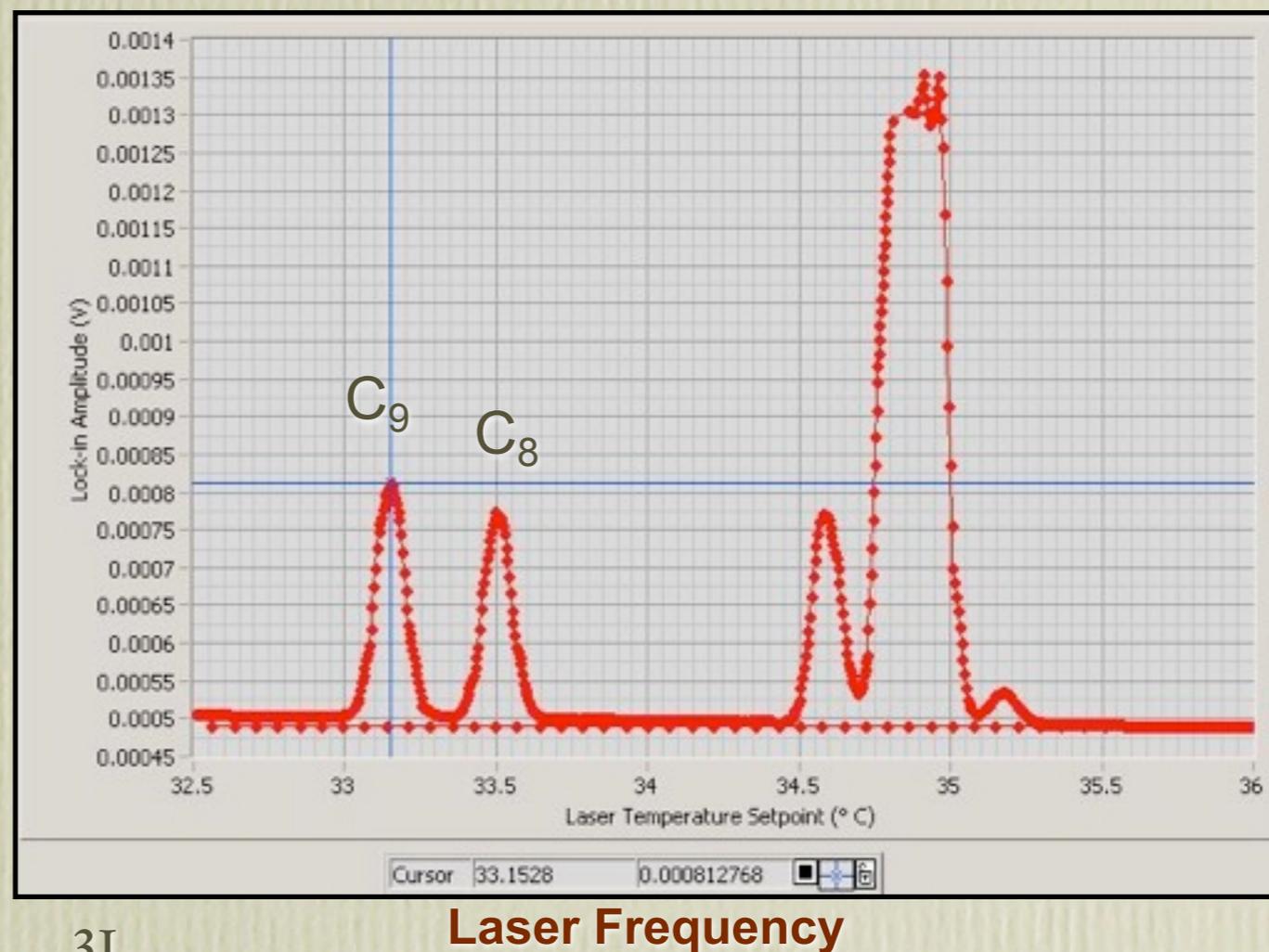
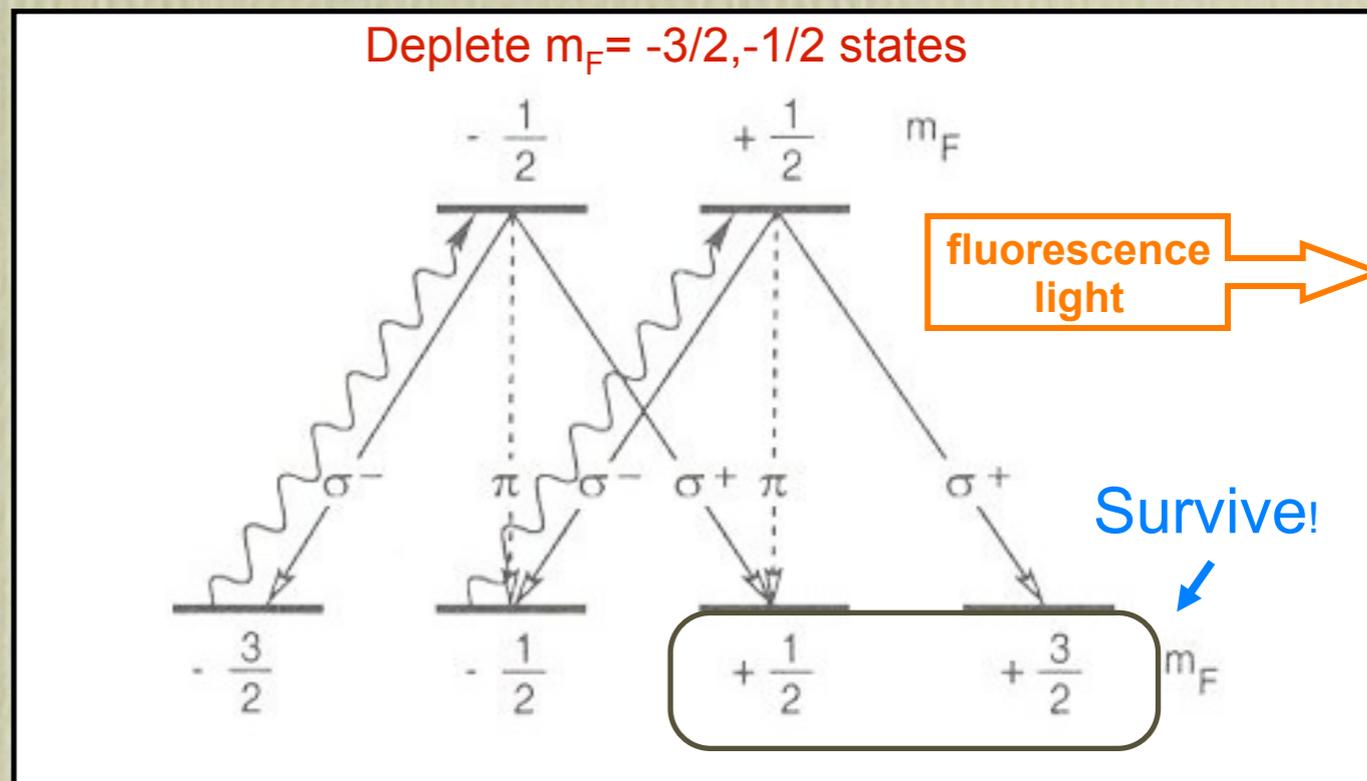


# Polarize $^3\text{He}$ with metastability exchange

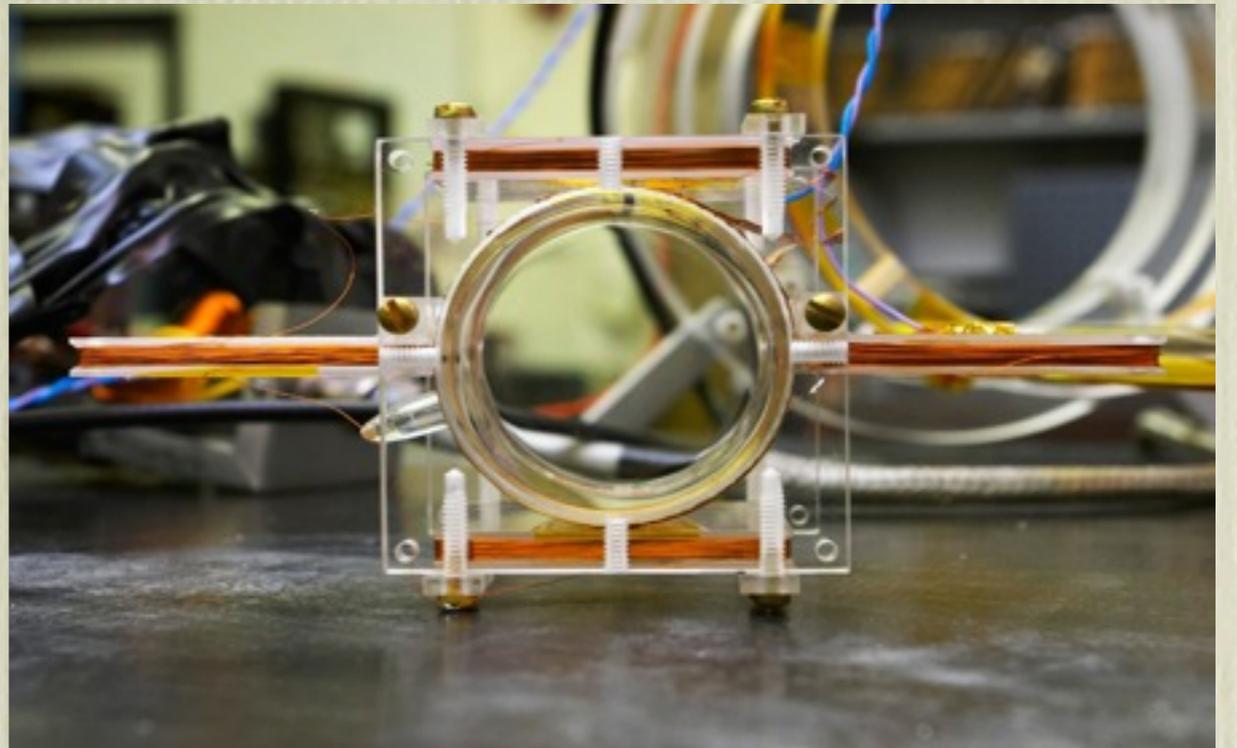
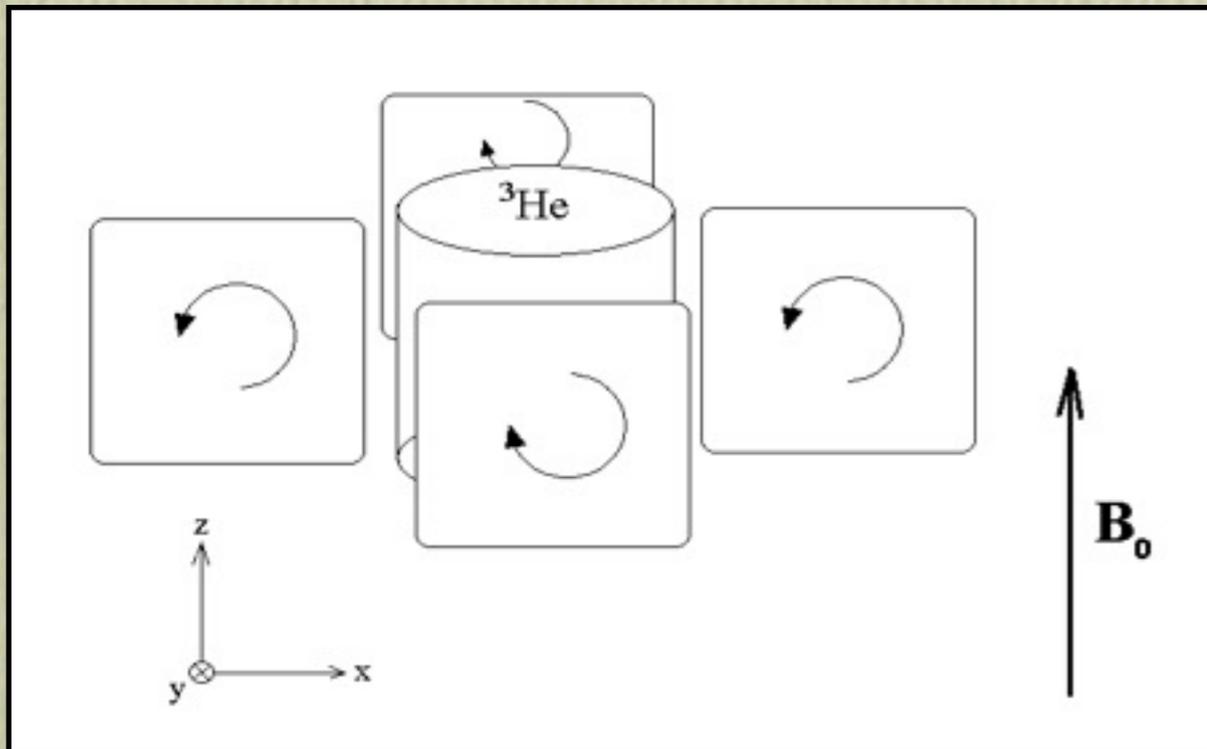
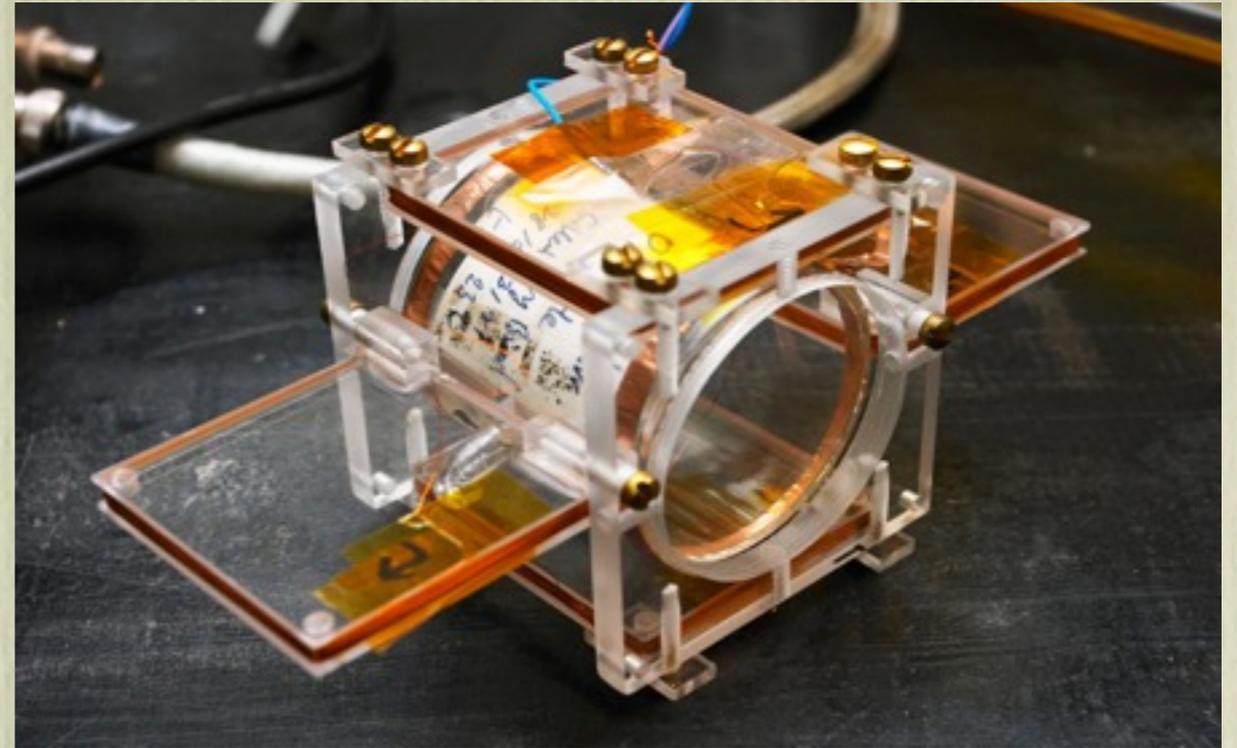
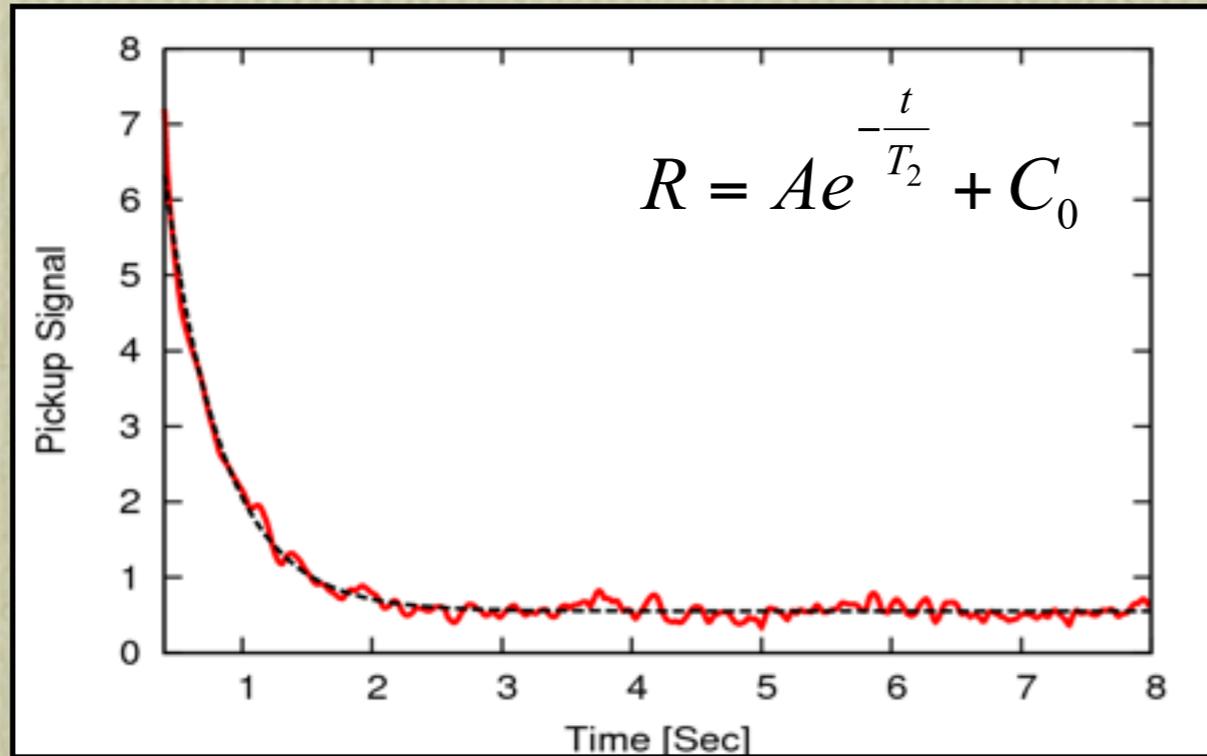
## Optical Pumping



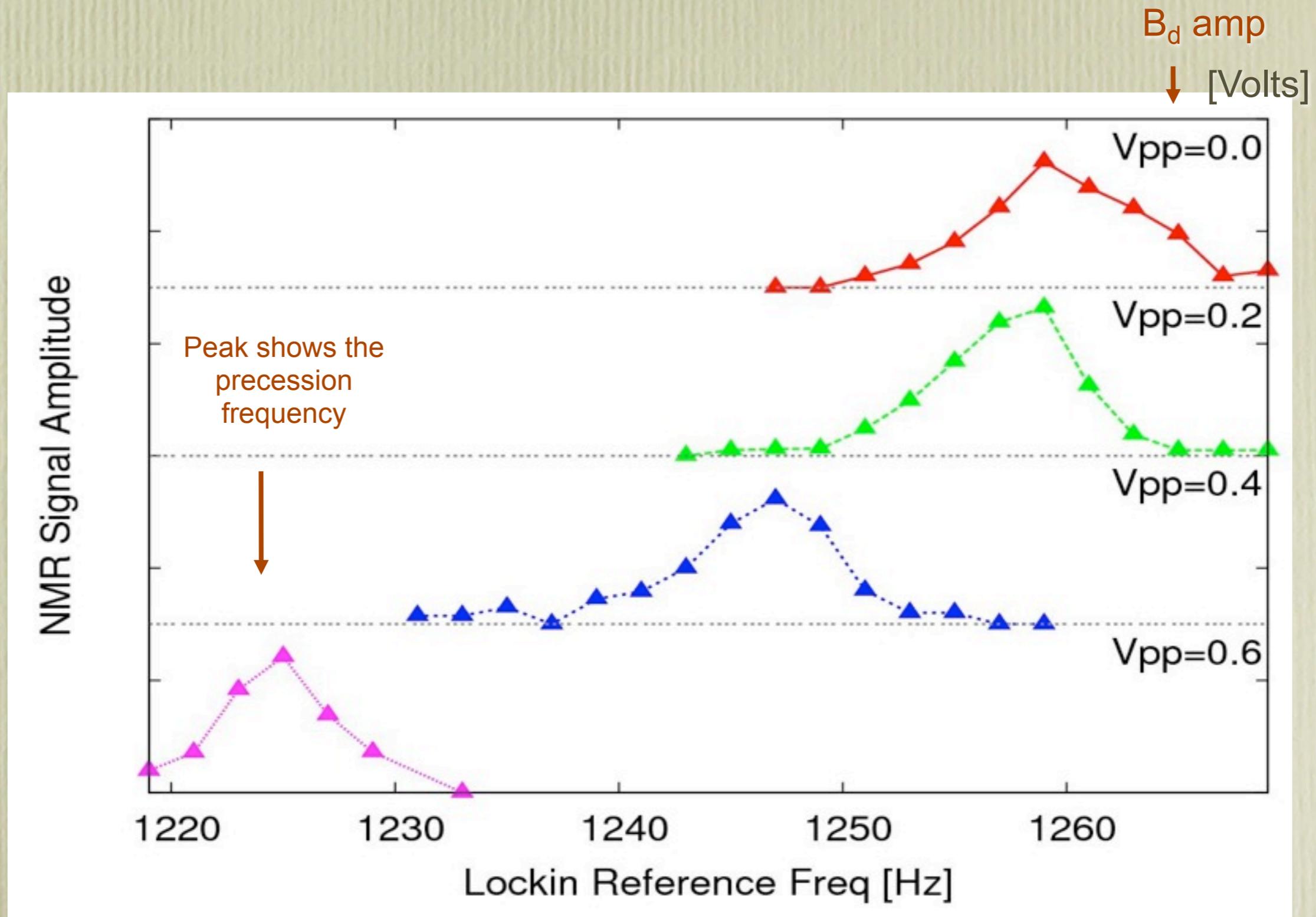
- 1) Transfer angular momentum of photon to atomic electrons
- 2) produce nuclear polarization via metastability exchange



# Pickup coils signal

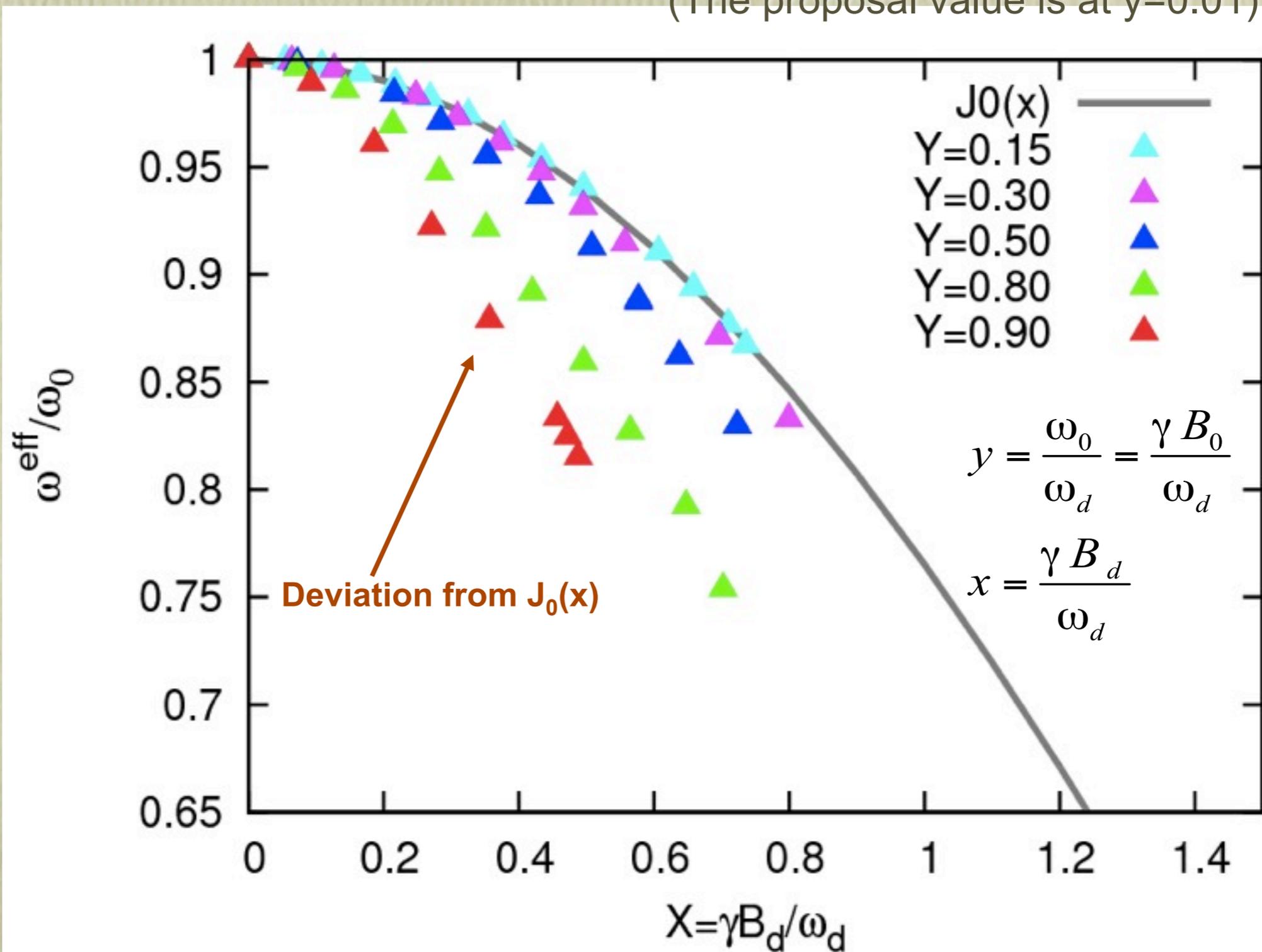


# Precession frequency measurement by using Lock-in amplifier



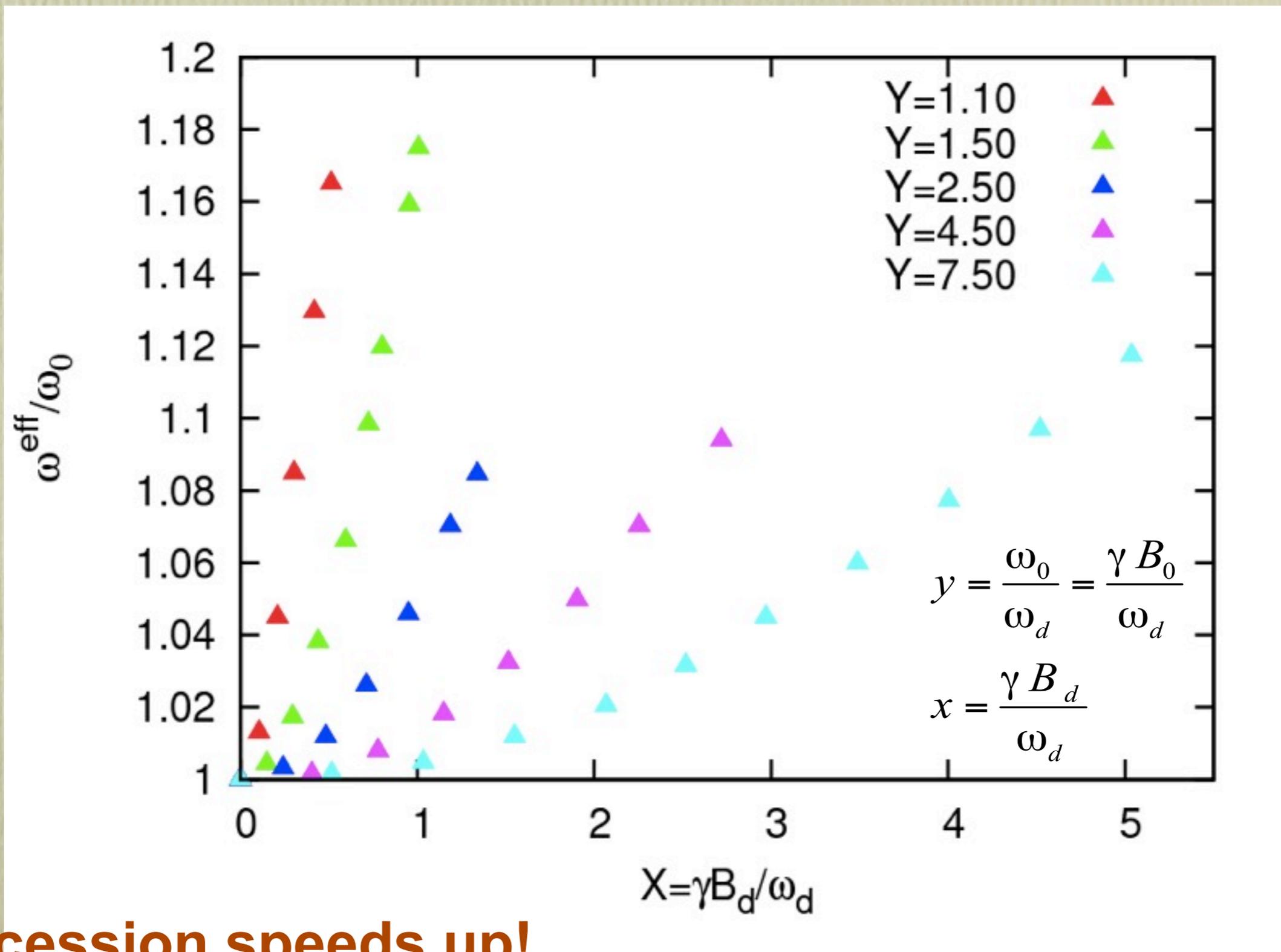
# The effective precession frequency for different dressing field configuration for $y < 1$ ( $\omega_0 < \omega_d$ )

(The proposal value is at  $y=0.01$ )



**Precession slows down!**

The effective precession frequency for different dressing field configuration for  $y > 1$  ( $\omega_0 > \omega_d$ )



# Quantum mechanical approach

$$H = H_M + H_{RF} + H_{int} = \hbar\omega_0 S_z + \hbar\omega_d a^\dagger a + \lambda S_x (a + a^\dagger)$$

$$\lambda = \hbar\gamma B_d / 2\bar{n}^{1/2}$$

Jaynes-Cummings Hamiltonian

$$Y = \frac{\gamma B_0}{\omega_d}$$

$$X = \frac{\gamma B_d}{\omega_d}$$

$n = \text{number of photons}$

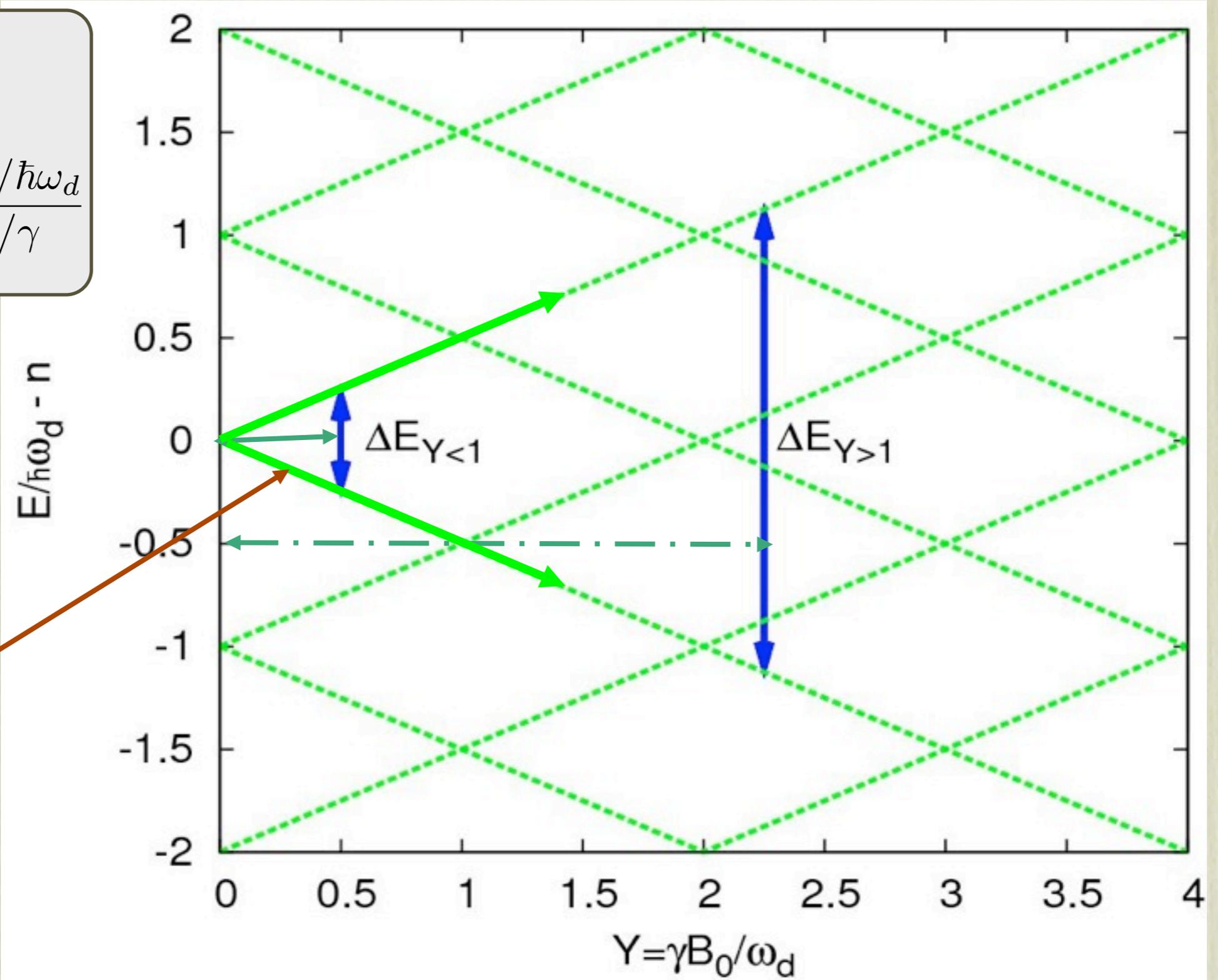
$$\hbar\omega_d \begin{bmatrix} n+1 + \frac{Y}{2} & 0 & 0 & \frac{X}{4} & 0 & 0 \\ 0 & n+1 - \frac{Y}{2} & \frac{X}{4} & 0 & 0 & 0 \\ 0 & \frac{X}{4} & n + \frac{Y}{2} & 0 & 0 & \frac{X}{4} \\ \frac{X}{4} & 0 & 0 & n - \frac{Y}{2} & \frac{X}{4} & 0 \\ 0 & 0 & 0 & \frac{X}{4} & n-1 + \frac{Y}{2} & 0 \\ 0 & 0 & \frac{X}{4} & 0 & 0 & n-1 - \frac{Y}{2} \end{bmatrix}$$

6x6

46x46

# Dependence of effective $\gamma$ in dressing field without dressing field

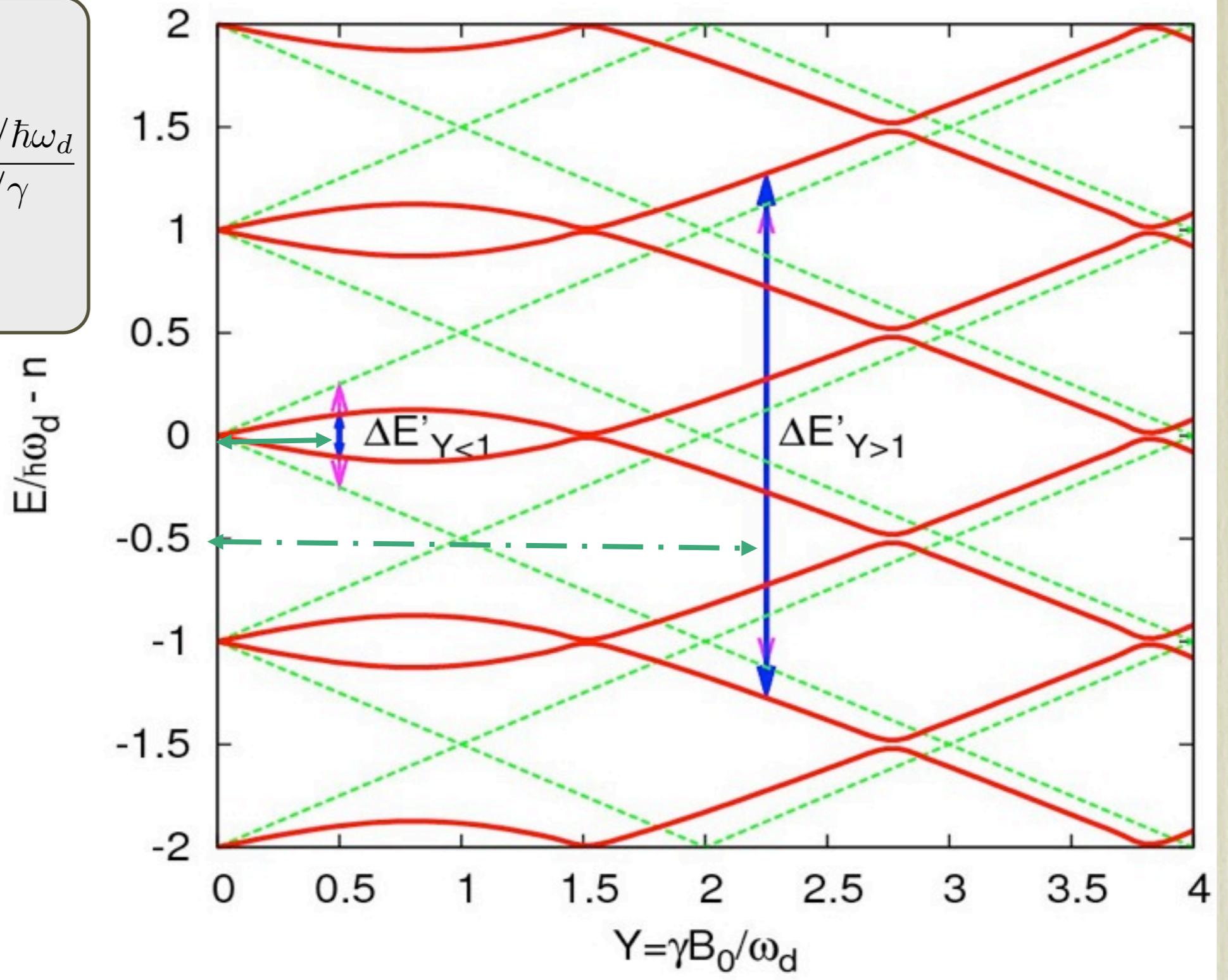
$$\begin{aligned}\gamma &= \frac{\omega}{B_0} = \frac{\Delta E/\hbar}{B_0} \\ &= \frac{\Delta E/\hbar\omega_d}{B/\omega_d} = \frac{\Delta E/\hbar\omega_d}{Y/\gamma}\end{aligned}$$



Zeeman  
Splitting

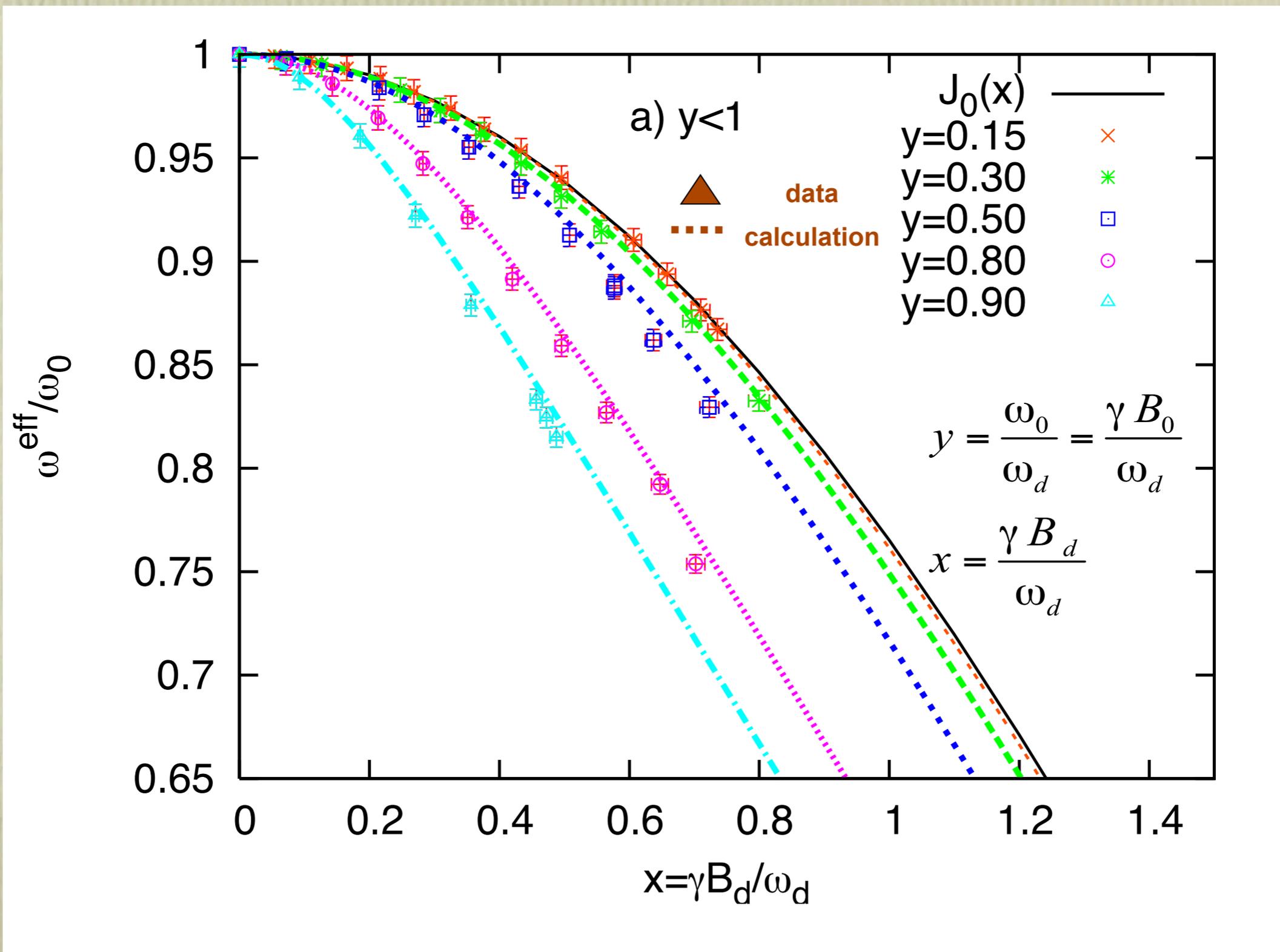
# Dependence of effective $\gamma$ in dressing field with dressing field

$$\begin{aligned} \gamma' &= \frac{\omega}{B_0} = \frac{\Delta E' / \hbar}{B_0} \\ &= \frac{\Delta E' / \hbar \omega_d}{B / \omega_d} = \frac{\Delta E' / \hbar \omega_d}{Y / \gamma} \\ \rightarrow \frac{\gamma'}{\gamma} &= \frac{\Delta E'}{\Delta E} \end{aligned}$$

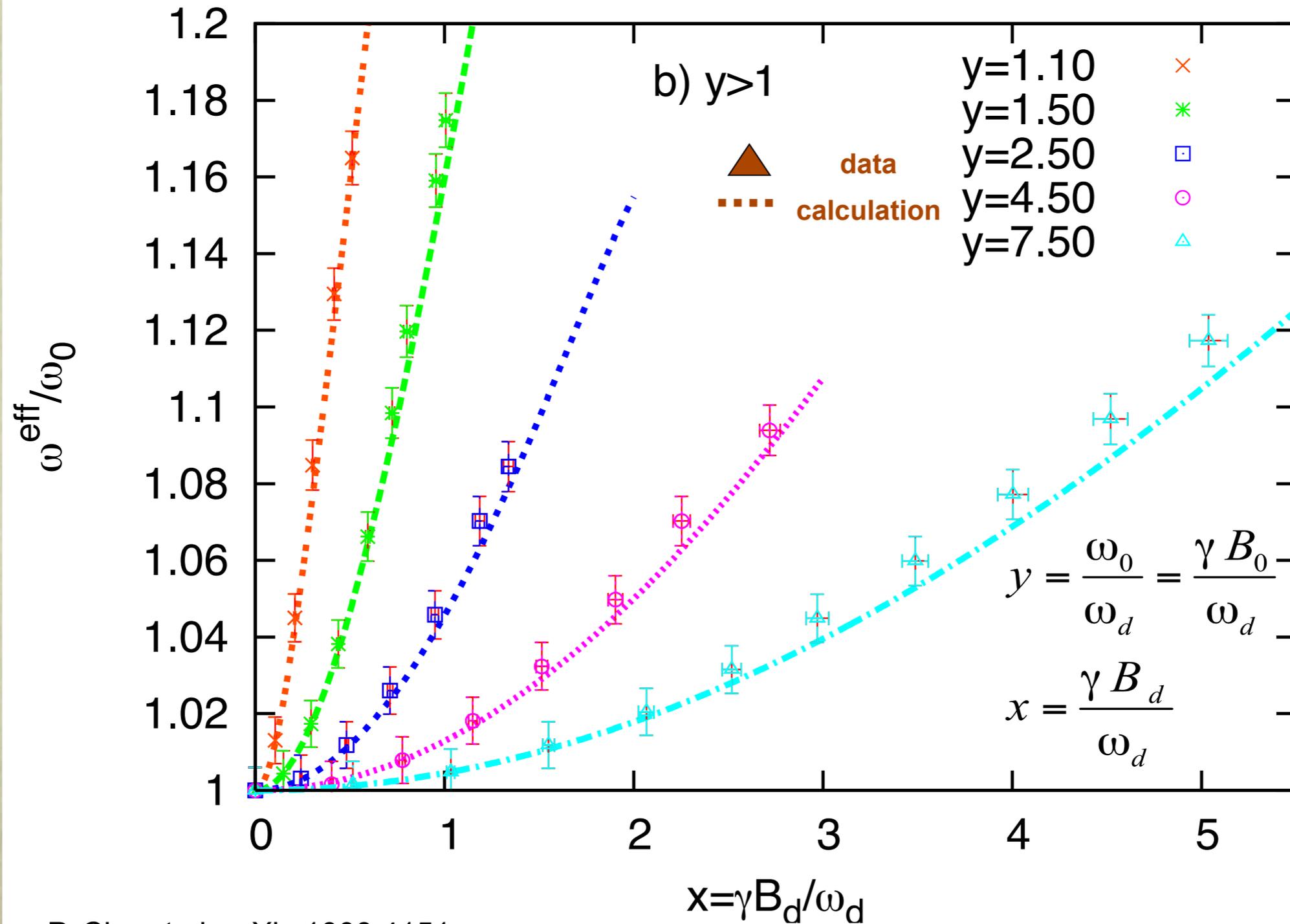


g ratio is equal to energy spacing ratio.

# The effective precession frequency for different dressing field configuration for $y < 1$ ( $\omega_0 < \omega_d$ )

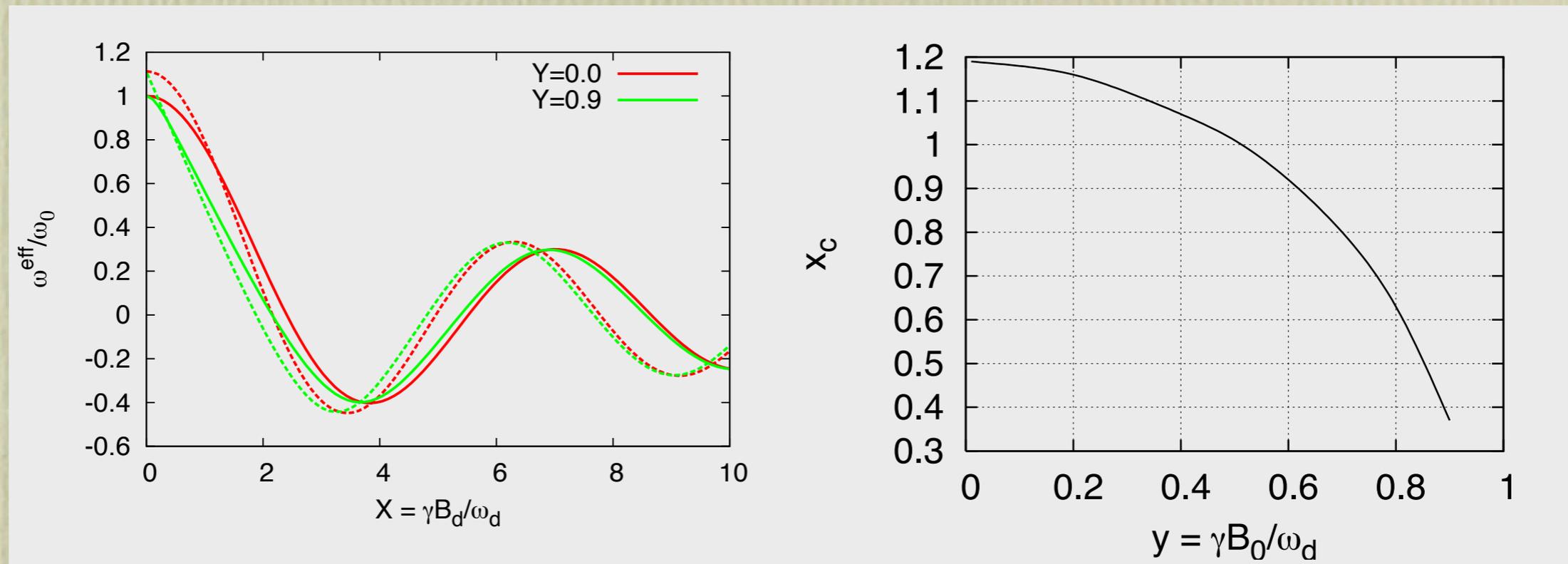


# The effective precession frequency for different dressing field configuration for $y > 1$ ( $\omega_0 > \omega_d$ )



P. Chu et al, arXiv:1008.4151

# Critical dressing for other $y$ 's (lower dressing frequencies)



- Other choices for the critical dressing?
- It may help the design of the dressing coils so that we don't need to run at the high dressing frequency condition.

# Simulation of the dressed spin

- Simulation of the dressed spin dynamics is underway.
- Bloch equation simulation with the 4th order of the Runge-Kutta method is used to simulate the dressed spin,

$$\frac{d\vec{S}(t)}{dt} = \vec{S}(t) \times \gamma\vec{B}(t)$$
$$\vec{B}(t) = B_0\hat{z} + B_d \cos \omega_d t \hat{x}$$

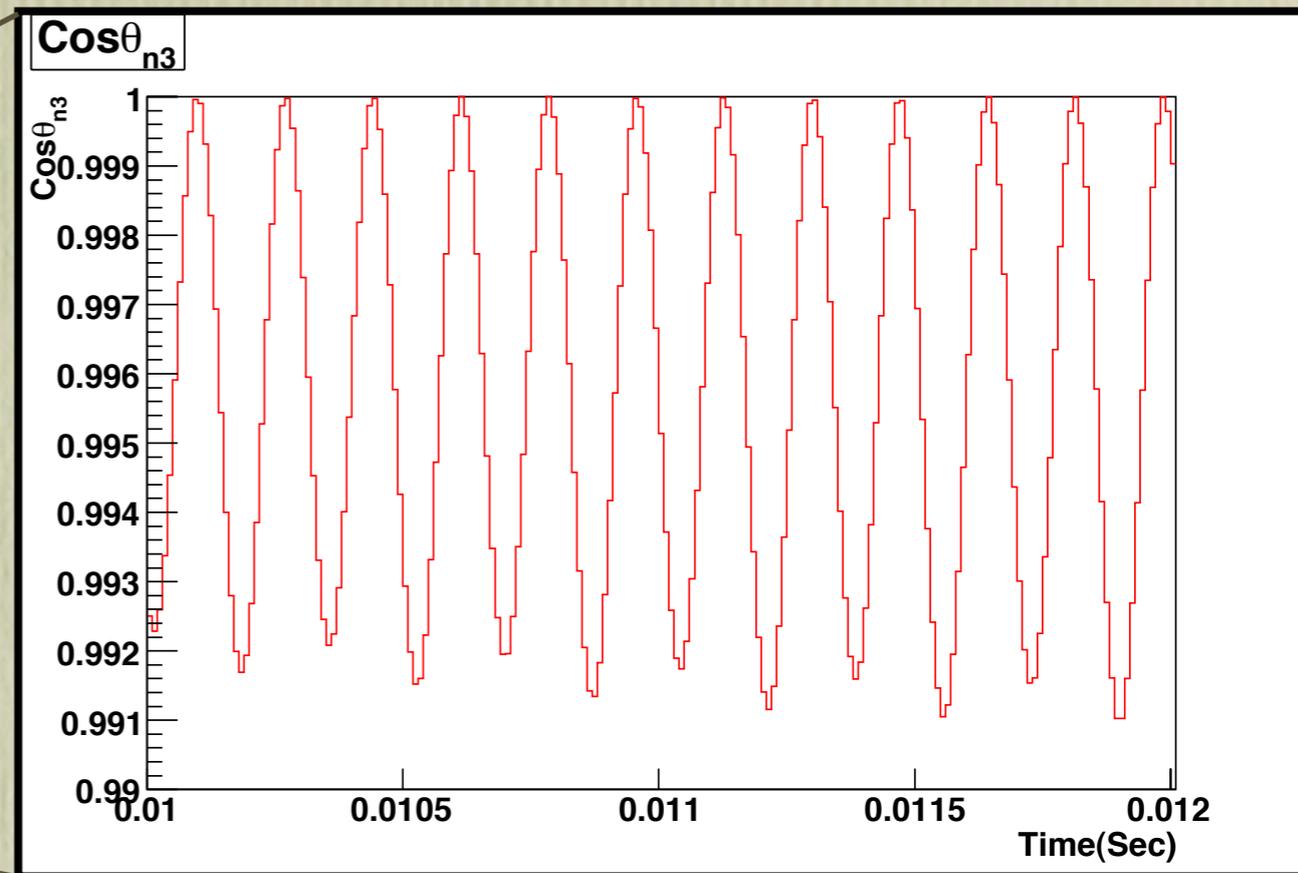
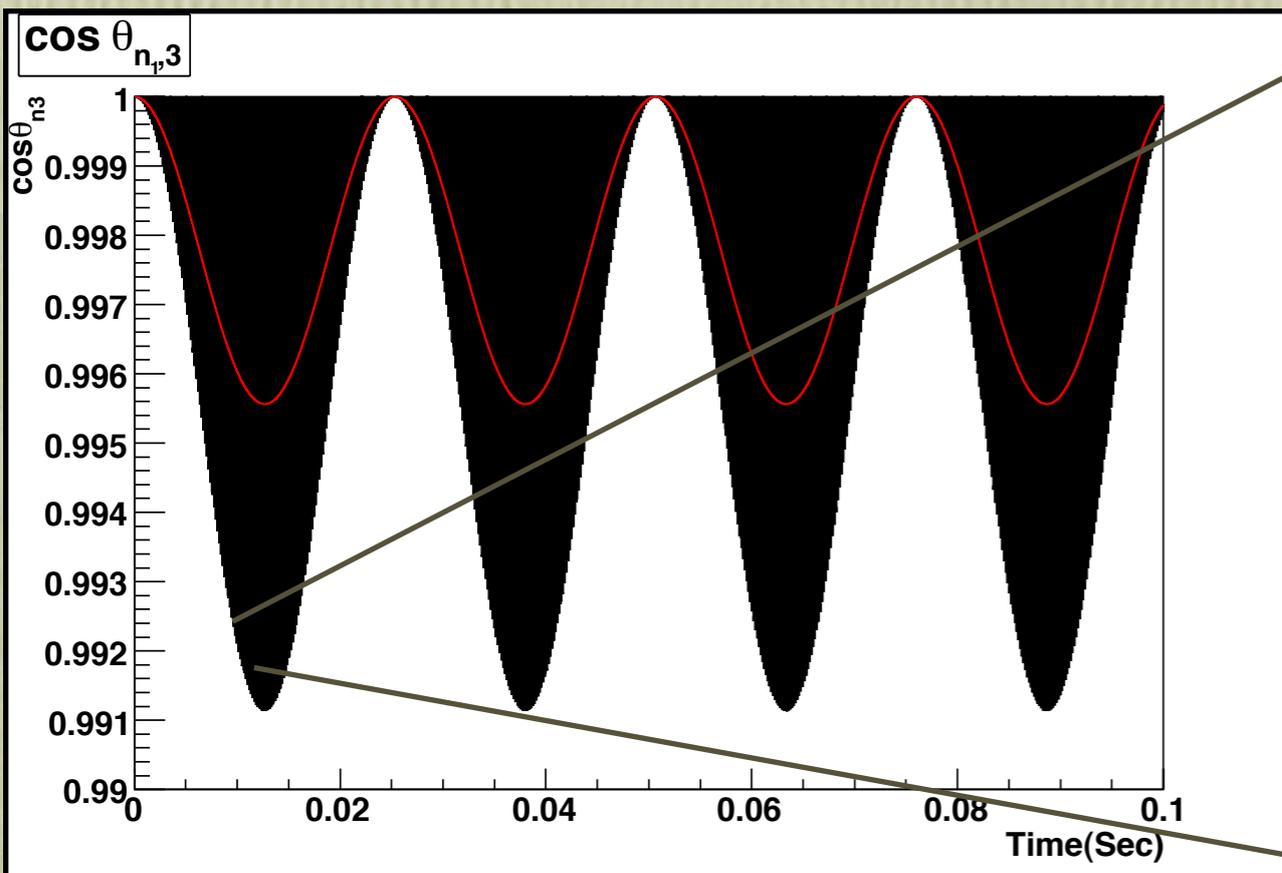
Bloch equation

- The time dependence of  $\cos\theta_{n3}$ , the relative angle between  $^3\text{He}$  and neutron spins, is derived in Physics Report 237, 1-62(1994) as:

$$\cos \theta_{n3} = \frac{1}{2}[1 + J_0(x_n - x_3)] \cos[(\omega_n - \omega_3)t] + \frac{1}{2}[1 - J_0(x_n - x_3)] \cos[(\omega_n + \omega_3)t]$$
$$x_n = \frac{\gamma_n B_d}{\omega_d}, \quad x_3 = \frac{\gamma_3 B_d}{\omega_d}, \quad \omega_n = \gamma_n B_0 J_0(x_n), \quad \omega_3 = \gamma_3 B_0 J_0(x_3)$$

- The first term of the analytical expression is a constant close to 1 at the critical dressing where  $\omega_n = \omega_3$ . The second term has an oscillatory pattern.

# Simulation of the dressed spin



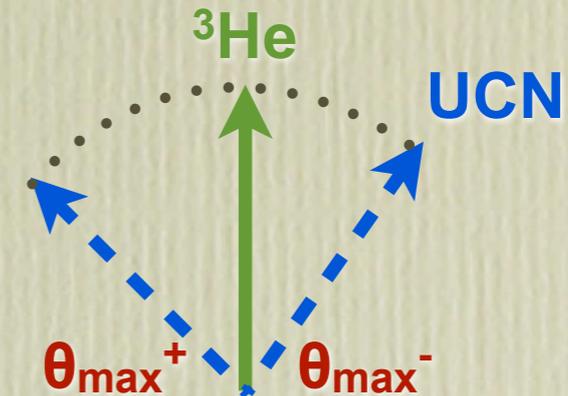
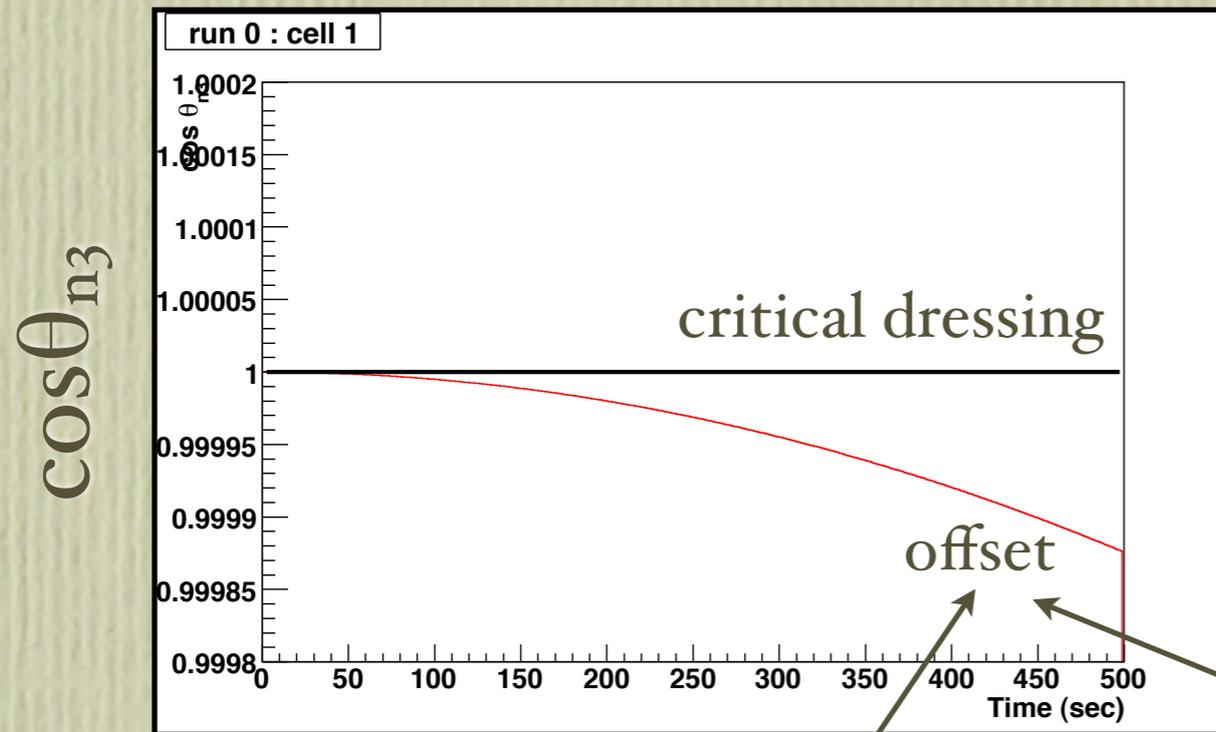
- Use the proposal values at  $y=0.01$ ,  $x=1.189$ ,  $B_0=10$  mG,  $B_d =1189$  mG,  $f_d=-2916.46954$ Hz, which is very close to the critical dressing.

- The black is the Bloch equation simulation. The red is the analytical expression, which is consistent with the time average of the simulation.

- The simulation also shows an additional oscillatory pattern at the dressing frequency and visualize the spin dynamics.

[http://www.youtube.com/watch?v=xBL\\_jDjtojC](http://www.youtube.com/watch?v=xBL_jDjtojC)

# Idea of the feedback

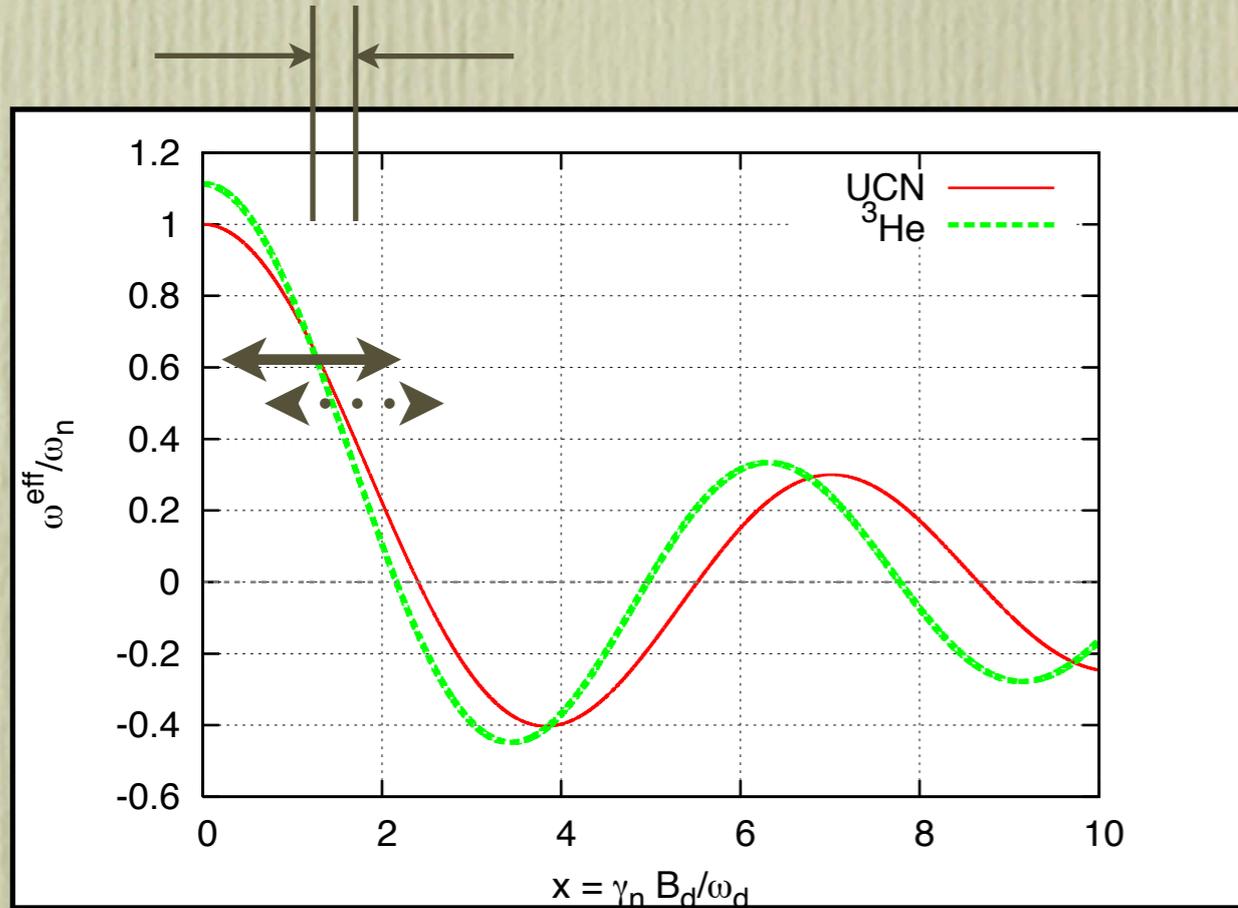


$$\cos \theta_{n3} \approx \frac{1}{2} [1 + J_0(\Delta x + x_n - x_3)] \cos[(\Delta\omega + \omega_n - \omega_3)t]$$

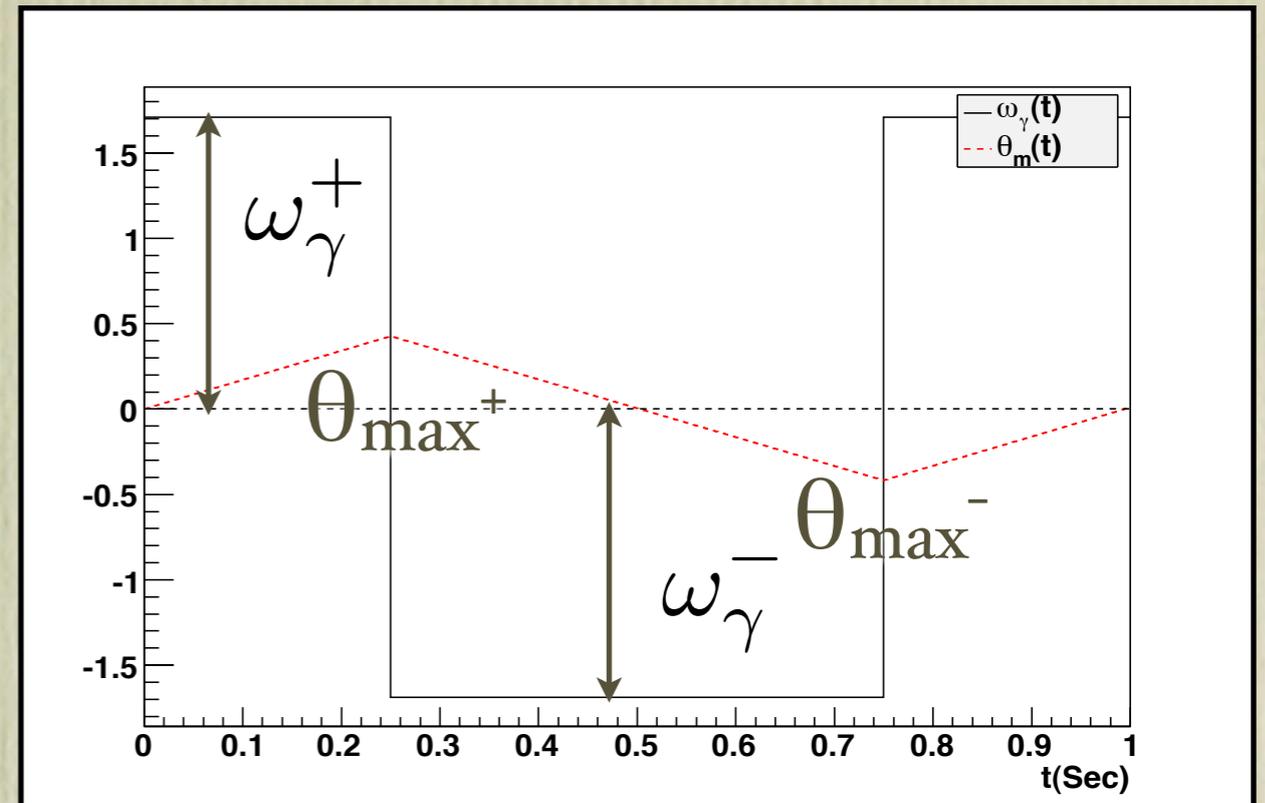
- If the dressing field deviates from the critical dressing,  $\cos\theta_{n3}$  will have time dependence which will mix with the EDM signal.
- Apply a **feedback** to compensate the offset, initially proposed by Golub and Lamoreaux in 1994.
- Add a modulation to vary the angle between neutron and  $^3\text{He}$ . Any difference between modulation angles in opposite directions (the scintillation light) will be the input to the feedback.

offset

# Apply a modulation

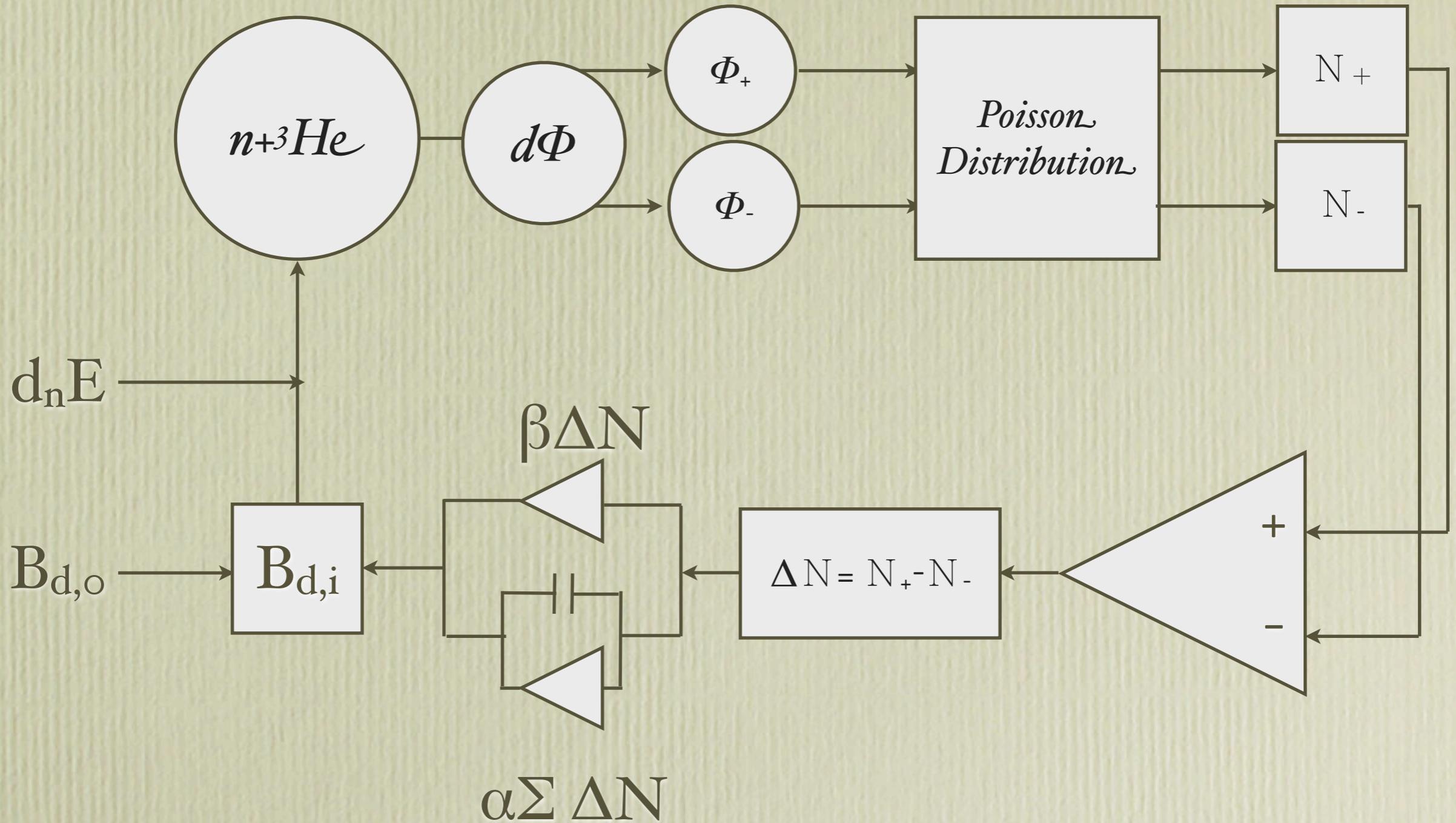


$$\omega_{\gamma}^{\pm} = \omega_0 [J_0(x_c \pm x_m) - aJ_0(a(x_c \pm x_m))]$$

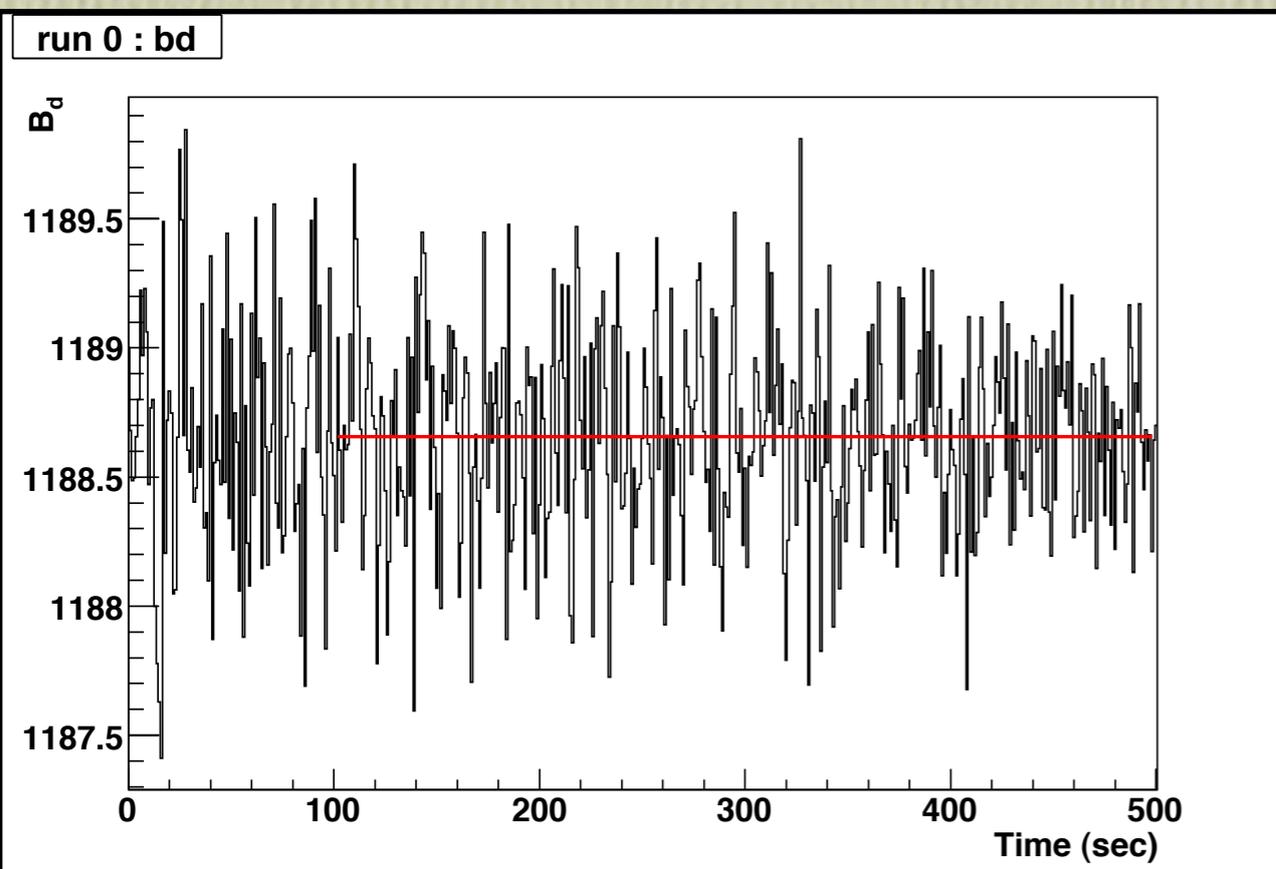
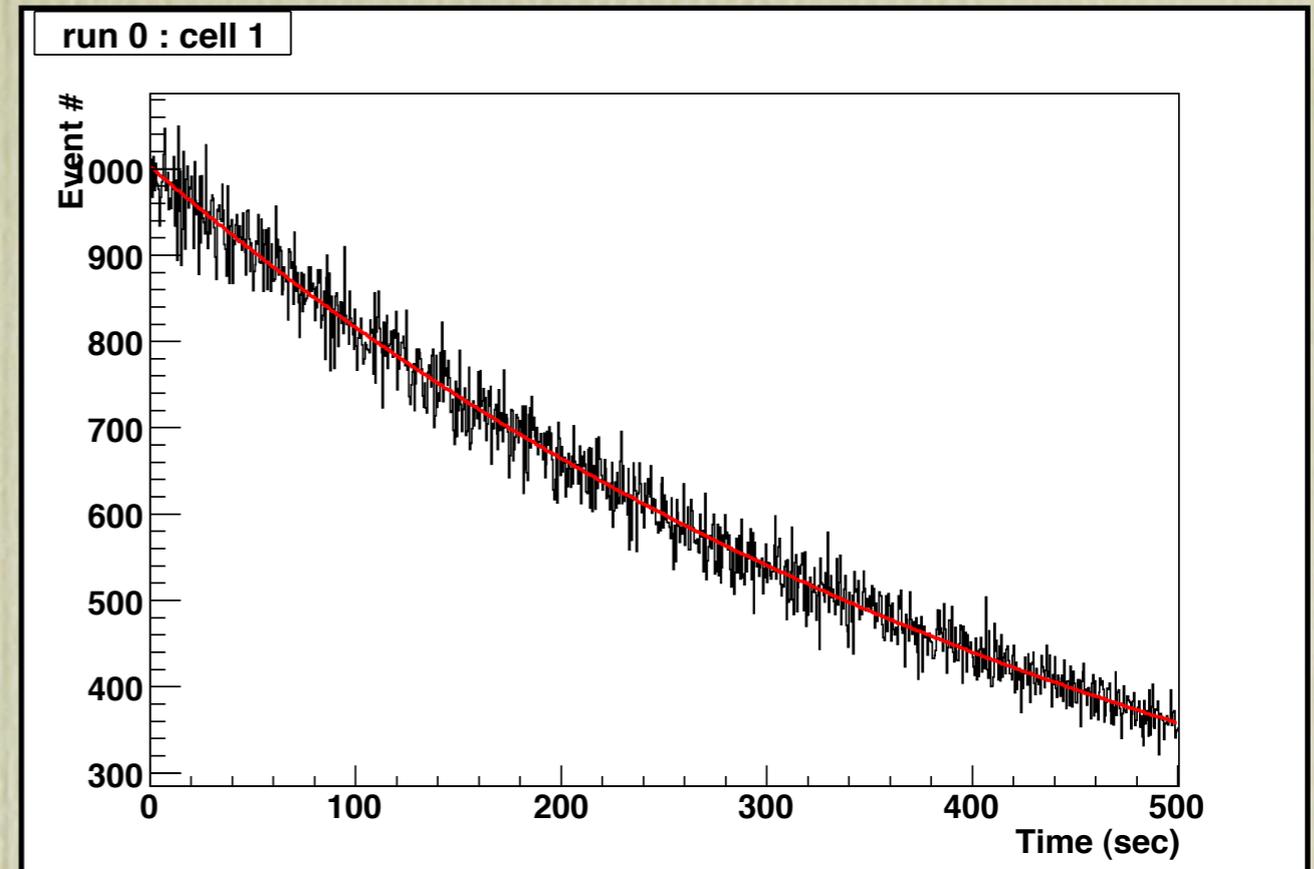
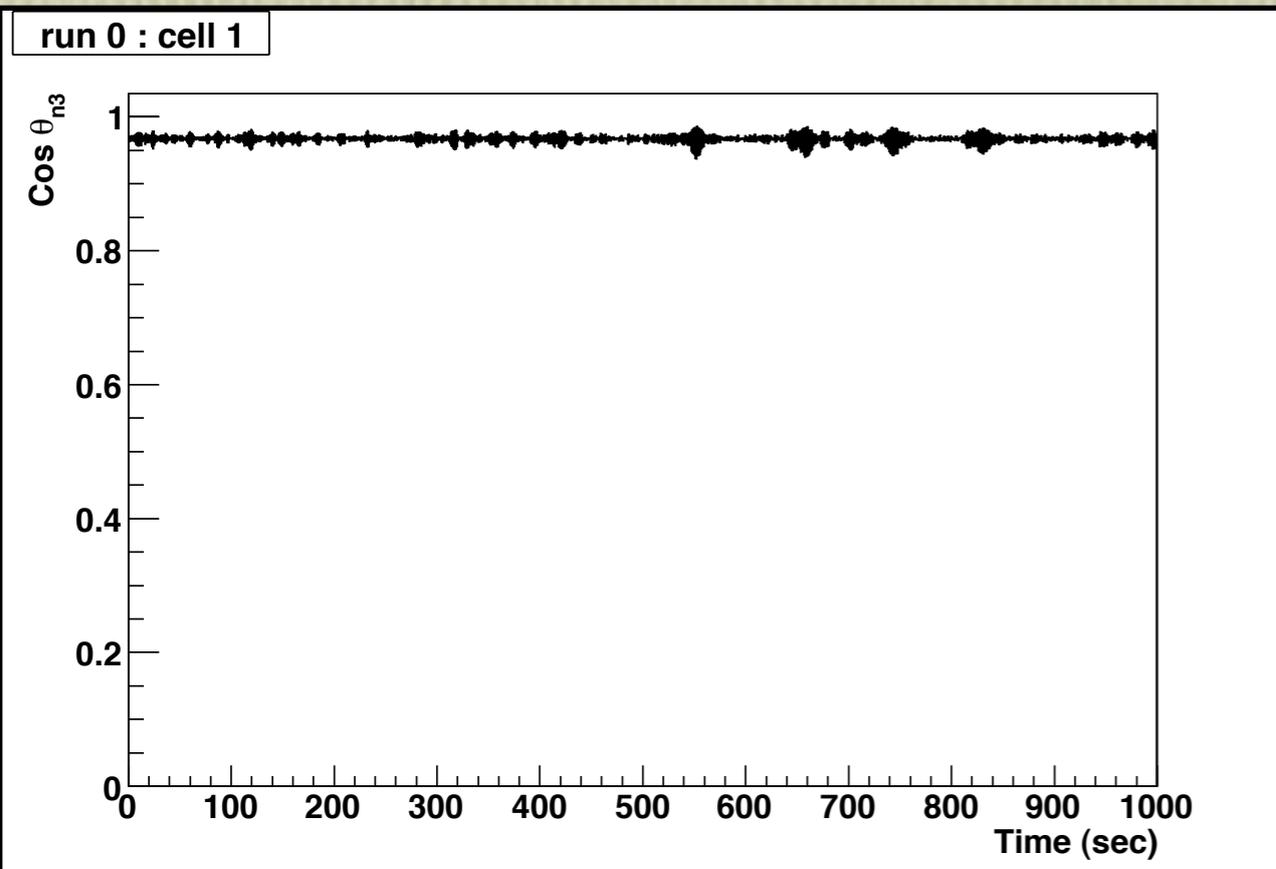


- Add a modulation on the dressing field so that  $x_c \rightarrow x_c \pm x_m$
- The relative angle between neutron and  $^3\text{He}$  is varied between  $\theta_{\text{max}}^+$  and  $\theta_{\text{max}}^-$ .  $\theta_{\text{max}}^+ = \theta_{\text{max}}^-$  at the critical dressing.
- Any offset will cause difference in  $\theta_{\text{max}}^+$  and  $\theta_{\text{max}}^-$ .
- Measure the scintillation light difference in opposite modulation directions.

# Schematic of feedback loop



# Monte Carlo for the feedback loop

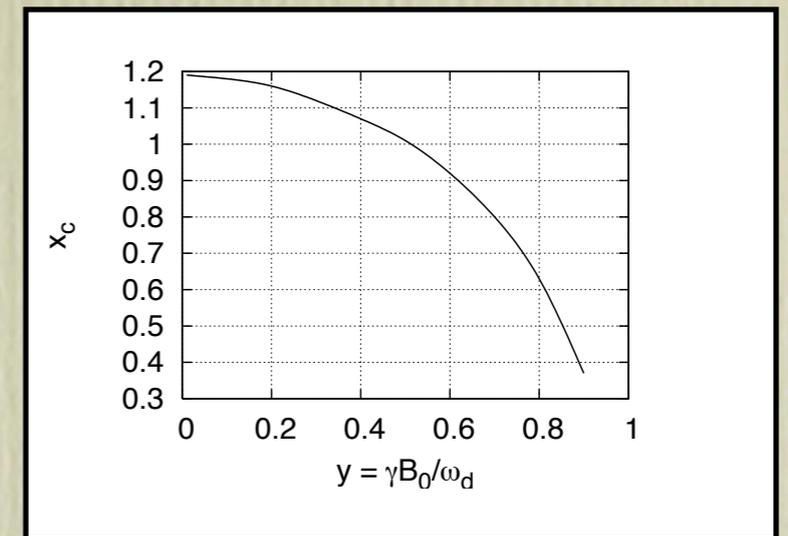


- $\text{Cos}\theta_{n3}$  is kept at a constant.
- The signal is kept at the critical dressing.
- Relate the EDM effective field to  $B_d$ , fit.
- The feedback can be only applied in a single measurement cell in the SNS experiment (since both two cells share the same dressing coils).
- Many parameters remain to be optimized

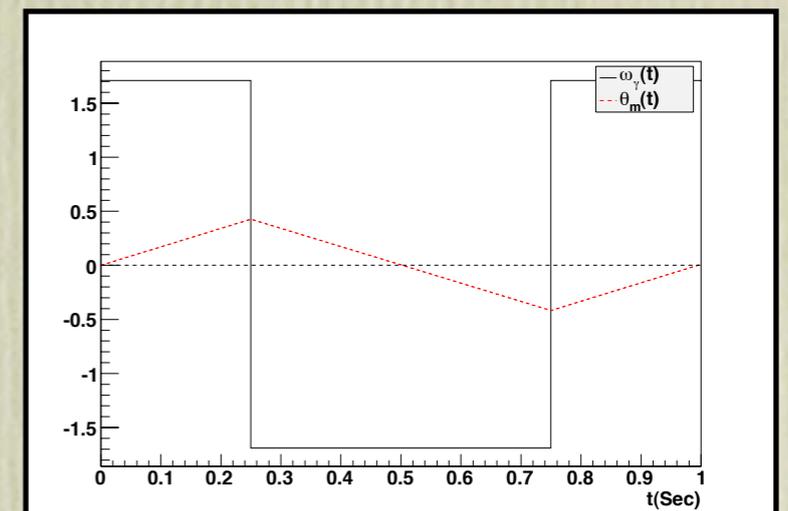
# Parameters for dressing/modulation/feedback

- Several parameters should be considered and optimized.

- $x$  and  $y$  are discussed in the dressed spin study. There are critical points for different  $y$ 's.

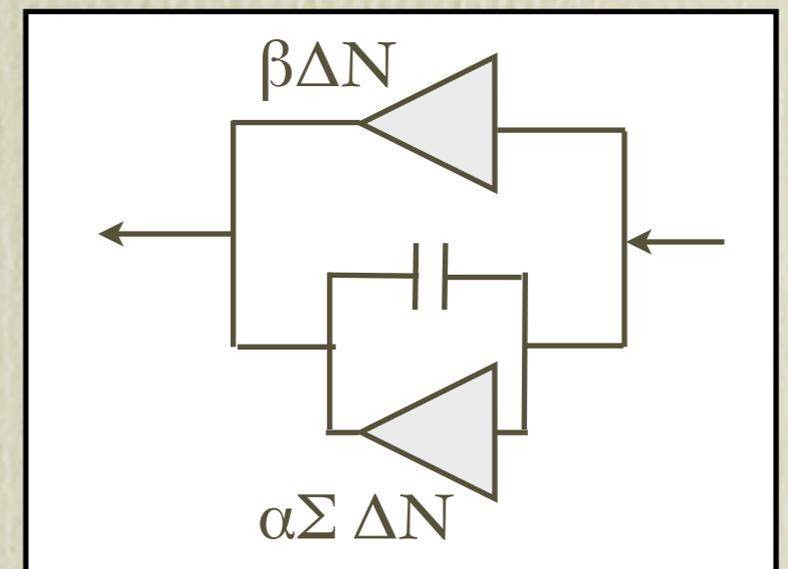


- Modulation amplitude  $B_m$  and period  $\tau_m$  should be carefully determined since it is related to the input signal.



- The feedback parameters  $\alpha$  and  $\beta$  are important for the feedback loop to succeed.

- The optimization is still ongoing.

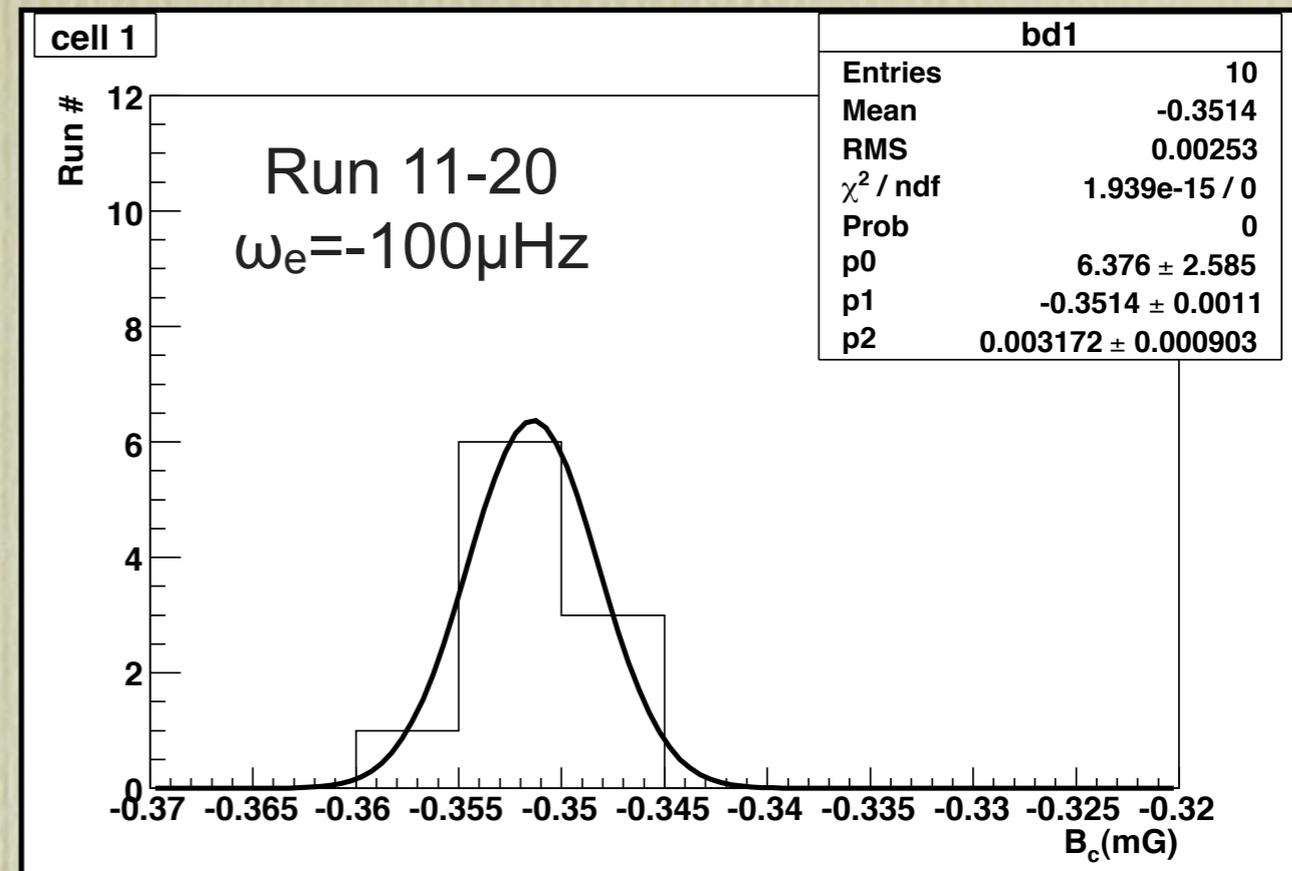
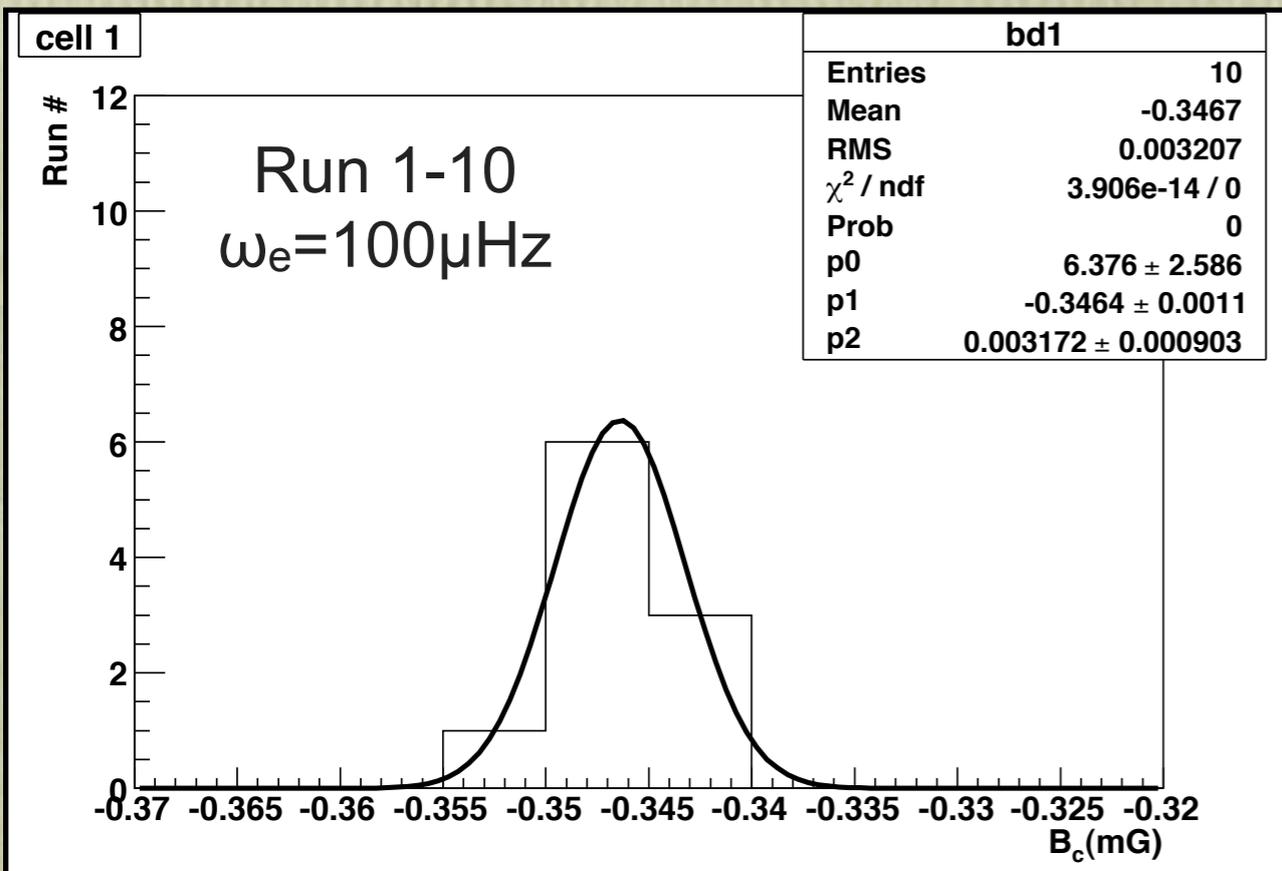


# Summary

- Neutron EDM is a powerful tool searching for physics beyond SM.
- The goal of next generation experiments is to reach the sensitivity at  $10^{-28}$  e cm.
- A new neutron EDM experiment uses ultracold neutron produced in superfluid  $^4\text{He}$ , with  $^3\text{He}$  as a spin analyzer and a comagnetometer. The dressed spin technique will be applied to reduce the systematic uncertainty.
- The dressed spin phenomena have been studied over a broad range of dressing field configuration in UIUC. The observed effects are compared with calculations based on quantum optics formalism
- The optimal implementation of the dressed spin technique for the neutron EDM experiment is still ongoing.

# Back-up slides

# Monte Carlo for the feedback loop



- Apply an electric field in different direction for different runs. Assume  $\omega_e = 100 \mu\text{Hz}$ .
- The correction field  $B_c = B_{d,\text{fit}} - B_{d,0}$  for Run 1-10 is  $-0.3467 \text{mG}$  and for Run 11-20 is  $-0.3514 \text{mG}$ , which include both the offset and the EDM effective field. Thus  $\Delta B_c = 0.0047 \text{mG}$ .
- Use the relation between the correction field and the EDM effective field:

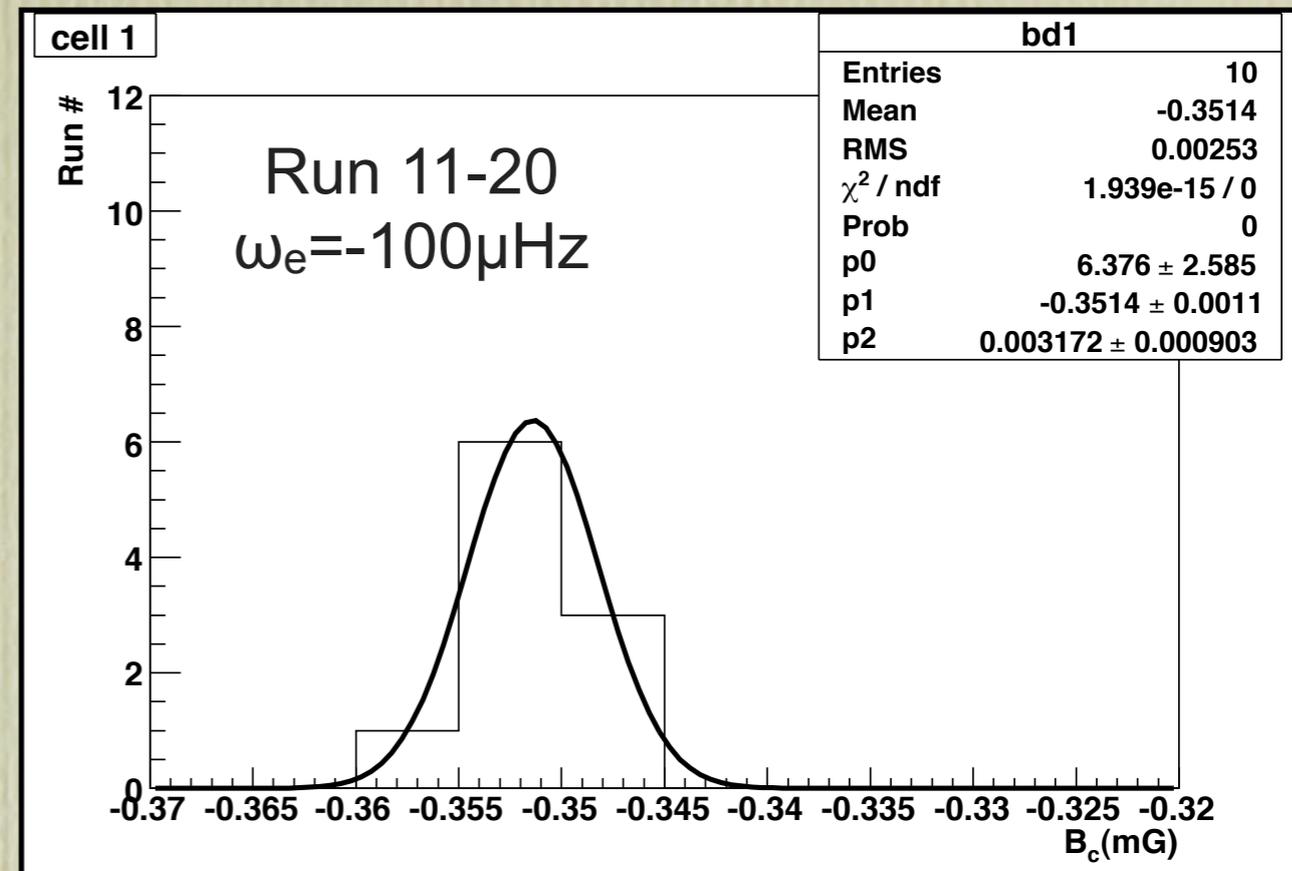
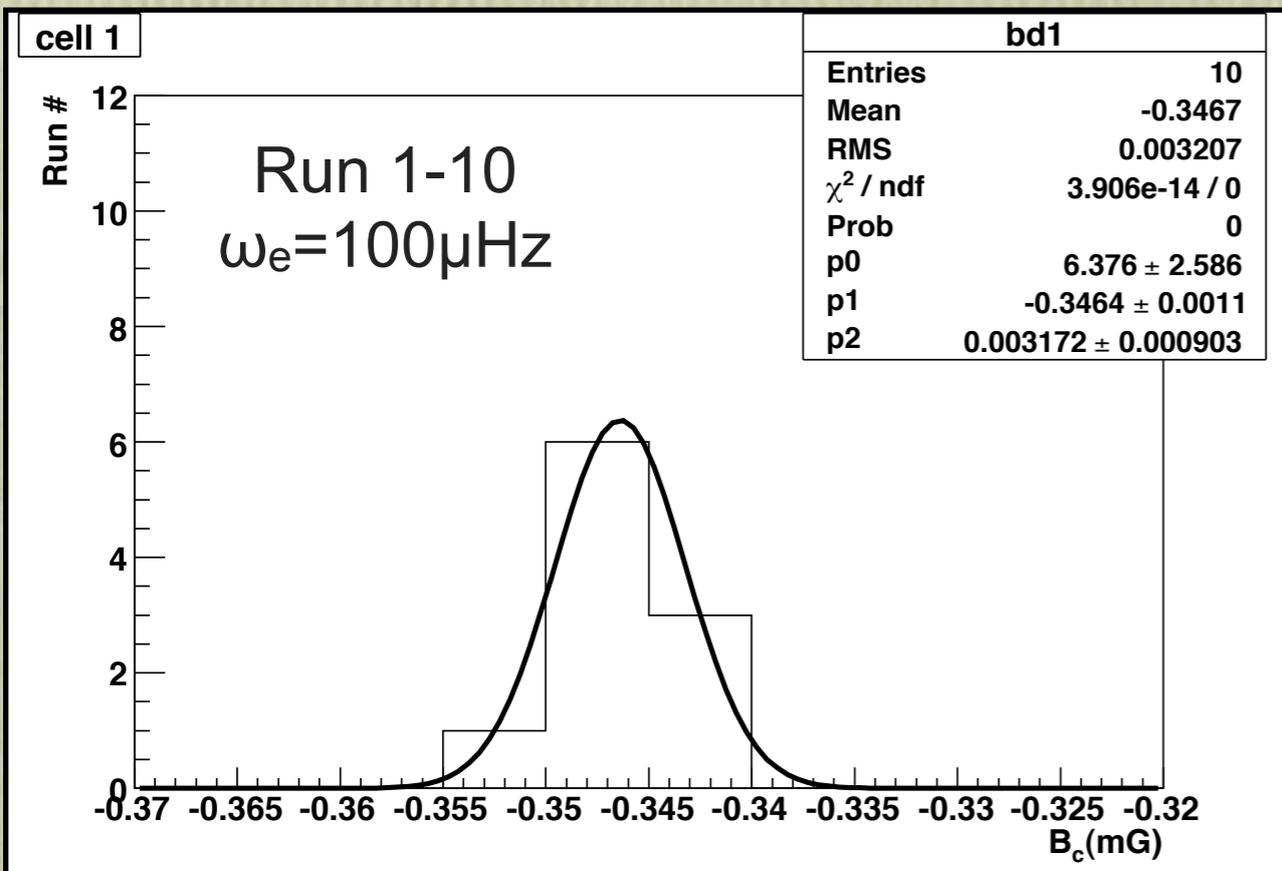
$$\Delta\omega_\gamma = \omega_0 [J_0(x_c + \Delta x) - \gamma_3/\gamma_n J_0(\gamma_3/\gamma_n(x_c + \Delta x))]$$

$$= 0.156077\omega_n \Delta x = 0.156077\omega_n \frac{\gamma_n B_c}{\omega_d} = -0.0286007 B_c = \omega_e J_0(x_c)$$

$$\omega_e = -0.0422713 B_c$$

$$\Delta\omega_e = 198.675 \mu\text{Hz}$$

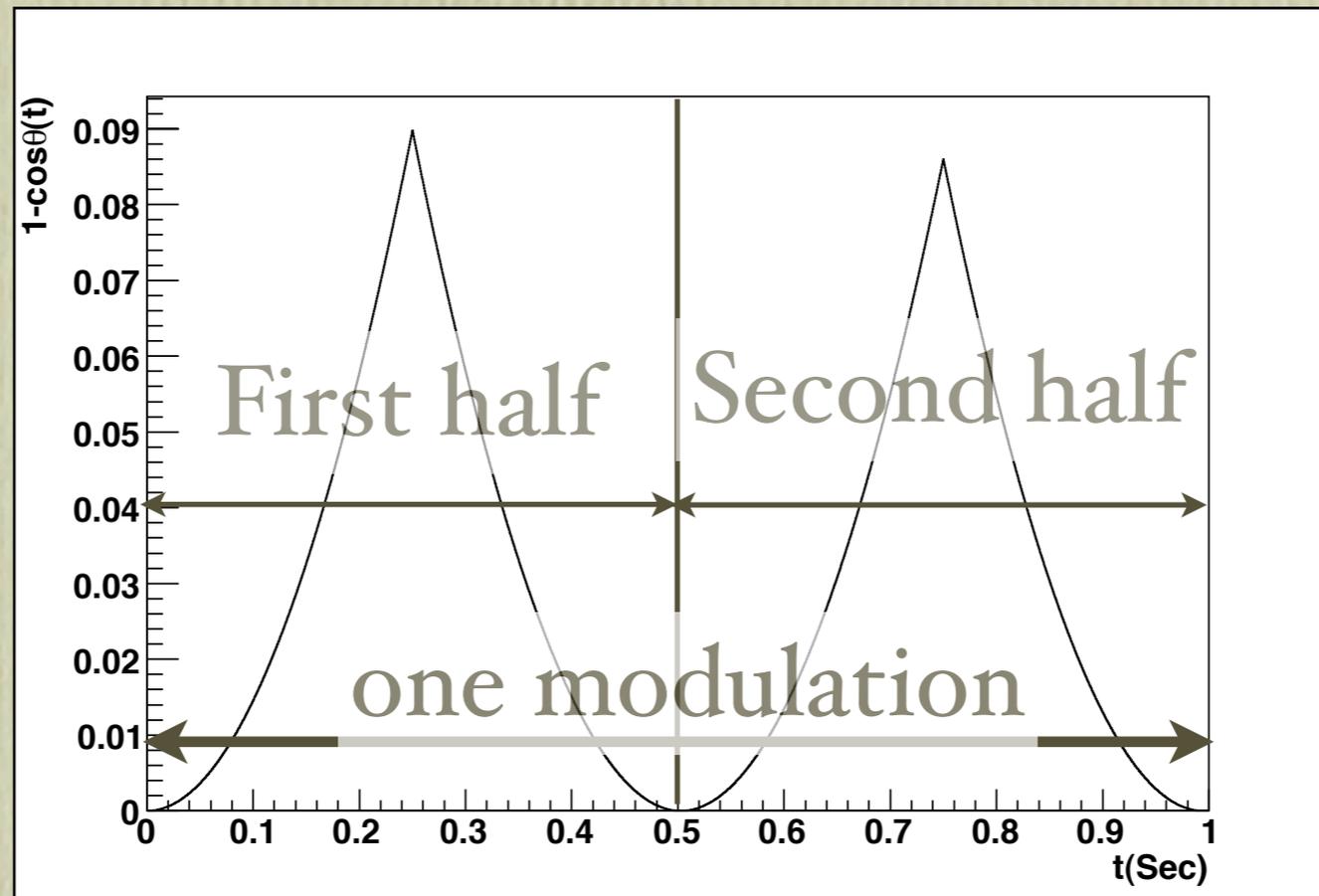
# Sensitivity of the feedback method



- The RMS for 20 runs is 0.0028884 mG.
- Thus, the sensitivity for the EDM is  $\sigma_{fe} = 19.4323 \mu\text{Hz}$ .
- Comparing with the case without the dressing field which is around  $2.7 \mu\text{Hz}$ , the feedback method still needs optimization (x and y, modulation parameters, feedback parameters, etc.).

# Modulation signal

The distribution function =  $(d\phi/dt)/N_0$  depends on  $1-\cos\theta_{n3}$ .

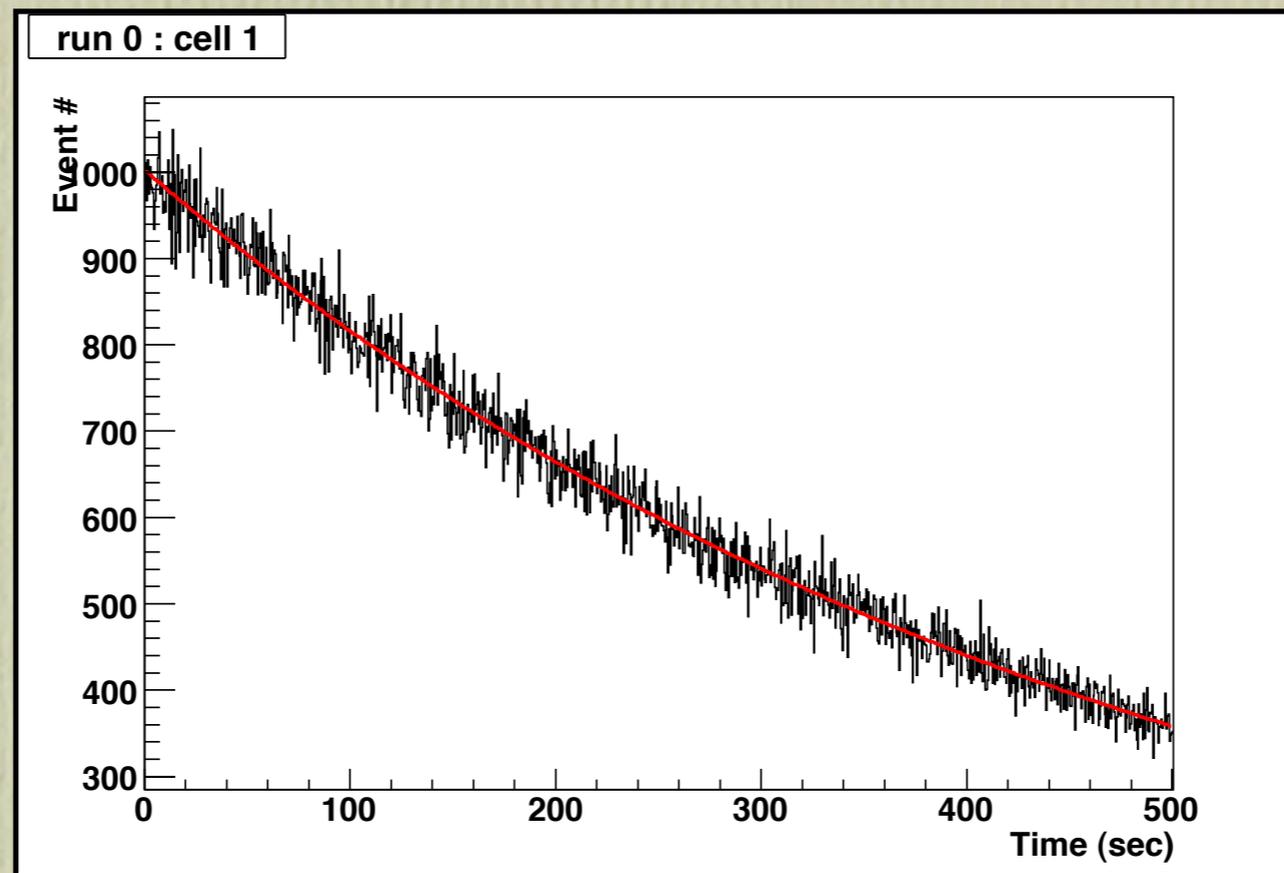


• The scintillation light rate is  $\frac{d\phi(t)}{dt} = N_0 e^{-\Gamma_{tot}t} \left[ \frac{1}{\tau_\beta} + \frac{1}{\tau_3} (1 - P_3 P_n \cos(\theta_{n3})) \right]$

• The counts in the **first half** and the **second half** of a modulation cycle should be *identical* at the critical dressing.

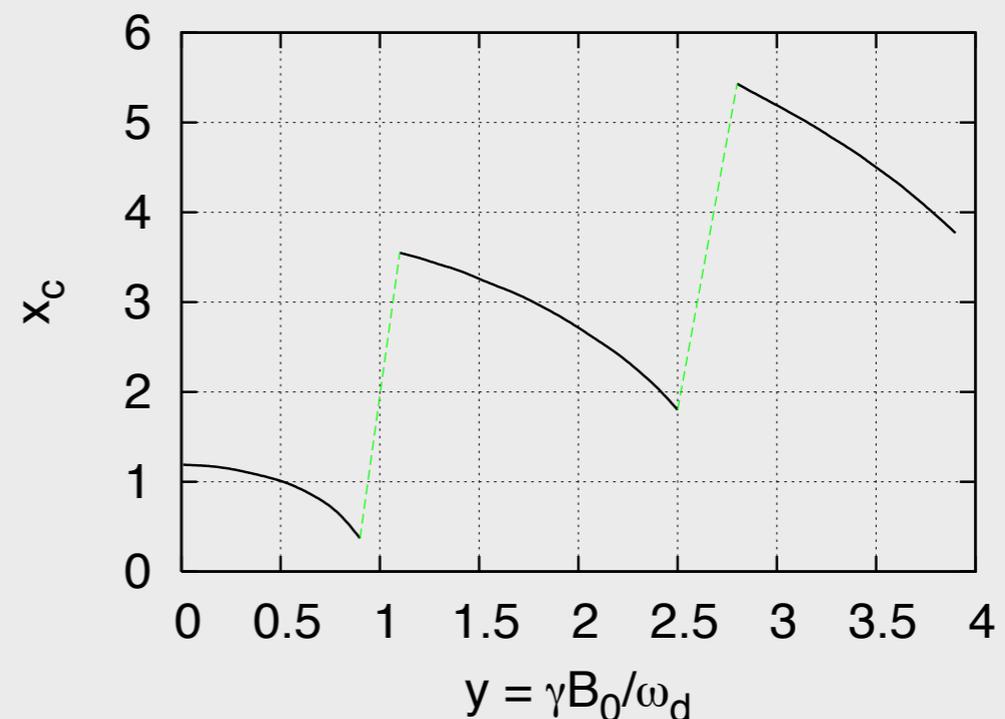
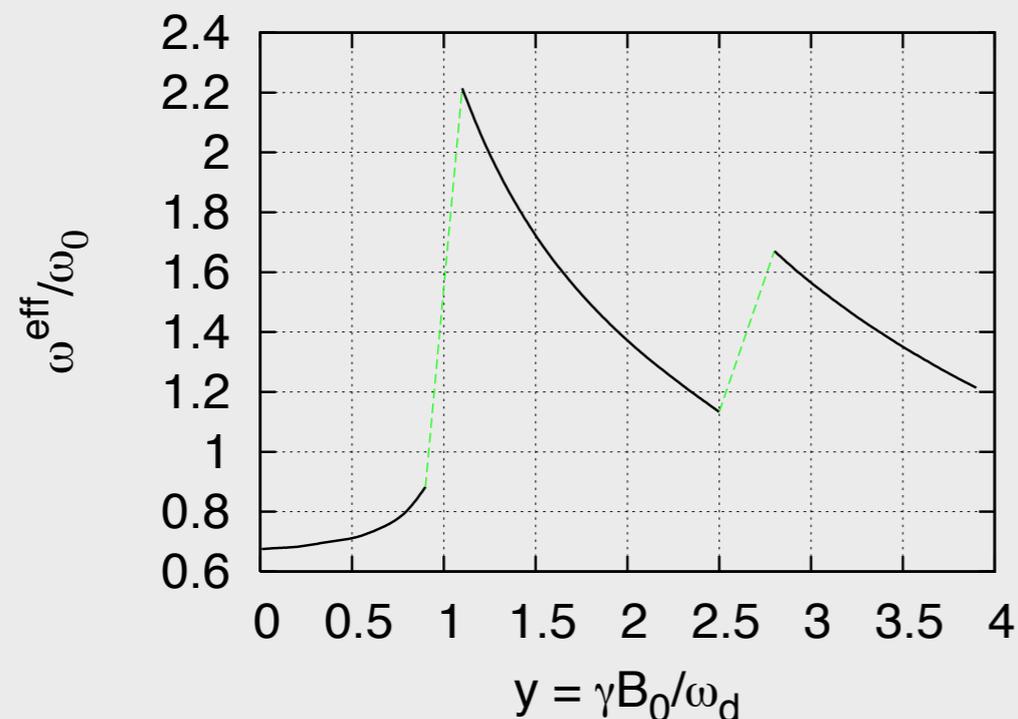
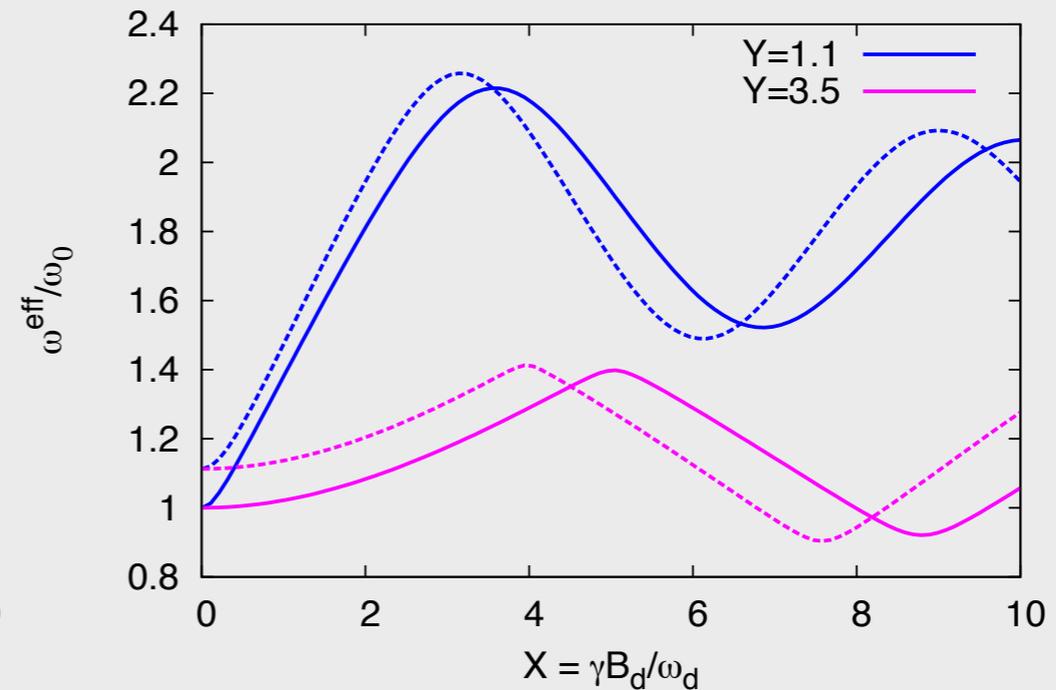
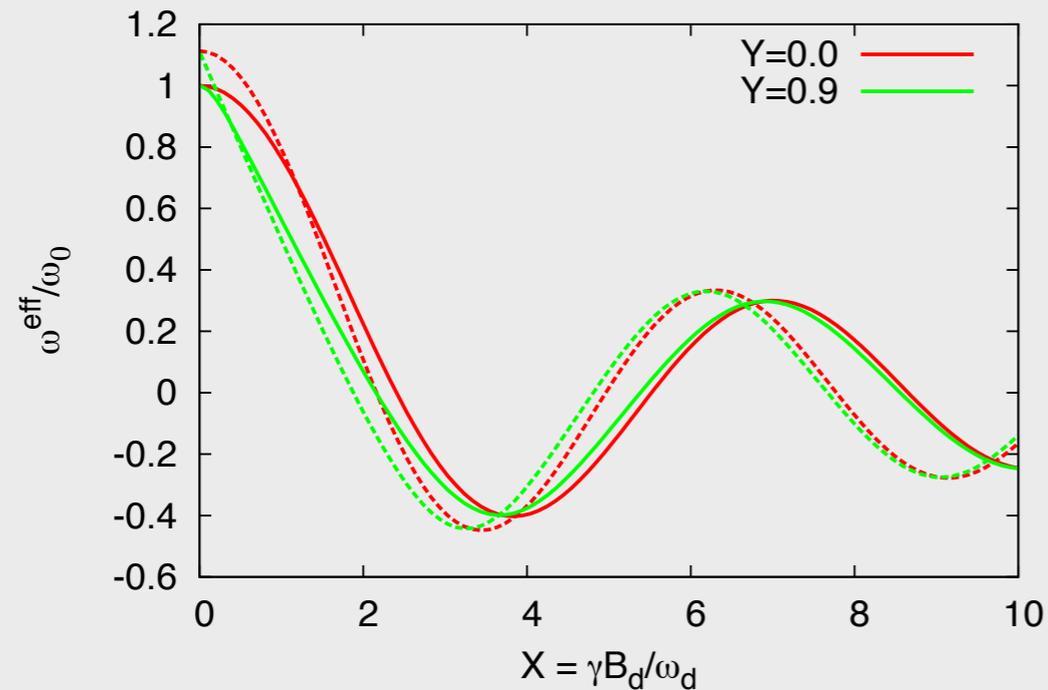
• The difference in the counts will be the input to the feedback.

# Monte Carlo for the feedback loop



- Example of the simulation for the scintillation events with modulation/ feedback scheme.
- many parameters remain to be optimized

# Critical dressing for other $y$ 's (lower dressing frequencies)



- Other choices for the critical dressing. Consider the possibility once we realize the dressed spin technique. It may help to the design of the dressing coils so that we don't need to run at the high dressing frequency condition.

# Apply a modulation

- At the critical dressing, no signal from the  $^3\text{He}$  capture. Add a modulation.

- The relative precession frequency between neutron and  $^3\text{He}$  at the critical dressing is

$$\omega_\gamma = \omega_0 [J_0(x_c) - aJ_0(ax_c)] = 0$$

- Apply a **cos square modulation** onto the dressing field such as

$$B_d(t) = [B_{d,c} + B_m \text{Sign}(\cos(\omega_m t))] \cos \omega_d t$$

$$x = x_c \pm x_m$$

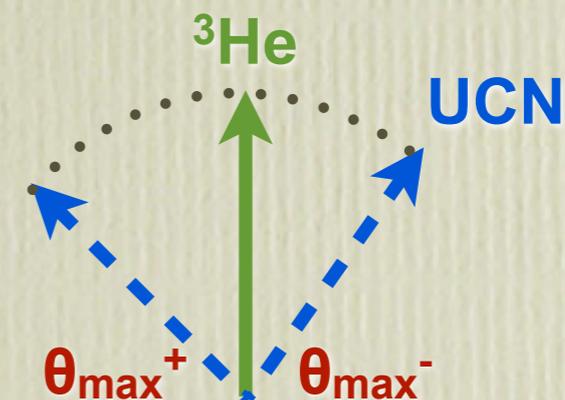
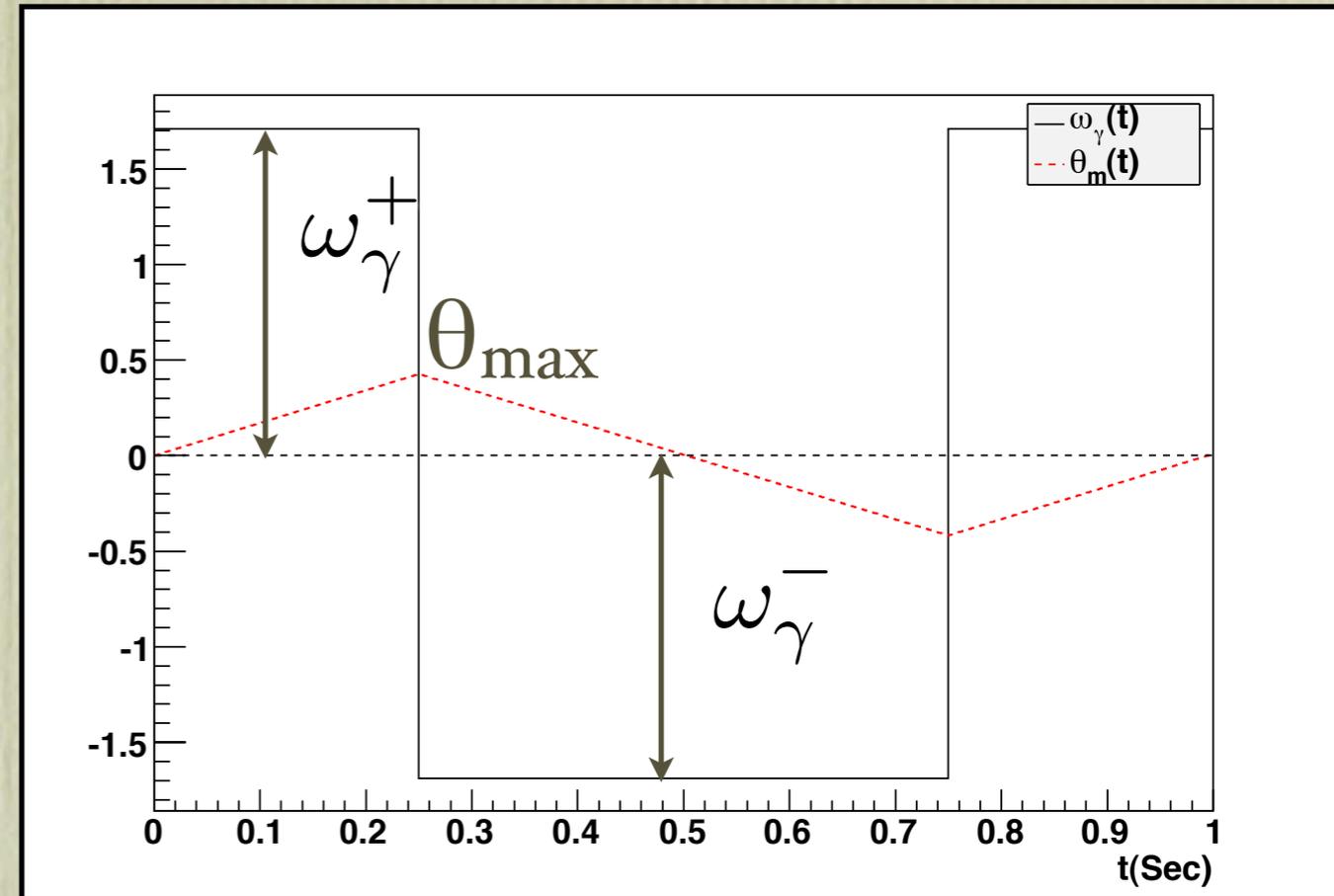
- The **relative precession frequency** becomes

$$\omega_\gamma^\pm = \omega_0 [J_0(x_c \pm x_m) - aJ_0(a(x_c \pm x_m))]$$

- The maximum **relative angle** becomes

$$\theta_{max}^\pm = \omega_\gamma^\pm \tau_m / 4$$

- The result can be also simulated by using Bloch equation.

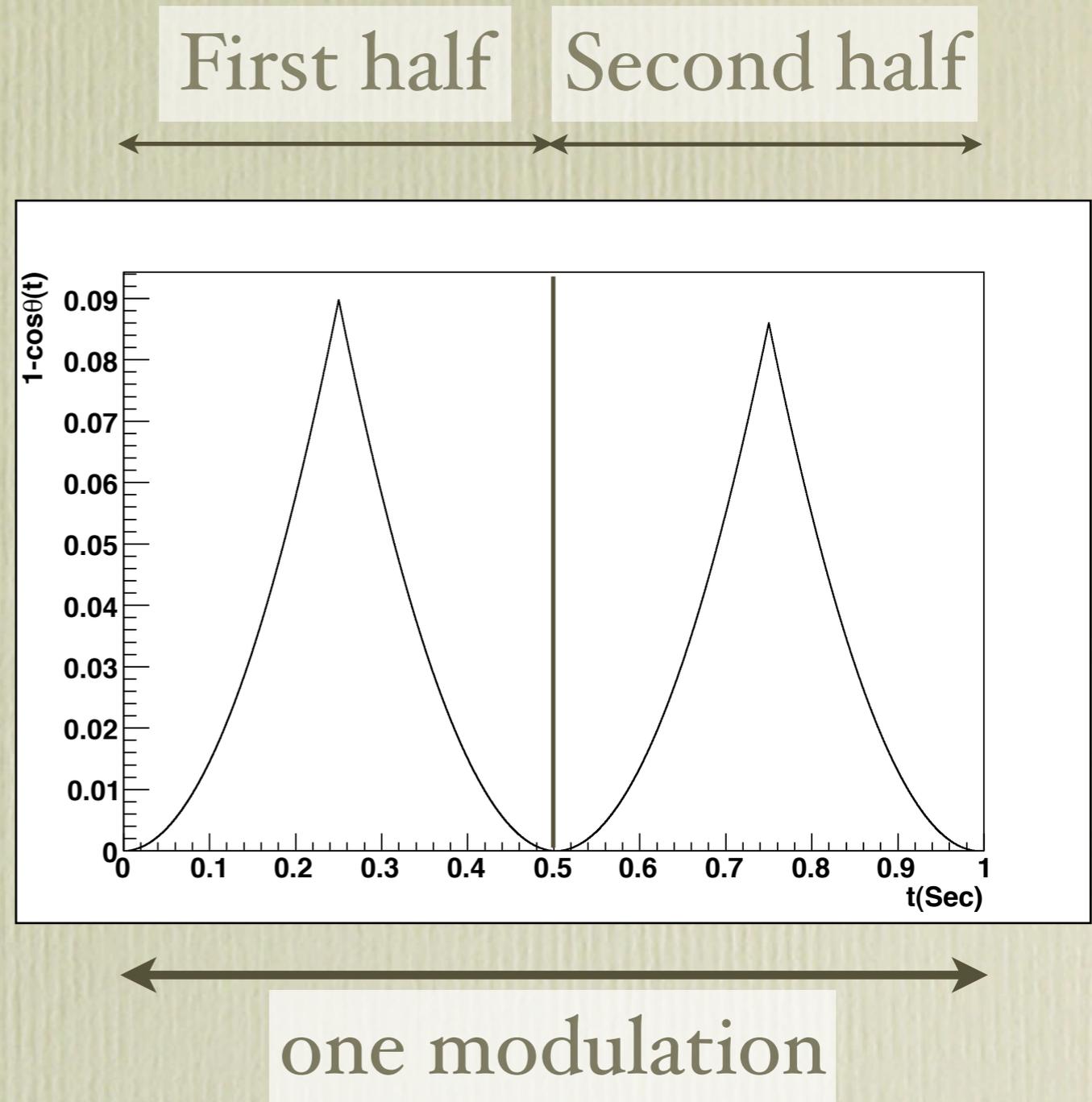


# Apply the feedback loop

- The scintillation light is

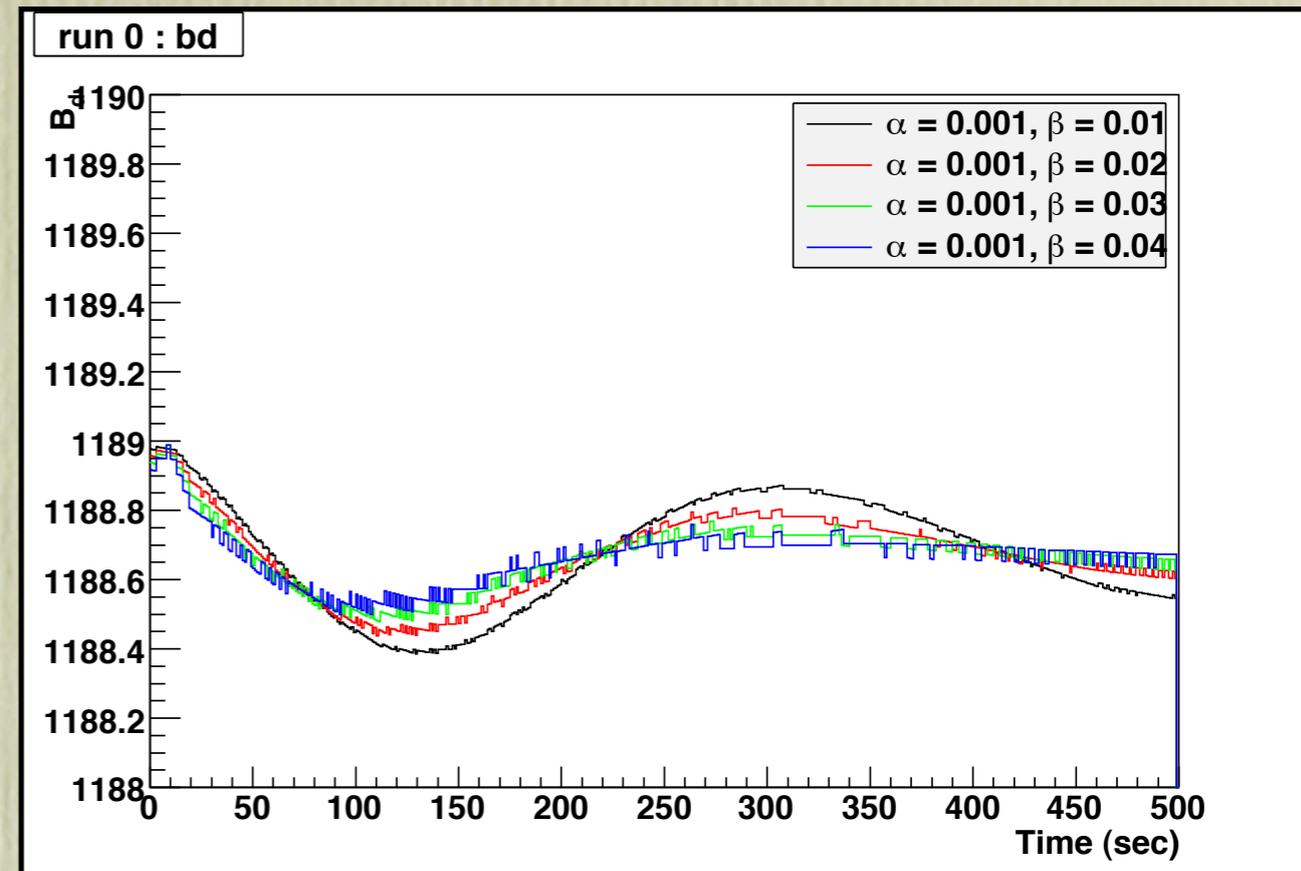
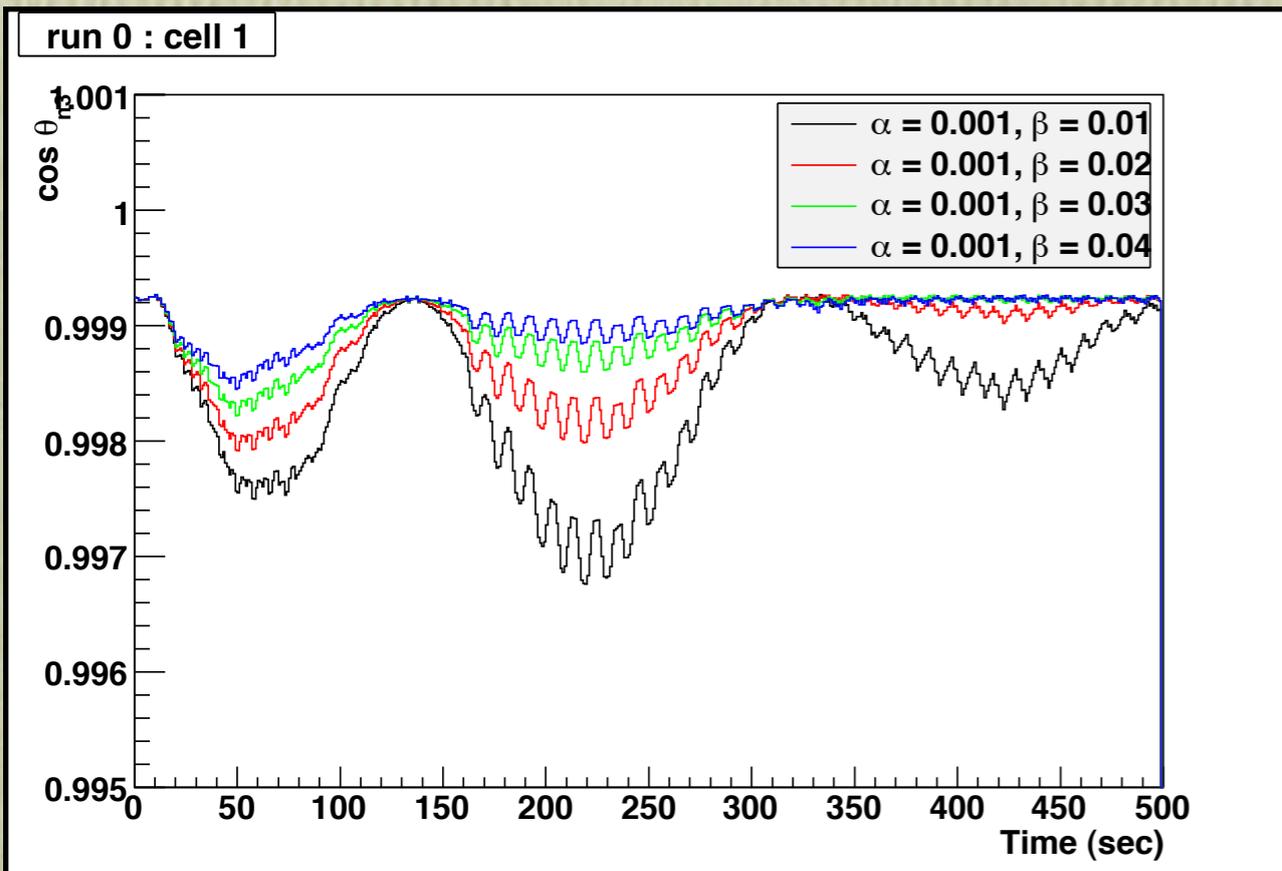
$$\frac{d\phi(t)}{dt} = N_0 e^{-\Gamma_{tot}t} \left[ \frac{1}{\tau_\beta} + \frac{1}{\tau_3} (1 - P_3 P_n \cos(\theta_{n3})) \right]$$

- The total light in the **first half** and the **second half** modulation should be *identical* at the critical dressing.
- The difference of the light in two periods will be the input of the feedback loop.
- The difference may come from **the offset of the dressing field** or **the EDM effective field**.
- The correction field can compensate the offset or the EDM effective field. Thus, the EDM can be obtained from **the correction field** in different runs.



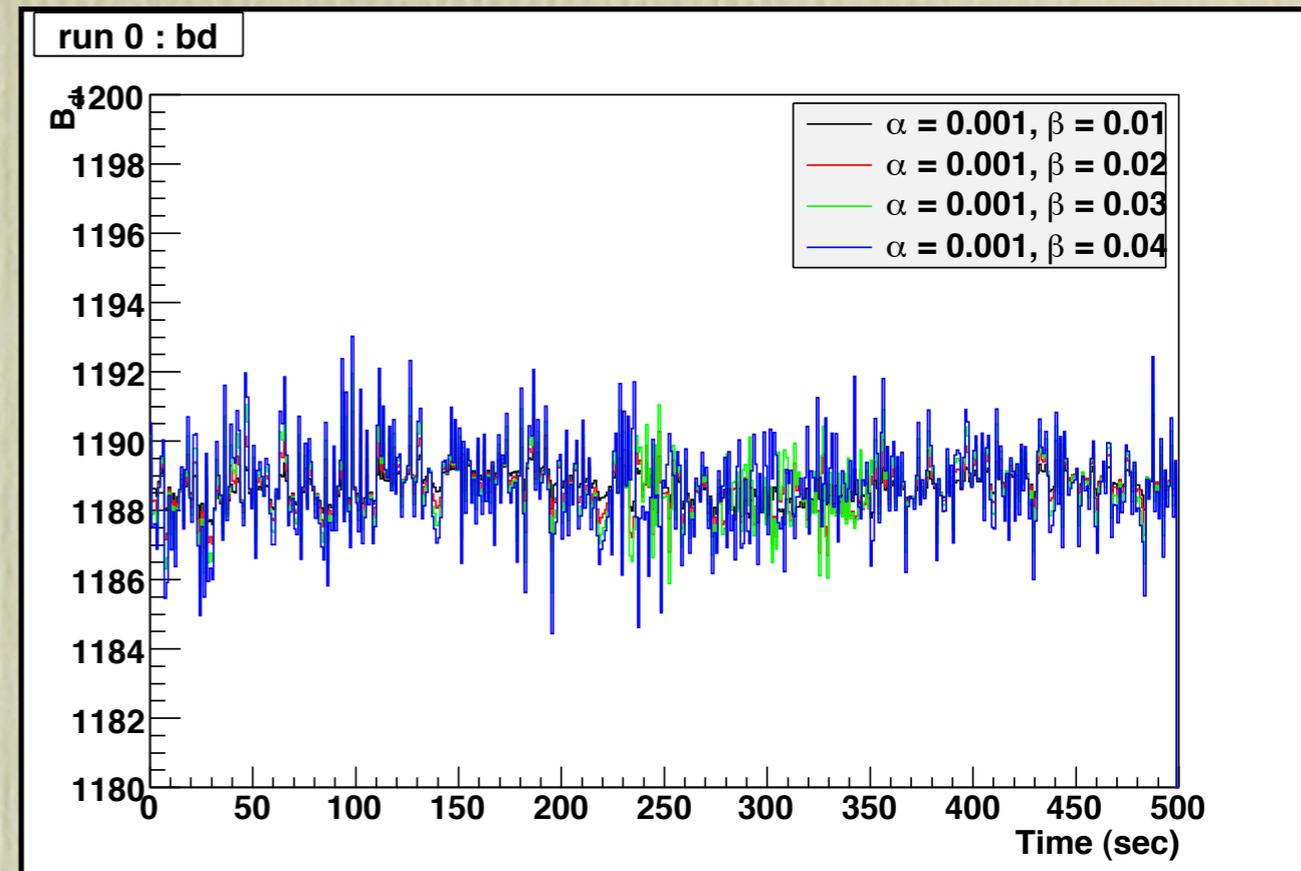
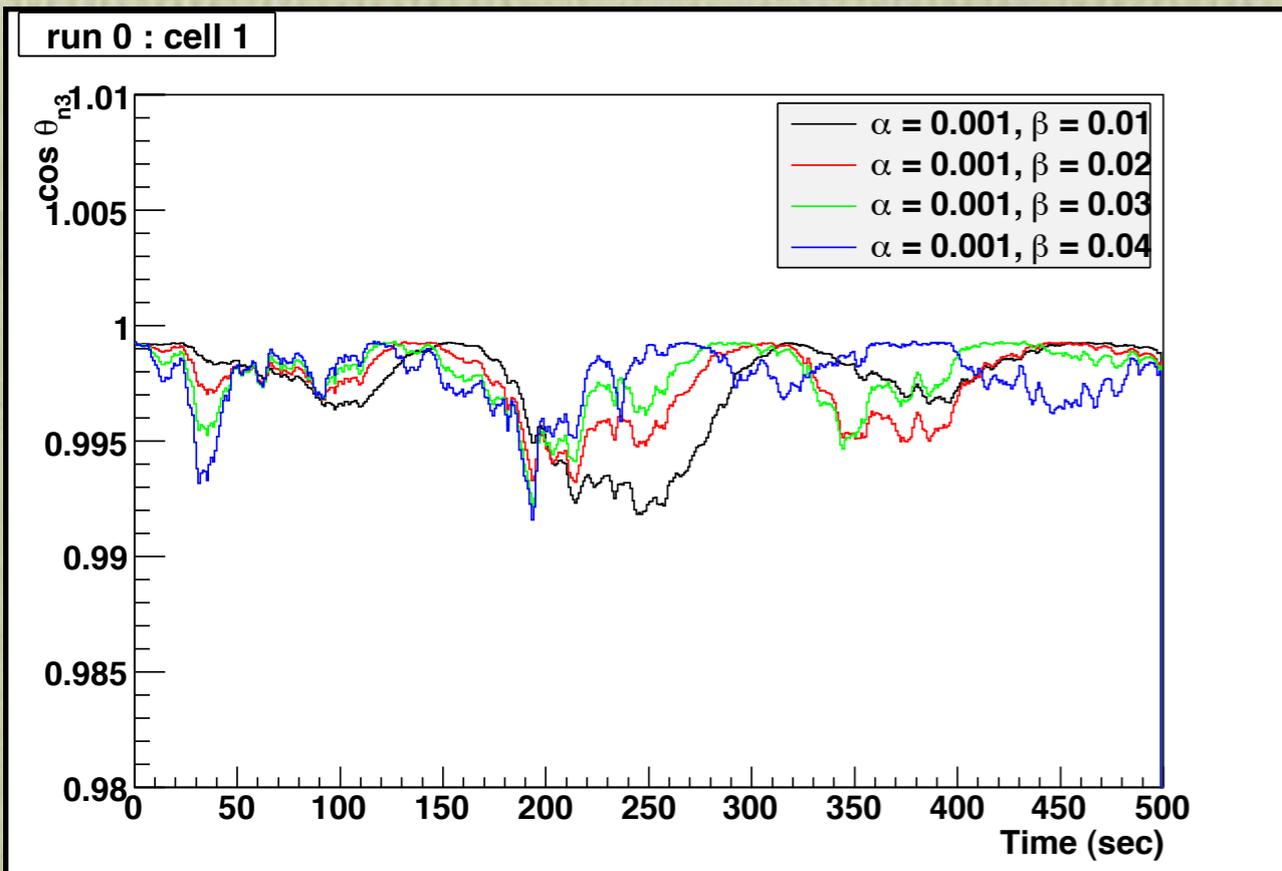
The distribution function =  $(d\phi/dt)/N_0$  depends on  $1 - \cos\theta_{n3}$ .

# Simulation of modulation/feedback



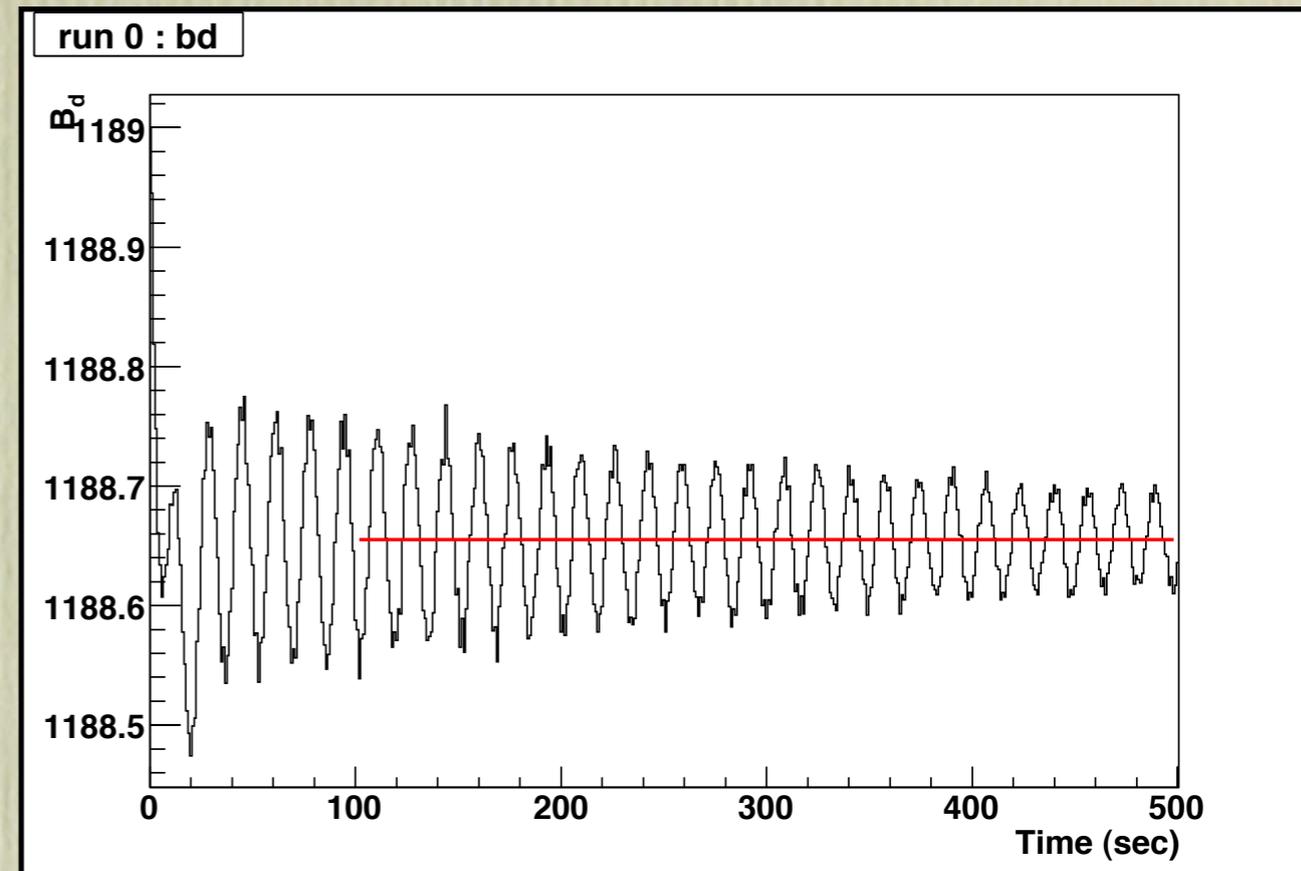
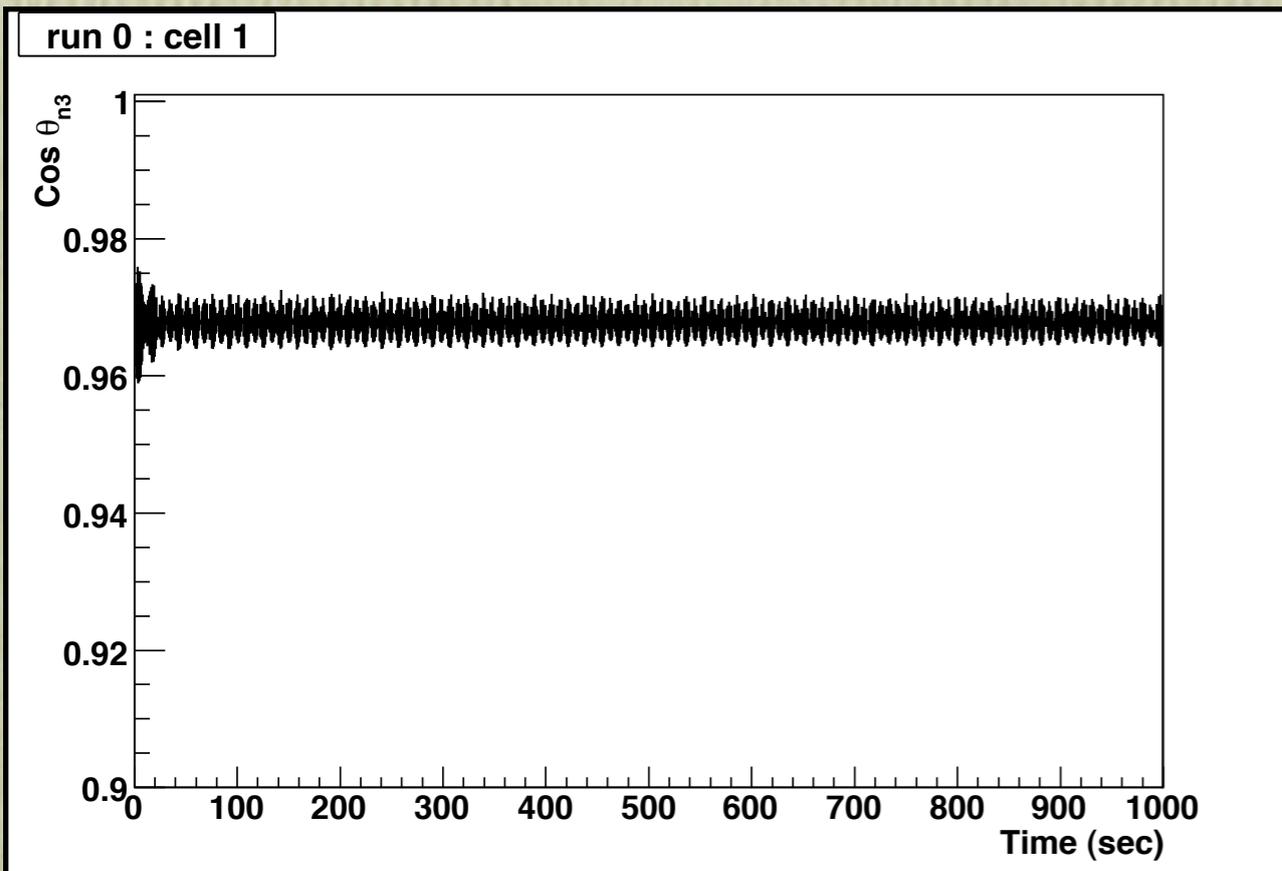
- One example *without* fluctuation with different  $\alpha$  and  $\beta$ . Set  $x=1.189$ ,  $B_m/B_d = 0.05$  and  $f_m=1$  Hz.
- $\cos \theta_{n3}$  can be tuned to be a constant.
- The system can be tuned to be the critical dressing.
- The feedback can be only applied in a single measurement cell in the SNS experiment (since both two cells share the same dressing coils).

# Monte Carlo for the feedback loop



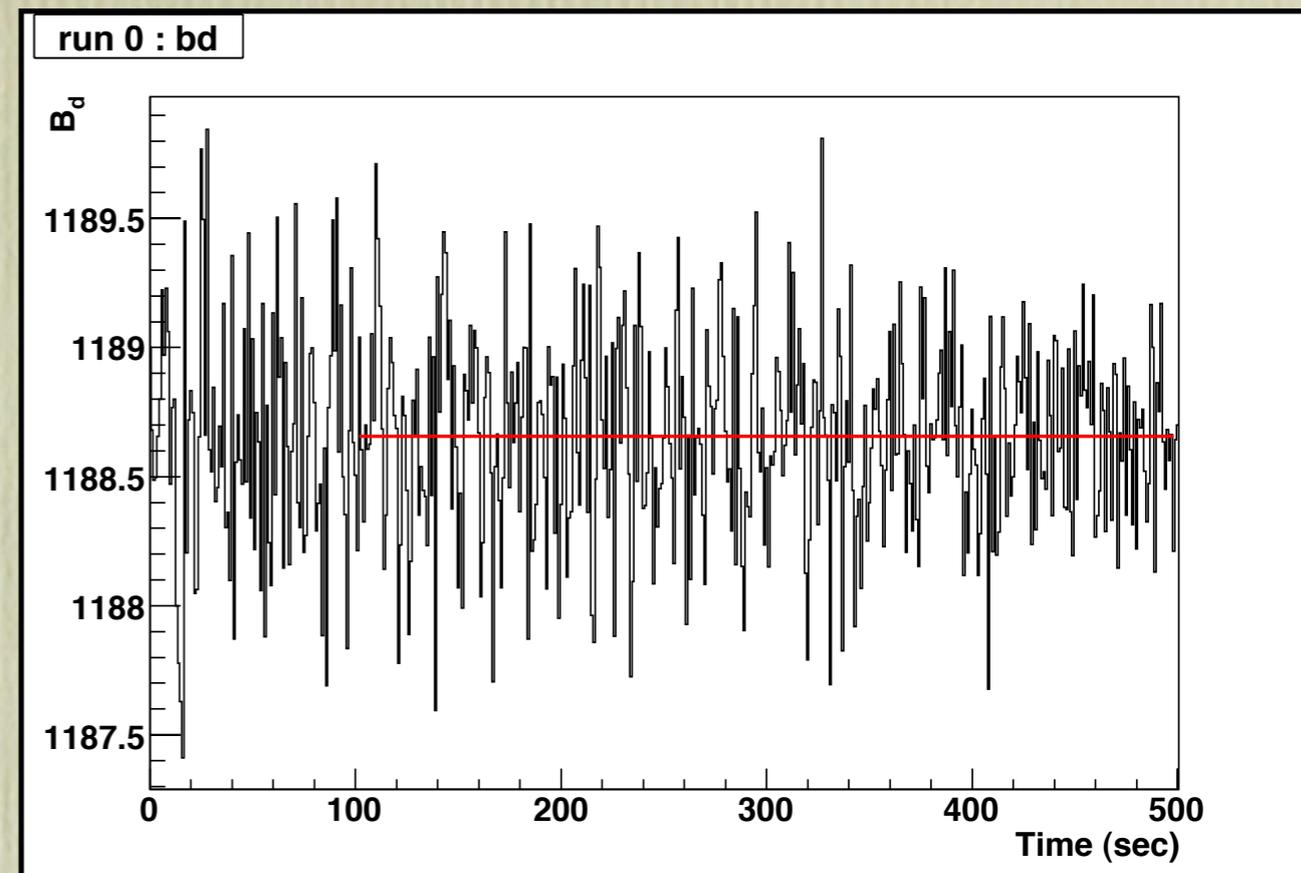
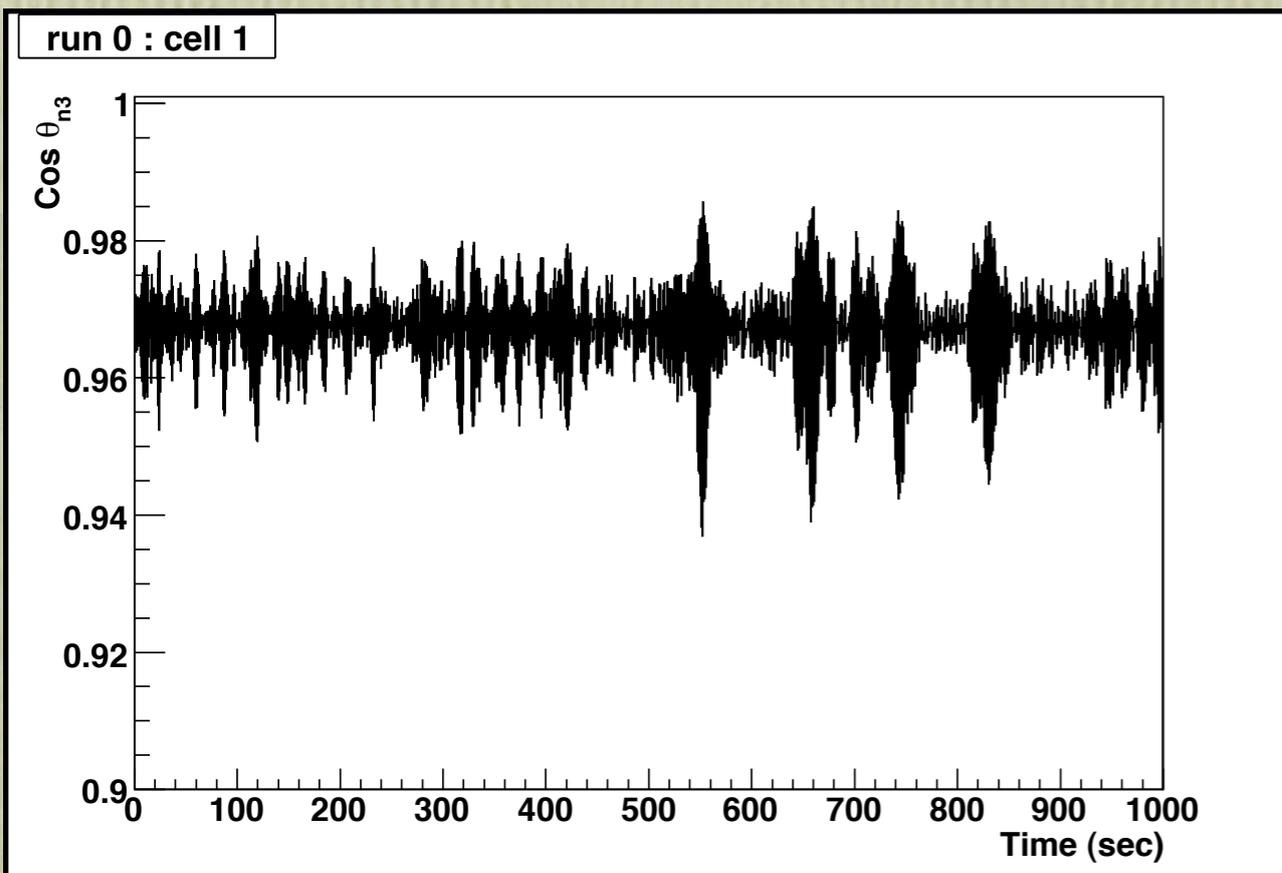
- One example *with* fluctuation with different  $\alpha$  and  $\beta$ . Set  $x=1.189$ ,  $B_m/B_d = 0.05$  and  $f_m=1$  sec.
- $\cos \theta_{n3}$  is (roughly) kept at a constant.
- Fit the dressing field *within* the final range. We use the time window  $t=100-500$  sec.
- Relate the EDM effective field to  $B_{d, \text{fit}}$ .

# Simulation for the feedback loop



- One example *without* fluctuation with  $\alpha=0.001$  and  $\beta=0.01$ . Set  $x=1.189$ ,  $B_d = 1189$  mG,  $B_m/B_d = 0.05$  and  $f_m=1$  Hz.
- $\text{Cos}\theta_{n3}$  can be tuned to be a constant.
- The system can be tuned to be the critical dressing.
- The feedback can be only applied in a single measurement cell in the SNS experiment(since both two cells share the same dressing coils).

# Monte Carlo for the feedback loop

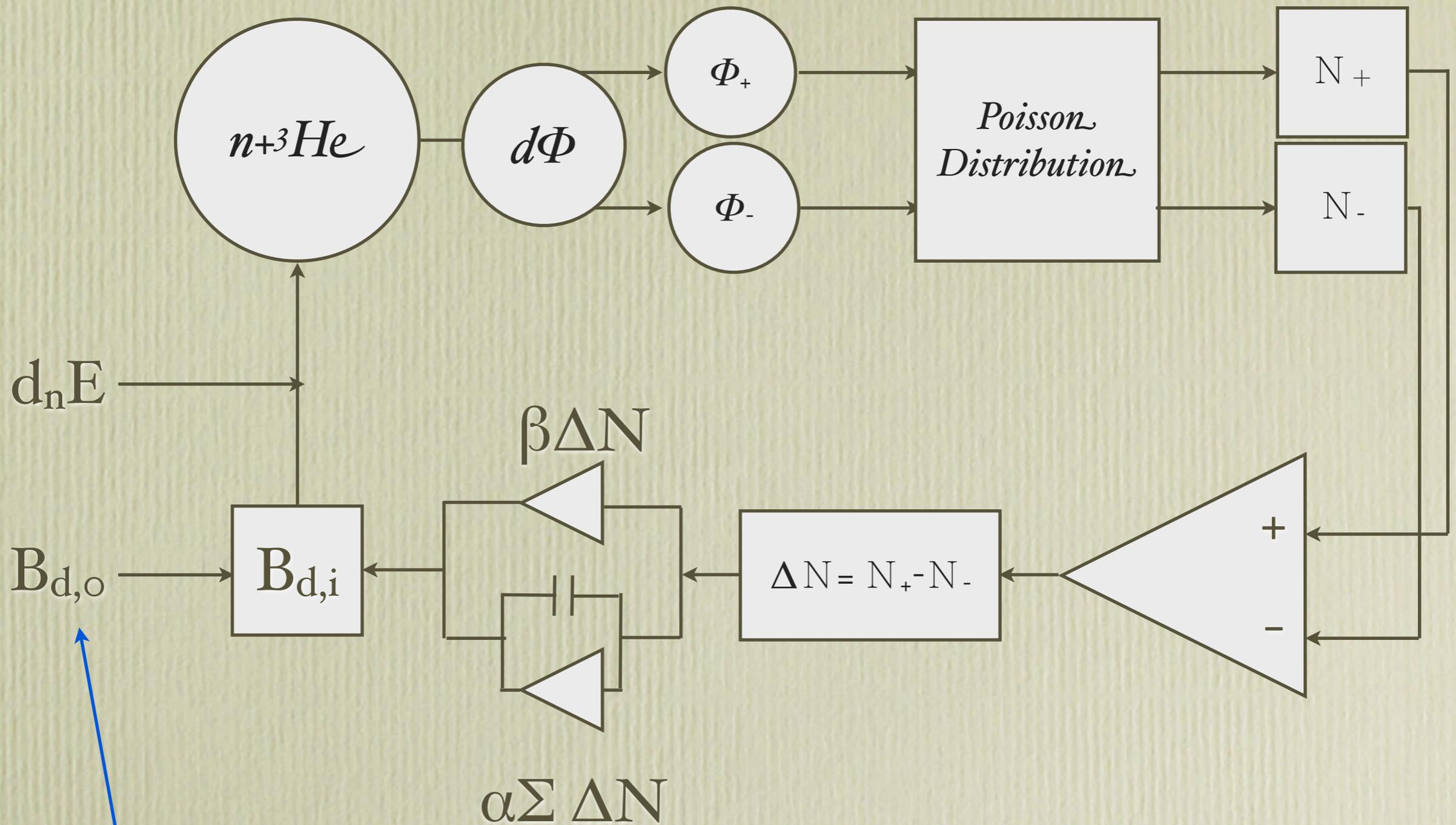


- One example *with* fluctuation with different  $\alpha$  and  $\beta$ . Set  $x=1.189$ ,  $B_m/B_d = 0.05$  and  $f_m=1$  sec.
- $\text{Cos } \theta_{n3}$  is (roughly) kept at a constant.
- Fit the dressing field *within* the final range. We use the time window  $t=100-500$  sec.
- Relate the EDM effective field to  $B_{d, \text{fit}}$ .

# Simulation of the dressed spin

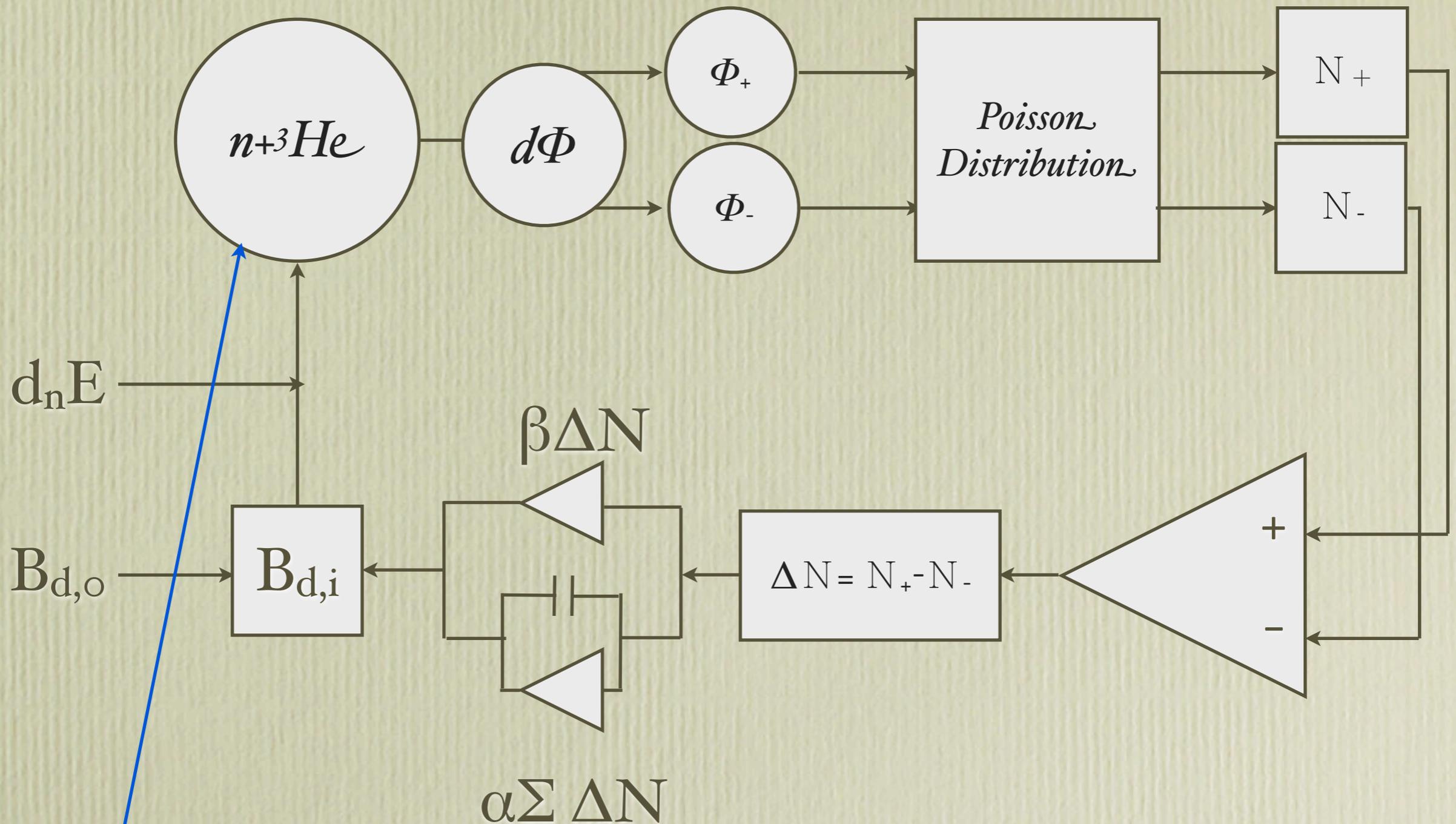
- The simulation result is consistent with the analytic solution.
- The simulation can be applied in any magnetic fields and spin dynamics. It will be used for **the feedback loop study** (proposed by Golub and Lamoreaux in 1994).
- It can be also used for
  - Optimization of  $\pi/2$  pulse for both neutron and  $^3\text{He}$ ,**
  - the systematic effect of **the pseudomagnetic field**, and
  - the systematic effect of **the initial polarization and the relative angle.**
- Together with **Monte Carlo**, we have a tool to study **the statistic error and systematic error** of the dressed spin technique.

# Schematic of feedback loop



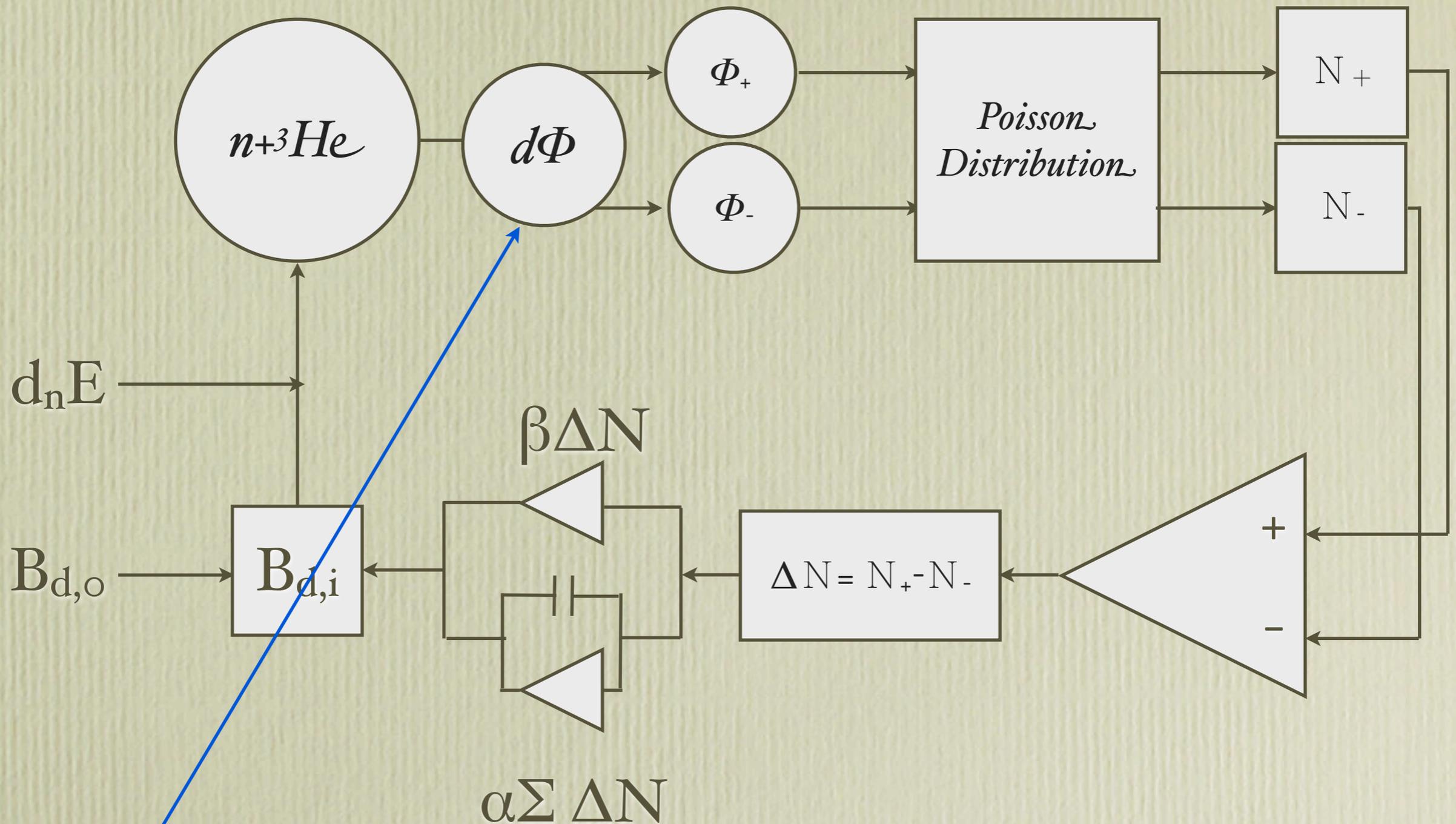
1. The initial value of  $B_d$  is  $B_{d,0}$ .

# Schematic of feedback loop



2. For given  $B_{d,i}$ , simulate  $n+^3\text{He}$  interaction. Use the Bloch equation to calculate  $\cos\theta_{n3}$  within the time window  $t = [t_i, t_i + \tau_m]$ , corresponding to one modulation cycle.

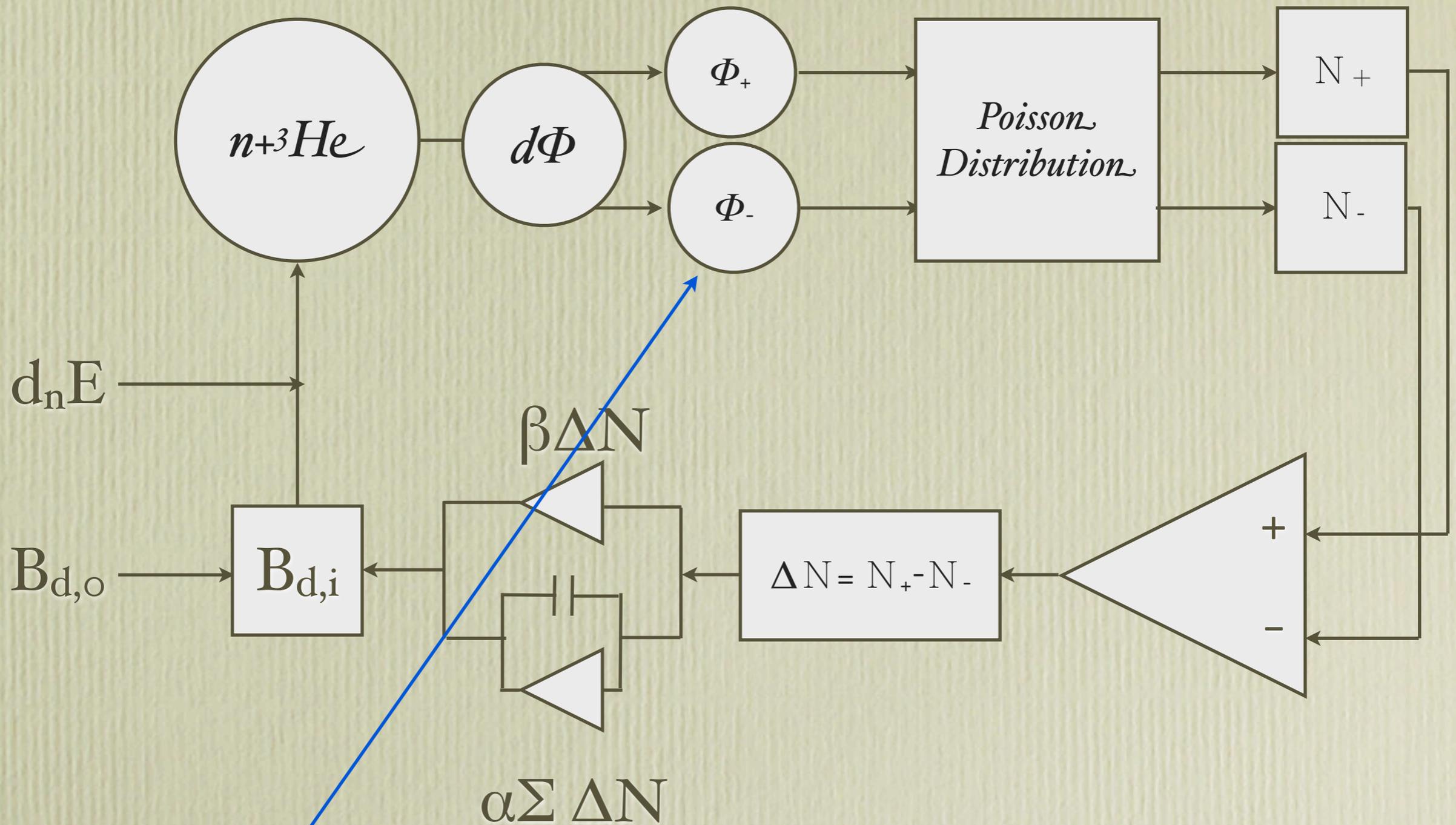
# Schematic of feedback loop



3. Insert  $\cos \theta_{n3}$  into the distribution function,

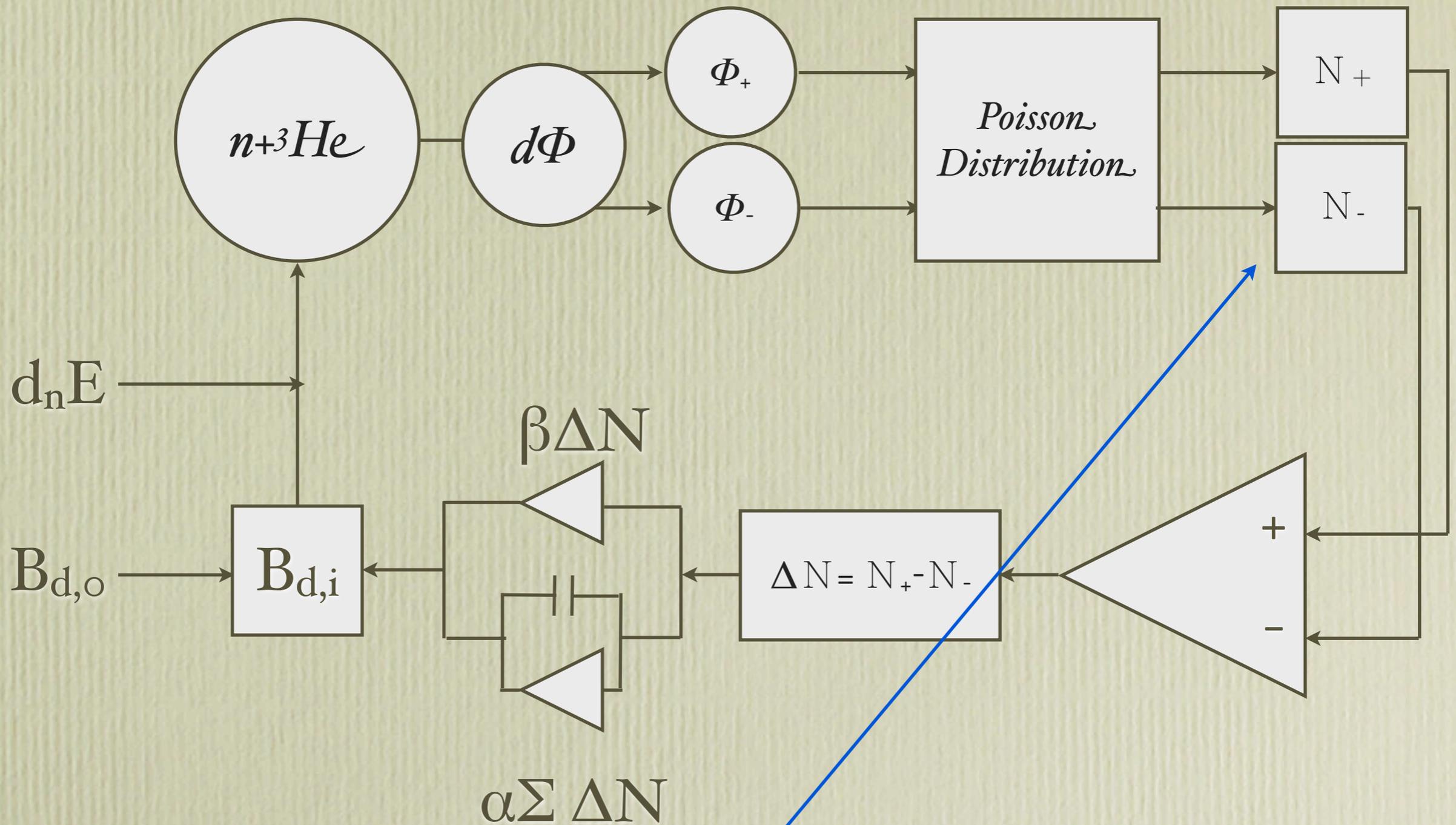
$$\frac{d\Phi}{dt} = N_0 e^{-\Gamma_{tot} t} \left[ \frac{1}{\tau_\beta} + \frac{1}{\tau_3} (1 - P_3 P_n \cos(\theta_{n3})) \right].$$

# Schematic of feedback loop



$$4. \Phi_{+,i} = \int_{t_i}^{t_i + \tau_m / 2} \frac{d\Phi}{dt} dt, \quad \Phi_{-,i} = \int_{t_i + \tau_m / 2}^{t_i + \tau_m} \frac{d\Phi}{dt} dt$$

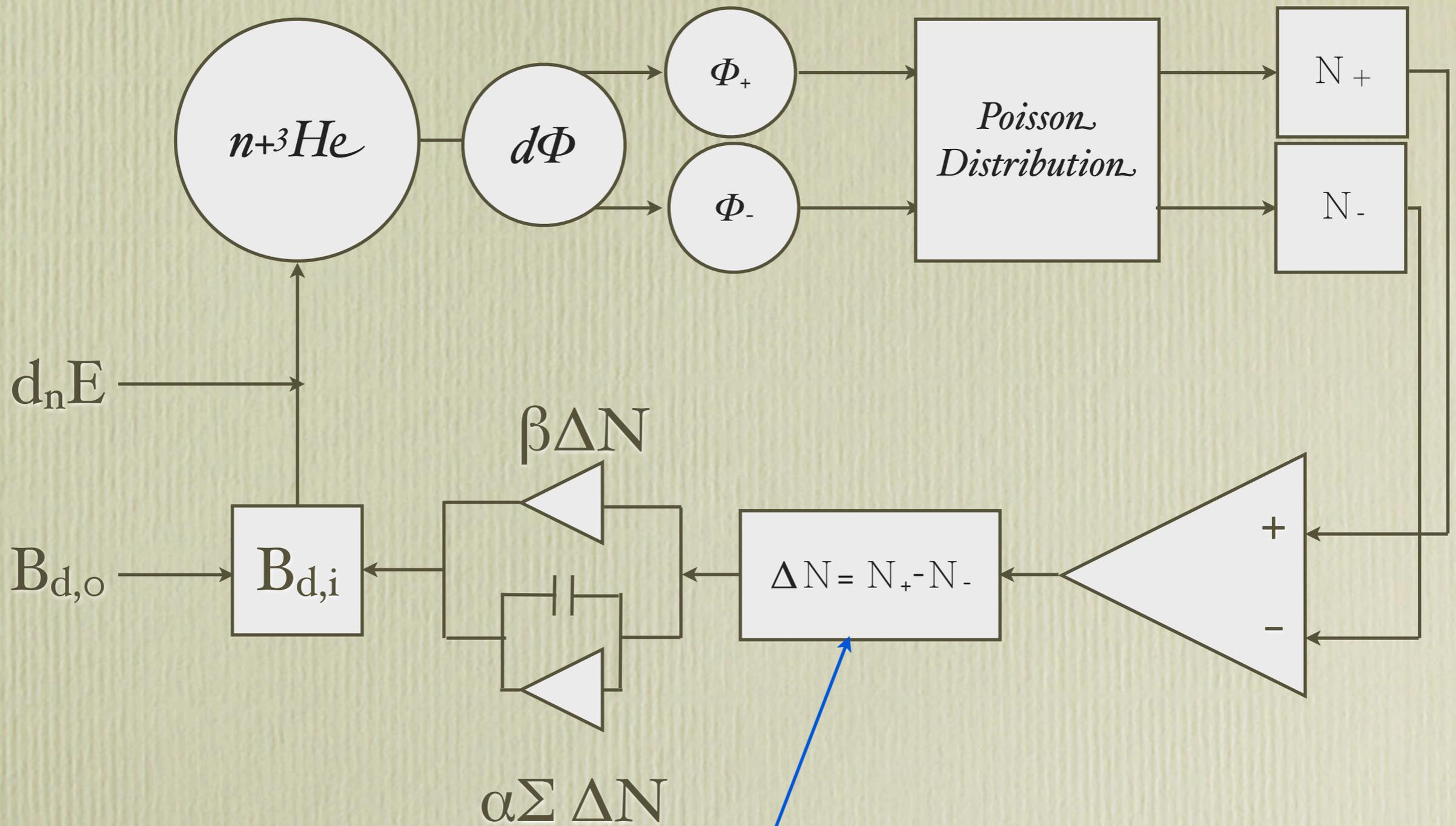
# Schematic of feedback loop



5. Generate Monte Carlo:

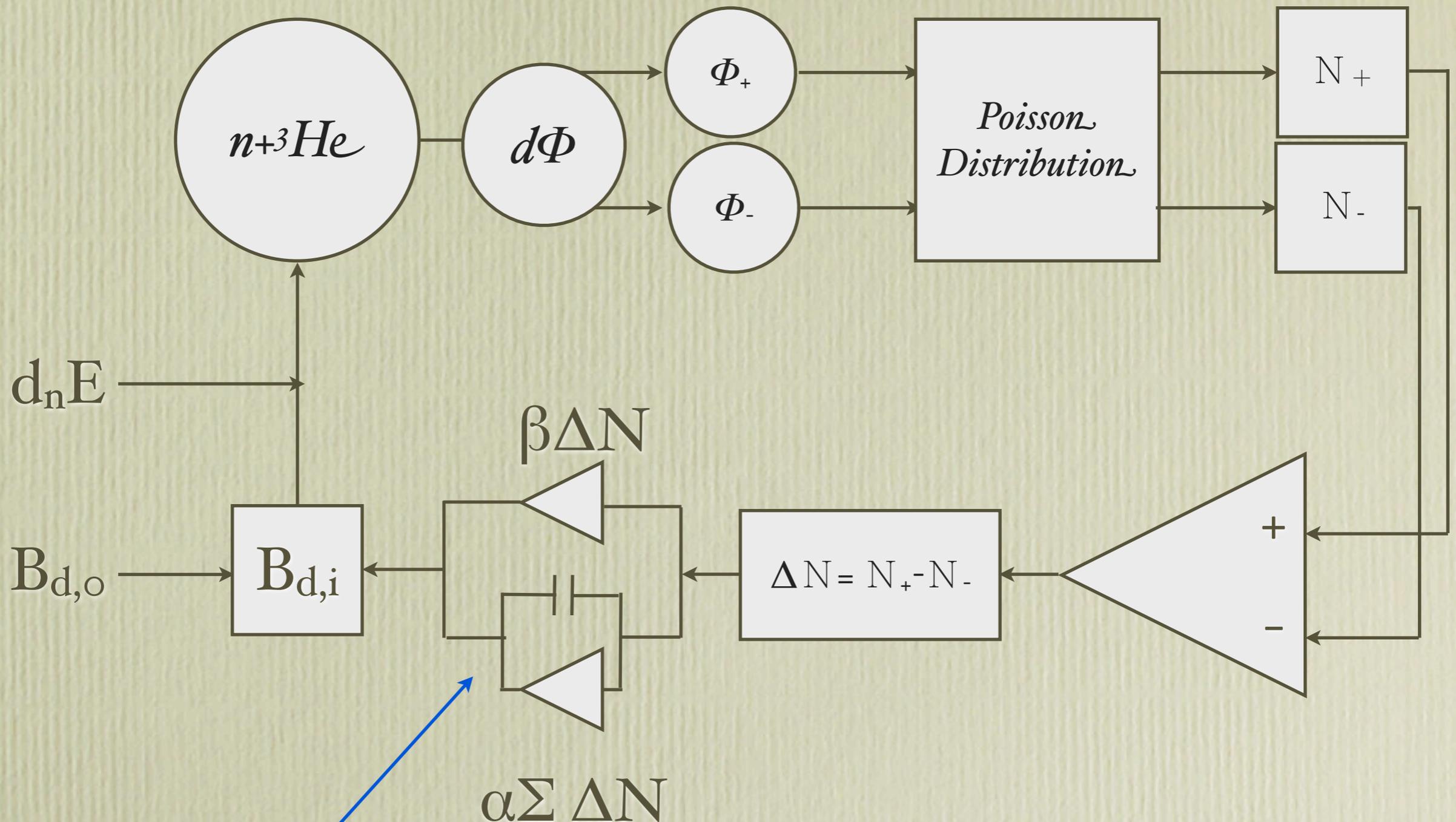
$$N_{+,i} = \text{Poisson}(\Phi_{+,i}) \text{ and } N_{-,i} = \text{Poisson}(\Phi_{-,i})$$

# Schematic of feedback loop



6. Calculate  $\Delta N_i = N_{+,i} - N_{-,i}$ .

# Schematic of feedback loop

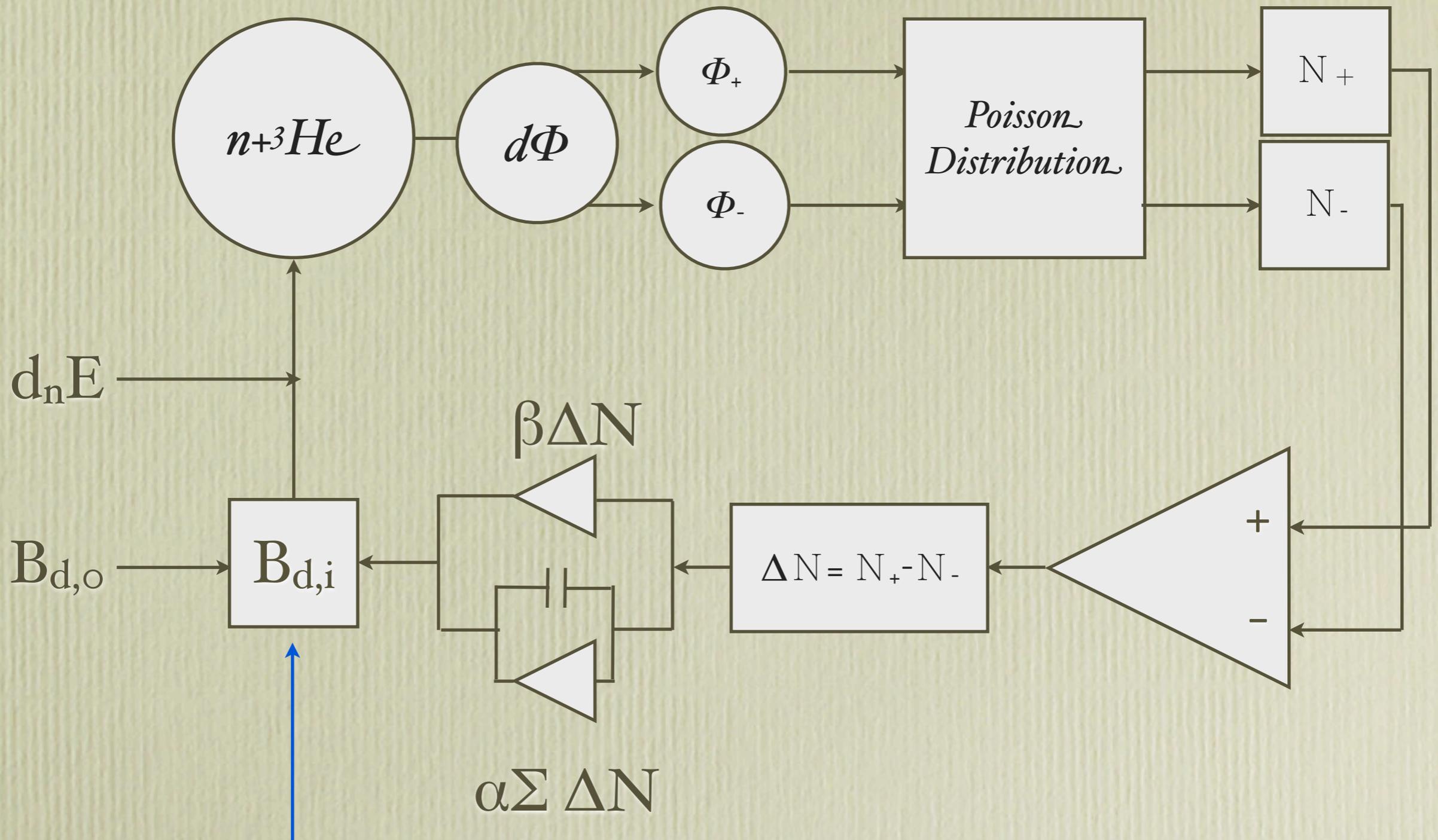


7. Run the feedback loop process and obtain the modified dressing field.

- Low Pass Integrator:  $B_{c,0,\alpha} = B_{d,0}$ ,  $B_{c,i,\alpha} = B_{c,i-1,\alpha} - \alpha \Delta N_i$ .

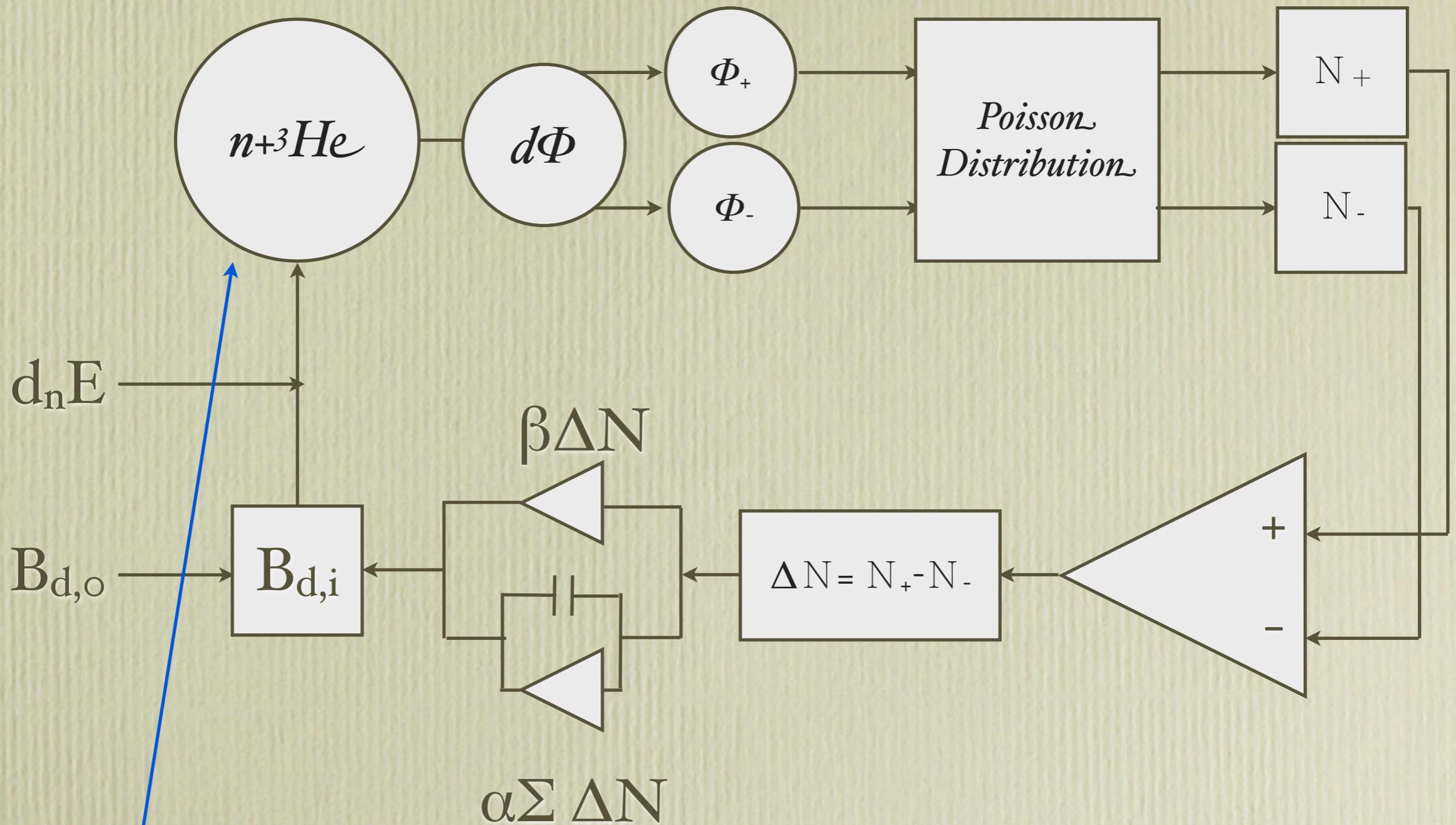
- Amplifier:  $B_{c,i,\beta} = -\beta \times \Delta N_i$ . 69

# Schematic of feedback loop



8. Modified field:  $B_{d,i+1} = B_{c,i,\alpha} + B_{c,i,\beta}$ .

# Schematic of feedback loop



9. Go to 2 and repeat the loop.

# Approach of the feedback method

- The feedback method is under investigation. Several factors should be considered.
- The modulation amplitude and period cannot be too short since there will not be enough events for the feedback loop.
- The modulation amplitude cannot be too large since the Bessel function is not symmetric at the critical point if the modulation is too large.
- The modulation period cannot be too long either since the decay effect will be involved and there is not enough time to correct the dressing field.
- One dominant factor is **the decay** which can affect the sensitivity a factor of 5 from the Monte Carlo study.
- **Correction factors** for  $\alpha$  and  $\beta$  are necessary to compensate the decay effect.
- The feedback method can only be applied to a **single cell** since two cells have the same dressing coils.
- Although the feedback loop can self-correct, different kinds of systematic error, including the pseudomagnetic field, the polarization of neutron and  $^3\text{He}$ , the neutron and  $^3\text{He}$  density, etc., should be studied.

# Summary

- The dressed spin measurement is consistent with the prediction. We can apply the theory to estimate the critical dressing at different magnetic field setups.
- It may help to the design of the dressing coils since we may not need to run at the high dressing frequency condition.
- It will be of interest to extend the measurement to higher  $x$  range.
- The Bloch equation simulation can simulate the spin dynamics in any magnetic fields. It can be used in many subjects of the nEDM, like the  $\pi/2$  optimization, the pseudomagnetic field.
- The Monte Carlo study can help to study the statistic sensitivity of the feedback loop. It will be done in months.

# Pseudomagnetic field

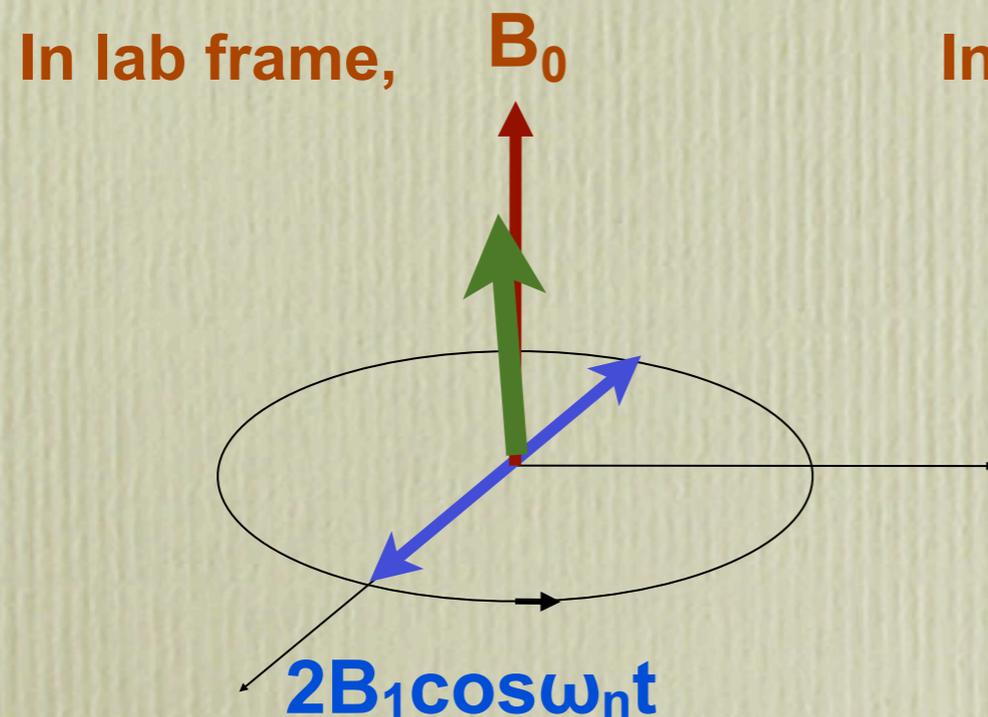
- The pseudomagnetic moment, which is originated from the real part of  $n\text{-}^3\text{He}$  scattering length (spin-dependent), like magnetic dipole moment, can produce the pseudomagnetic field, along the  $^3\text{He}$  spin direction.
- Ref : Nuclear Magnetism:order and disorder, A. Abragam and M. Goldman and Physics Report(1994)
- $B_a$  is around 1000 times larger than the  $^3\text{He}$  magnetization.
- $B_a$  is proportional to  $P_3$ , which is time dependent.

# $\pi/2$ Pulse

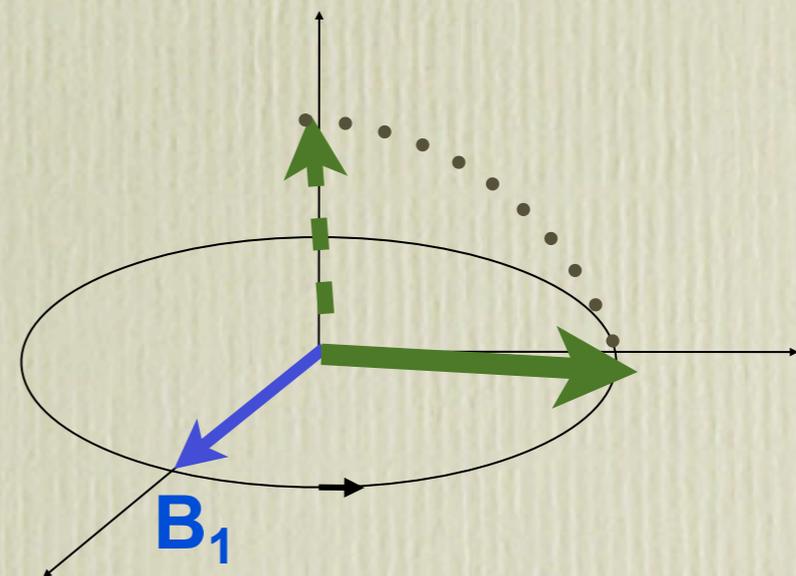
- Apply a linear oscillatory RF magnetic field along the x-axis.
- The frequency is expected at the Larmor frequencies of neutron ( $\omega_n$ ).

$$B_{RF}(t) = 2B_1 \cos \omega_n t \hat{x} = B_1 (\cos(\omega_n t) \hat{x} - \sin(\omega_n t) \hat{y}) + B_1 (\cos(\omega_n t) \hat{x} + \sin(\omega_n t) \hat{y})$$

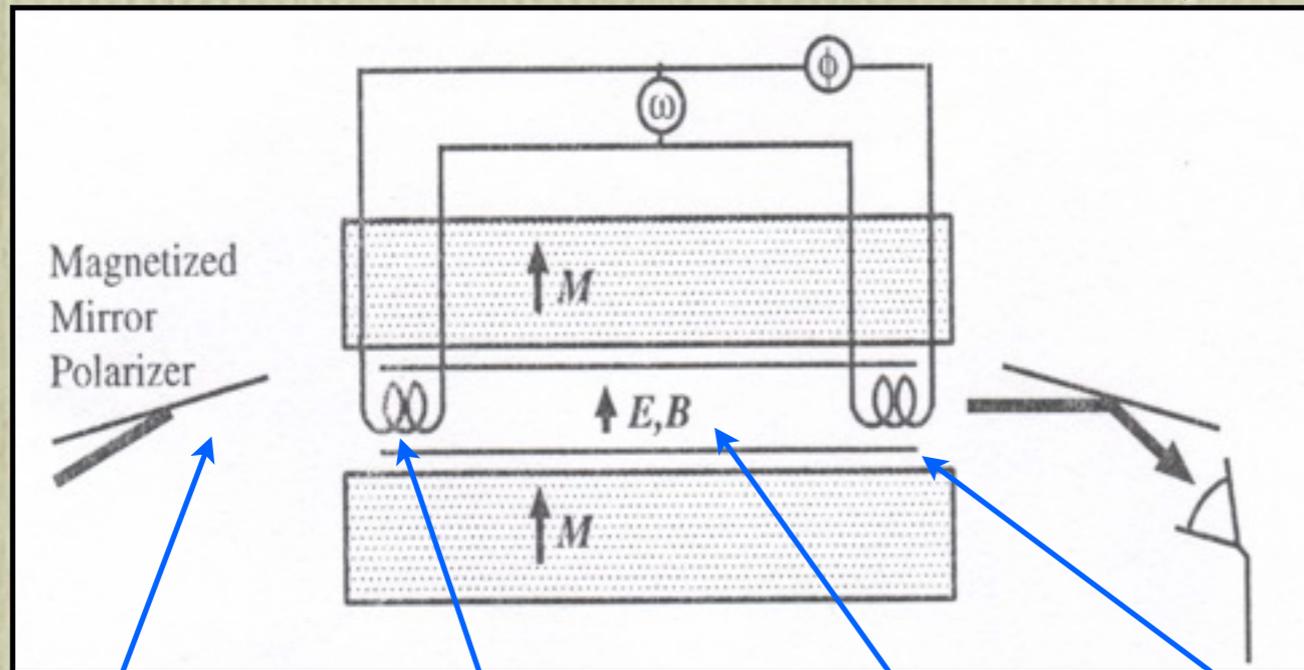
- In the rotating frame, only a constant  $B_1$  along the x-axis and another high frequency field. Ignore the high frequency term. The constant  $B_1$  field can rotate the spin from the z-axis to the x-y plane within a period of time.



In rotating frame,



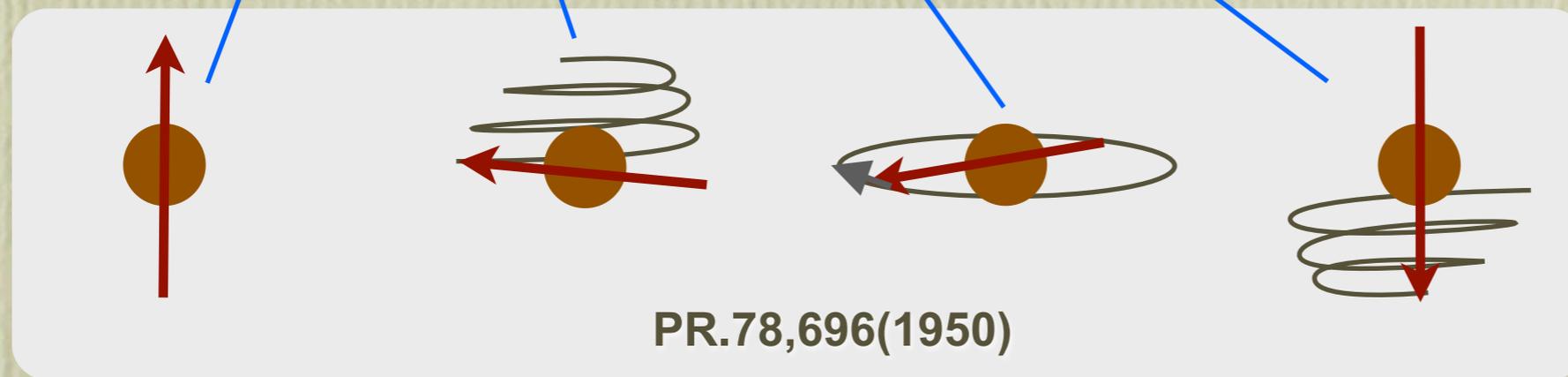
# Purcell and Ramsey's Experiment



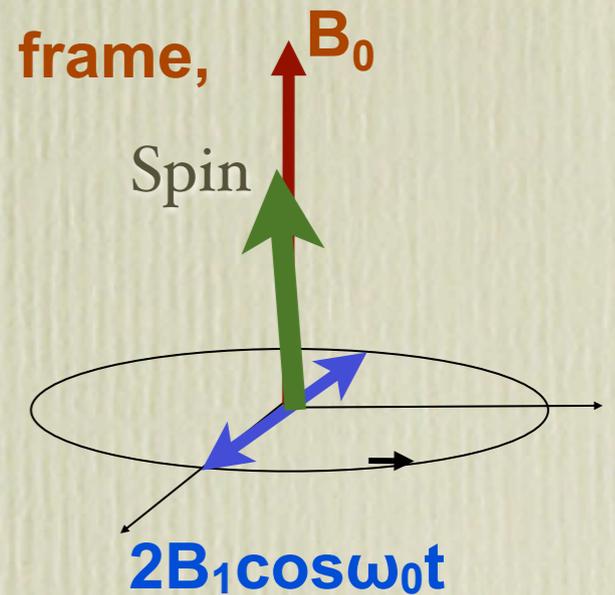
- Table-size experiment using **separated oscillatory field.**

• PR.108,120(1957):

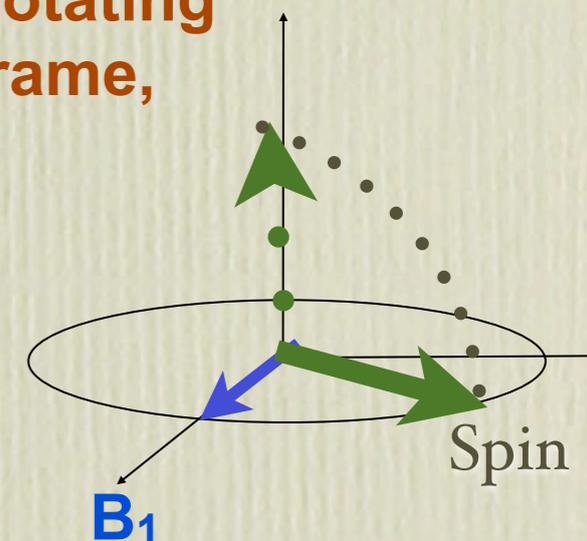
$$d_n < 5 \times 10^{-20} \text{ e cm}$$



In lab frame,



In rotating frame,

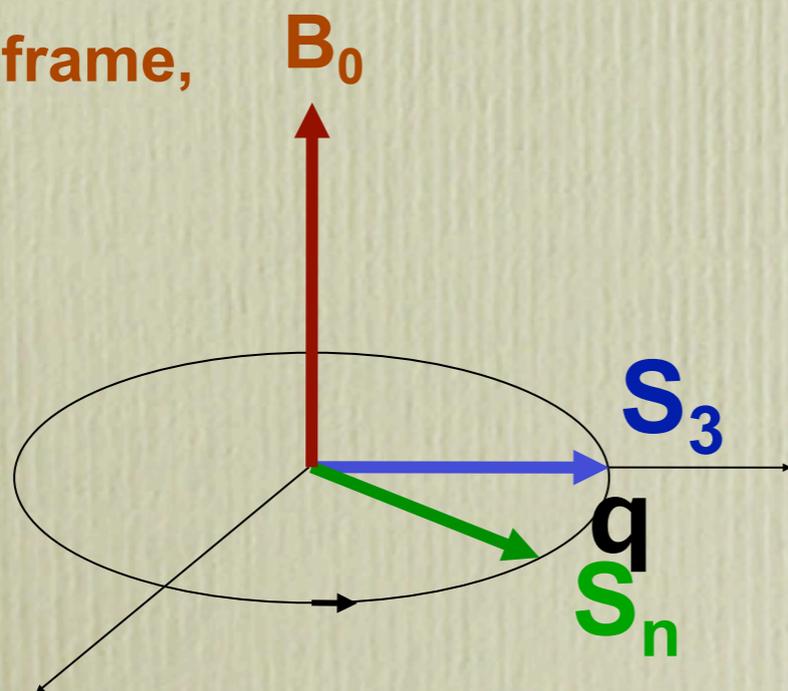


RF	off	on	off	on
	neutron spin is parallel to holding field	first $\pi/2$ pulse is applied; spin is rotated to be perpendicular to holding field	neutrons precess during storage time	second $\pi/2$ pulse is applied; spin is rotated to be anti-parallel to holding field

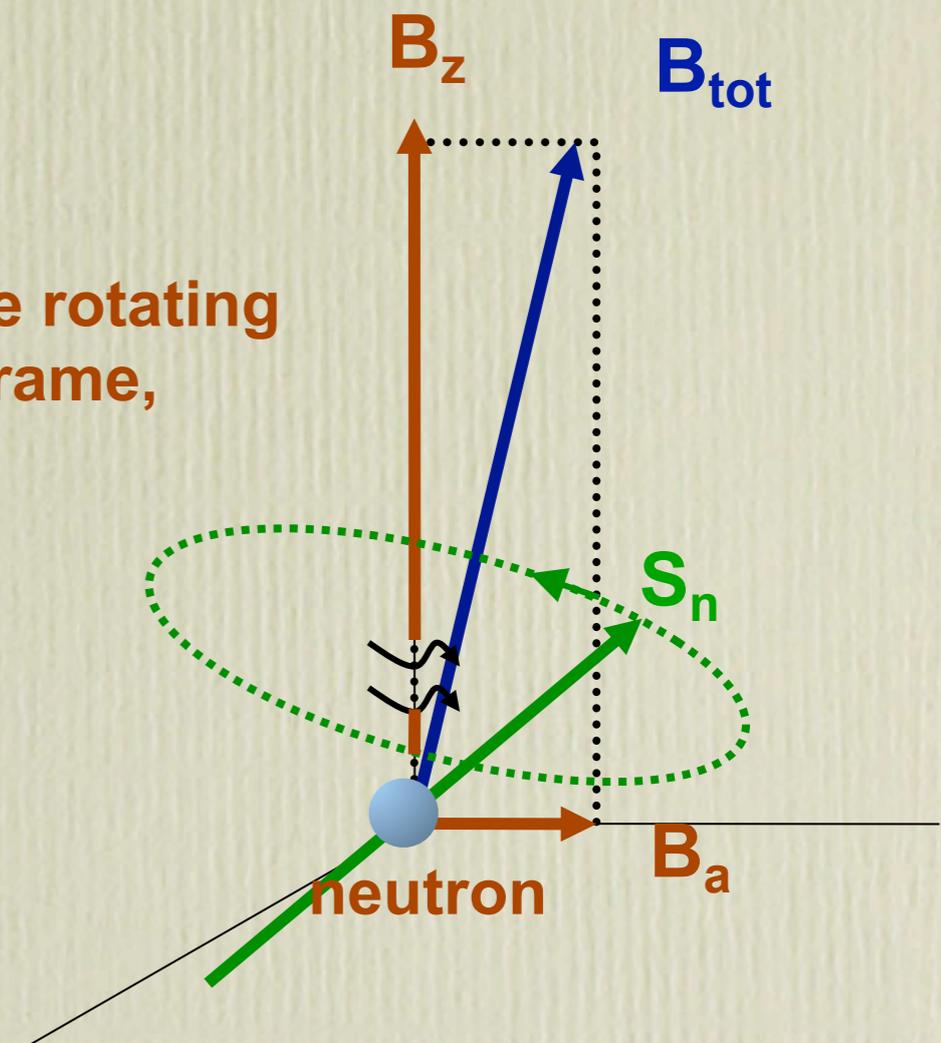
# Pseudomagnetic field

- The pseudomagnetic moment, which is originated from the real part of n-<sup>3</sup>He scattering length (spin-dependent), like magnetic dipole moment, can produce the pseudomagnetic field, along the <sup>3</sup>He spin direction.
- Ref : Nuclear Magnetism:order and disorder, A. Abragam and M. Goldman and Physics Report(1994)
- B<sub>a</sub> is around 1000 times larger than the <sup>3</sup>He magnetization.
- B<sub>a</sub> is proportional to P<sub>3</sub>, which is time dependent. The pseudomagnetic field is along the spin direction of <sup>3</sup>He. In the <sup>3</sup>He Larmor frequency rotating frame, the magnetic field is

In lab frame,

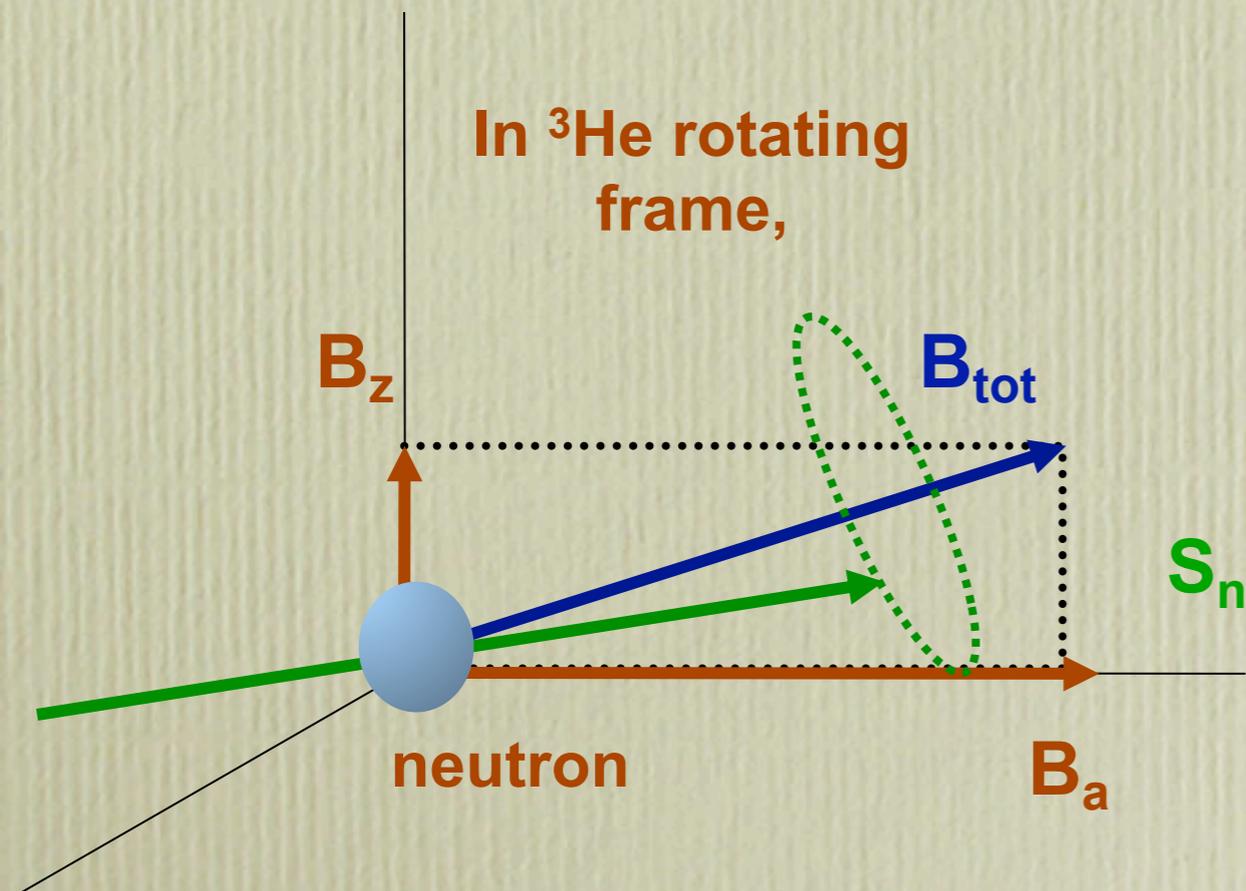


In <sup>3</sup>He rotating frame,



# Dressing field plus pseudomagnetic field

- At the critical dressing ( $g'_3 = g'_n$ ), the constant field becomes very small in the rotating frame.
- The neutrons spin direction will be confined in a small cone around the  $^3\text{He}$  spin direction.
- The EDM signal will be reduced by the pseudomagnetic field.
- Modulation and feedback of the dressing field are proposed to overcome this problem (discussed in the Physics Report).



# The schematic plot for the feedback loop (by Golub and Lamoreaux)

40

*R. Golub and S.K. Lamoreaux, Neutron electric-dipole moment, ultracold neutrons and polarized  $^3\text{He}$*

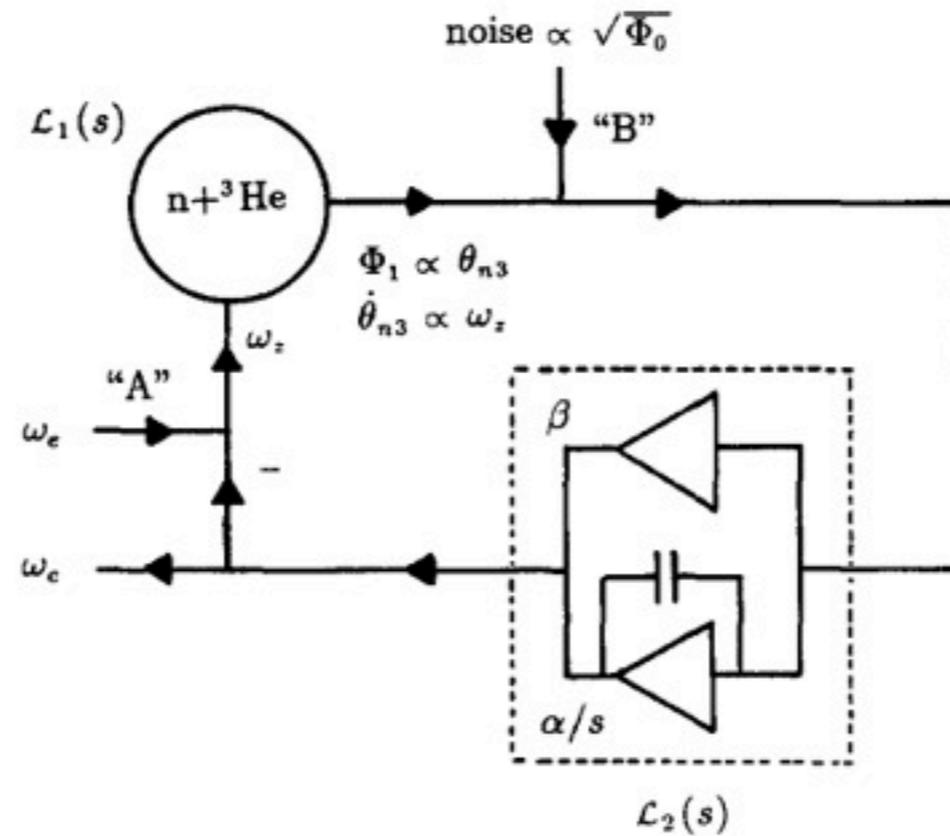


Fig. 7. Schematic of a feedback system following standard phaselock techniques.  $\omega_z$  represents the total magnetic field seen by the UCN.

# Generate Monte Carlo for the feedback loop

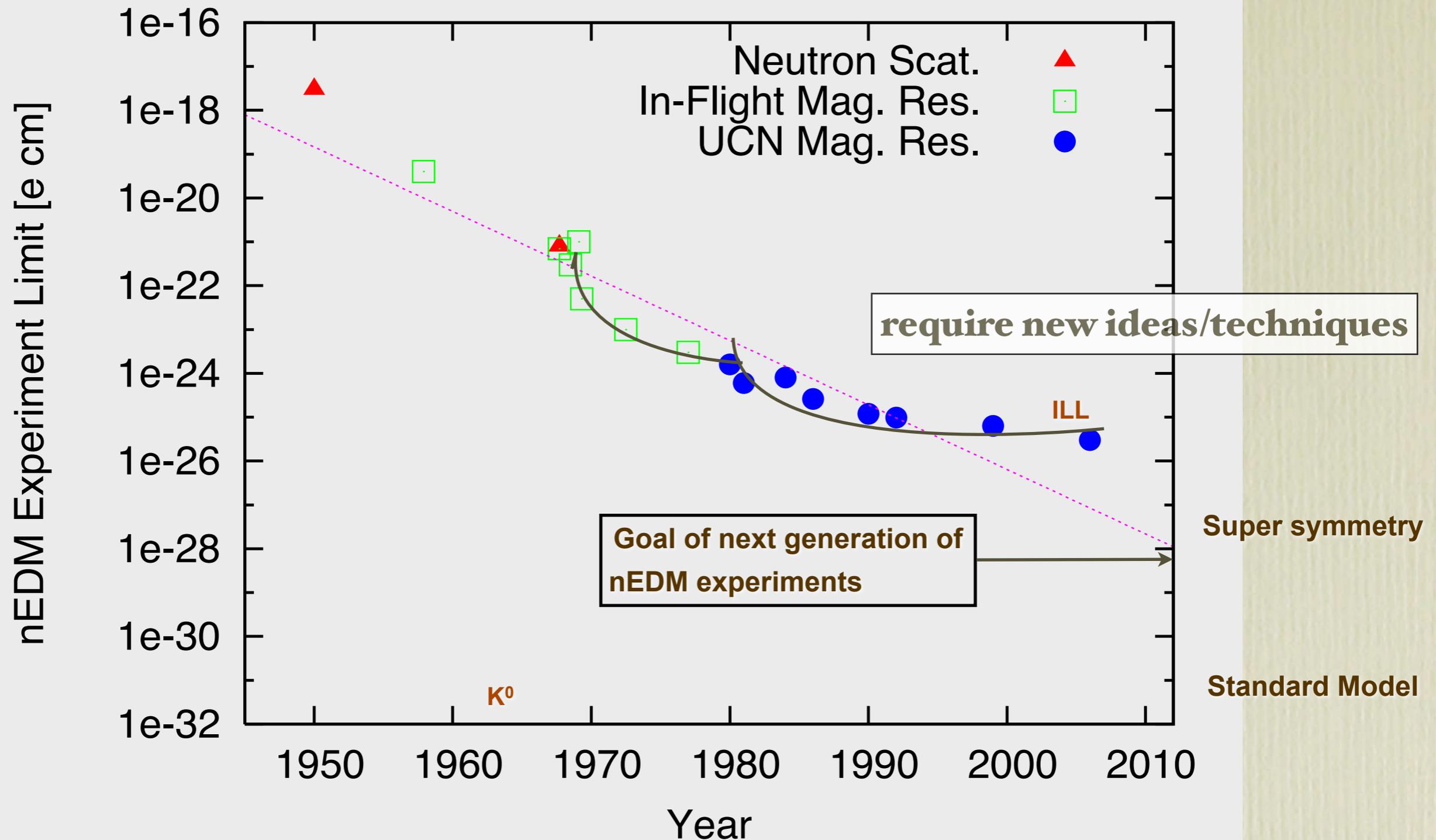
1. The initial value of  $B_d$  is  $B_{d,0}$ .
2. For given  $B_{d,i}$ , use the Bloch equation to calculate  $\cos \theta_{n3}$  within the time window  $t = [t_i, t_i + \tau_m]$ , corresponding to one modulation cycle.
3. Insert  $\cos \theta_{n3}$  into the distribution function,  $\frac{d\Phi}{dt}$ .
4. Calculate:

$$\Phi_{+,i} = \int_{t_i}^{t_i + \tau_m/2} \frac{d\Phi}{dt} dt,$$
$$\Phi_{-,i} = \int_{t_i + \tau_m/2}^{t_i + \tau_m} \frac{d\Phi}{dt} dt,$$

5. Generate Monte Carlo  $N_{+,i} = \text{Poisson}(\Phi_{+,i})$  and  $N_{-,i} = \text{Poisson}(\Phi_{-,i})$
6. Calculate  $\Delta N_i = N_{+,i} - N_{-,i}$ .
7. Run the feedback loop process and obtain the modified dressing field.
  - Low Pass Integrator:  $B_{c,0,\alpha} = B_{d,0}$ ,  $B_{c,i,\alpha} = B_{c,i-1,\alpha} - \alpha \Delta N_i$ .
  - Amplifier:  $B_{c,i,\beta} = -\beta \times \Delta N_i$ .
  - Modified field:  $B_{d,i+1} = B_{c,i,\alpha} + B_{c,i,\beta}$ .
8. Go to 2 and repeat the loop.

$\alpha, \beta$  are feedback parameters.

# History of neutron EDM search



- Current neutron EDM upper limit:  $< 2.9 \times 10^{-26}$  e cm (90% C.L.)
- Still no evidence for neutron EDM.

# Neutron electric dipole moment (Early history)



Dirac

$$\vec{d}_n = \int dx^3 \rho \vec{x} = d_n \hat{S}$$

- Electric dipole moment (EDM) is the first moment of the charge distribution ( $\rho$ ).
- Dirac's **magnetic monopole** can generate an EDM (1948).
- The EDM (**vector**) is parallel to the **Spin (axial vector)** direction.
- EDM is **Parity-odd** but spin is **Parity-even**.

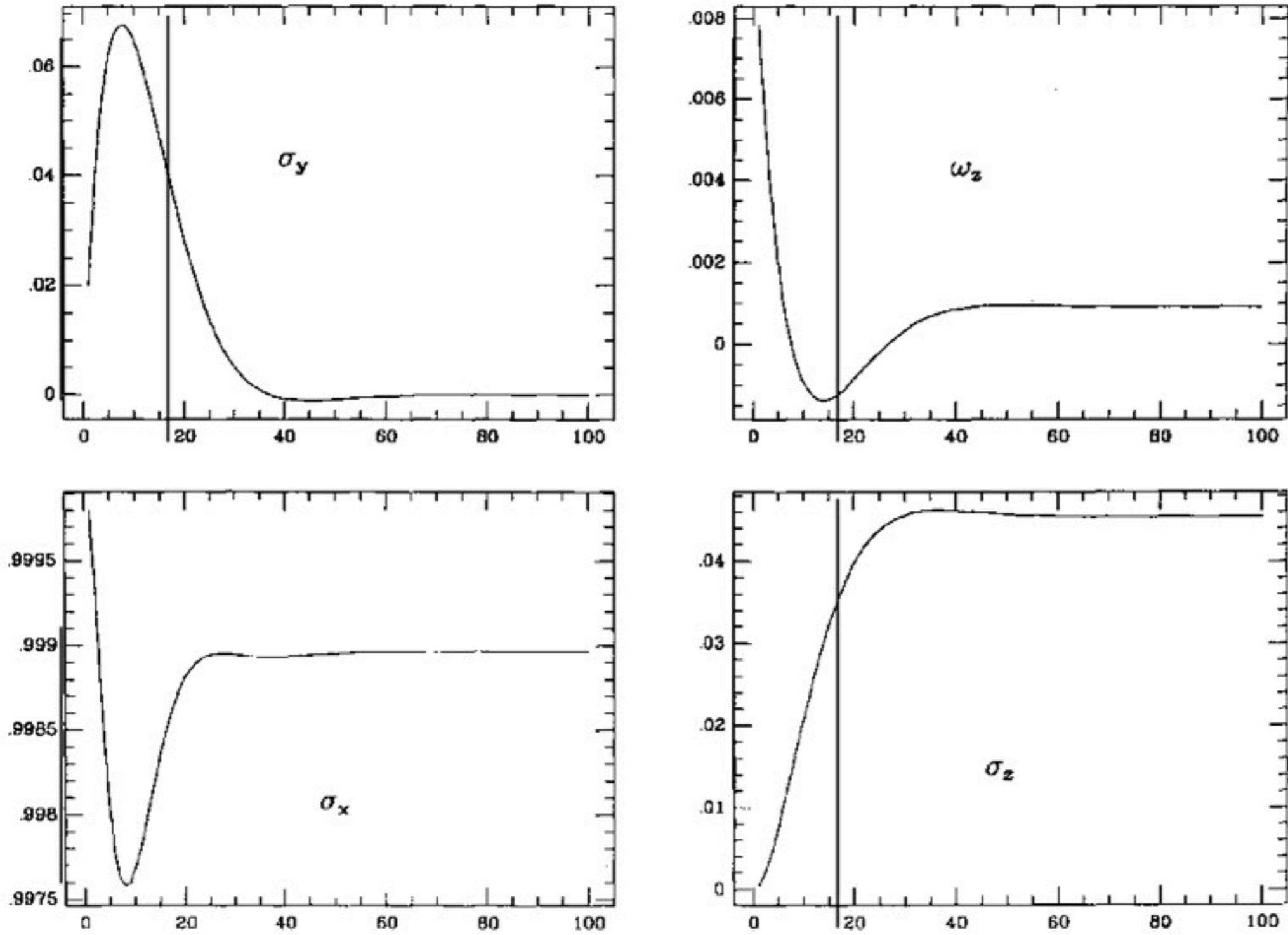
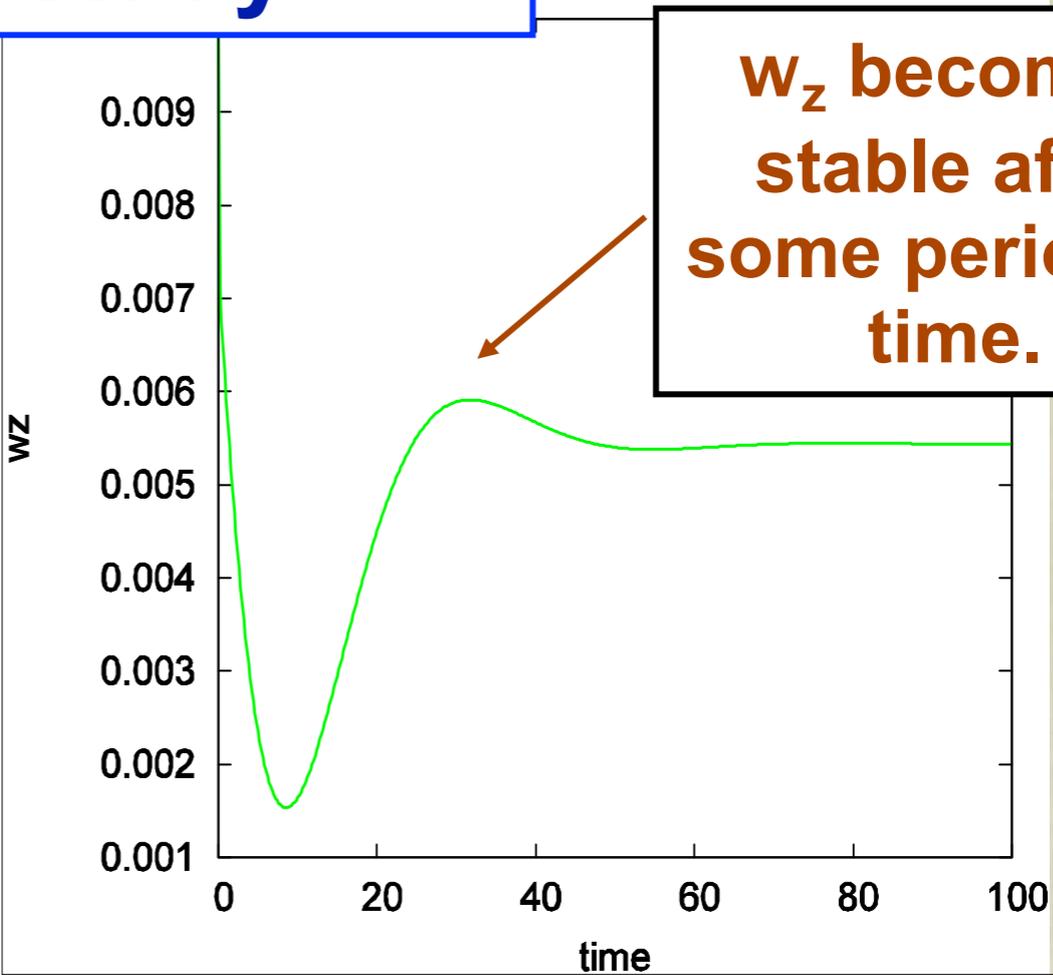
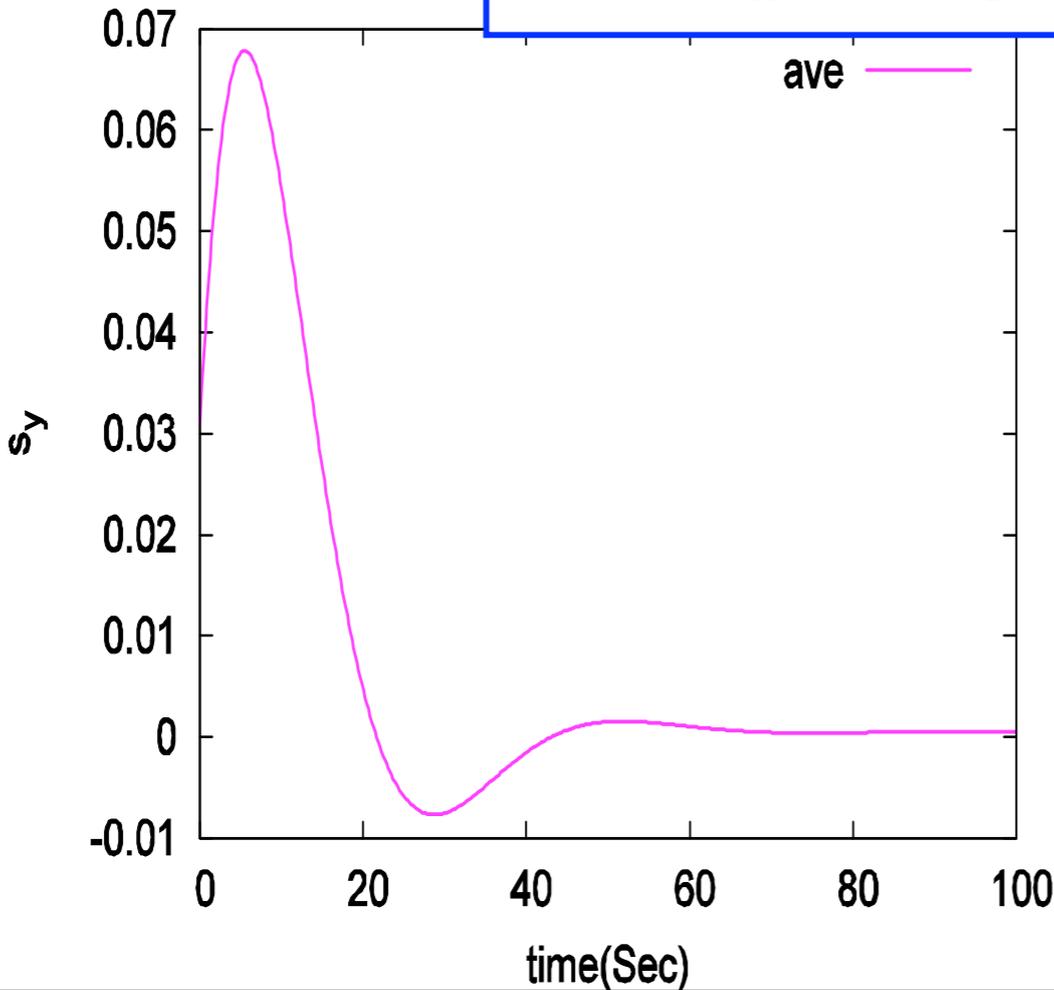
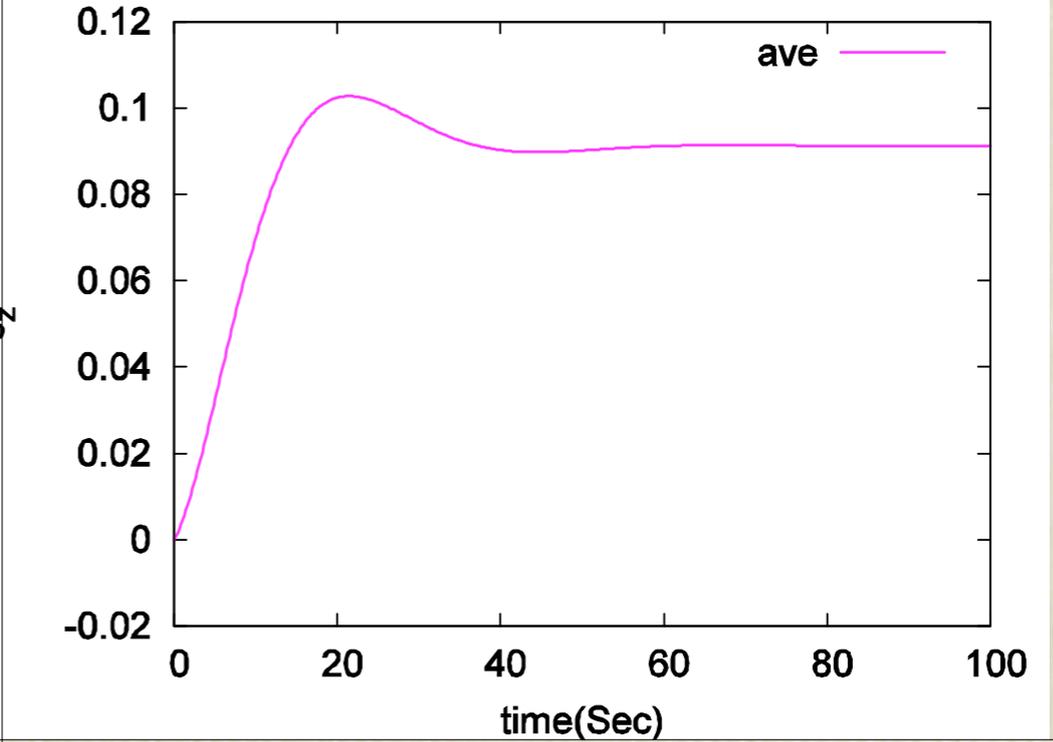
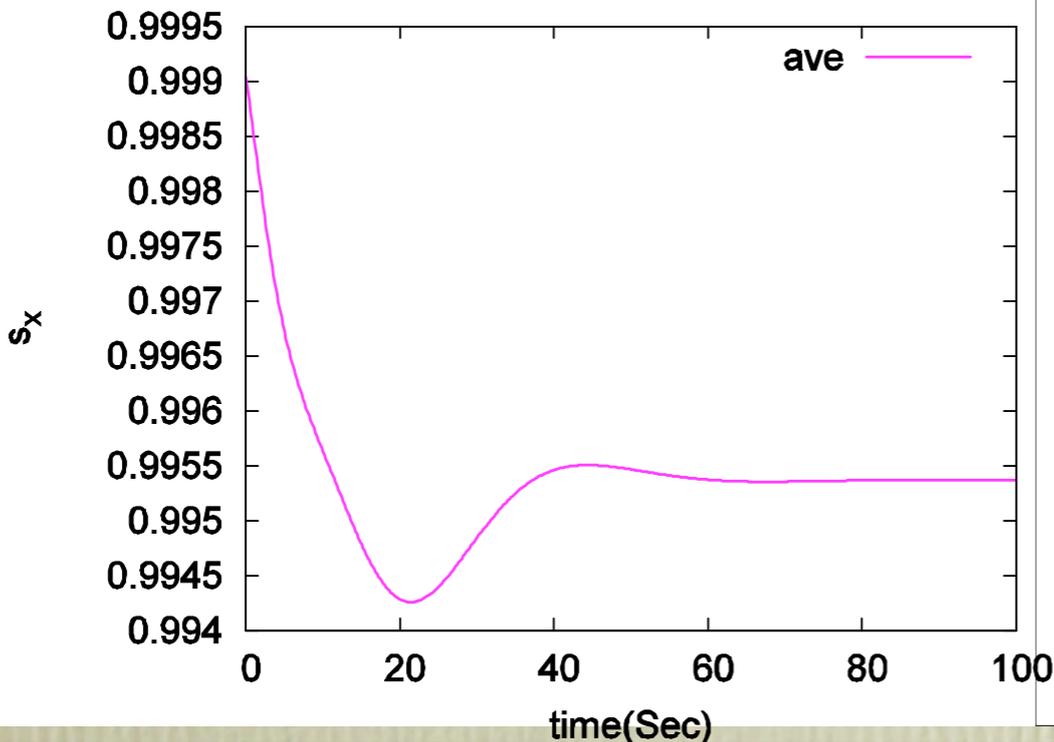


Fig. 8. Response of the system when  $\tau_L$  is rather long and with no UCN loss. The modulation period  $\tau = 0.1$  s. The interesting feature is that  $\omega_z \neq 0$ , which implies that there is an error in the correction signal, after the system has reached equilibrium.

# Similar study



**$w_z$  becomes stable after some period of time.**



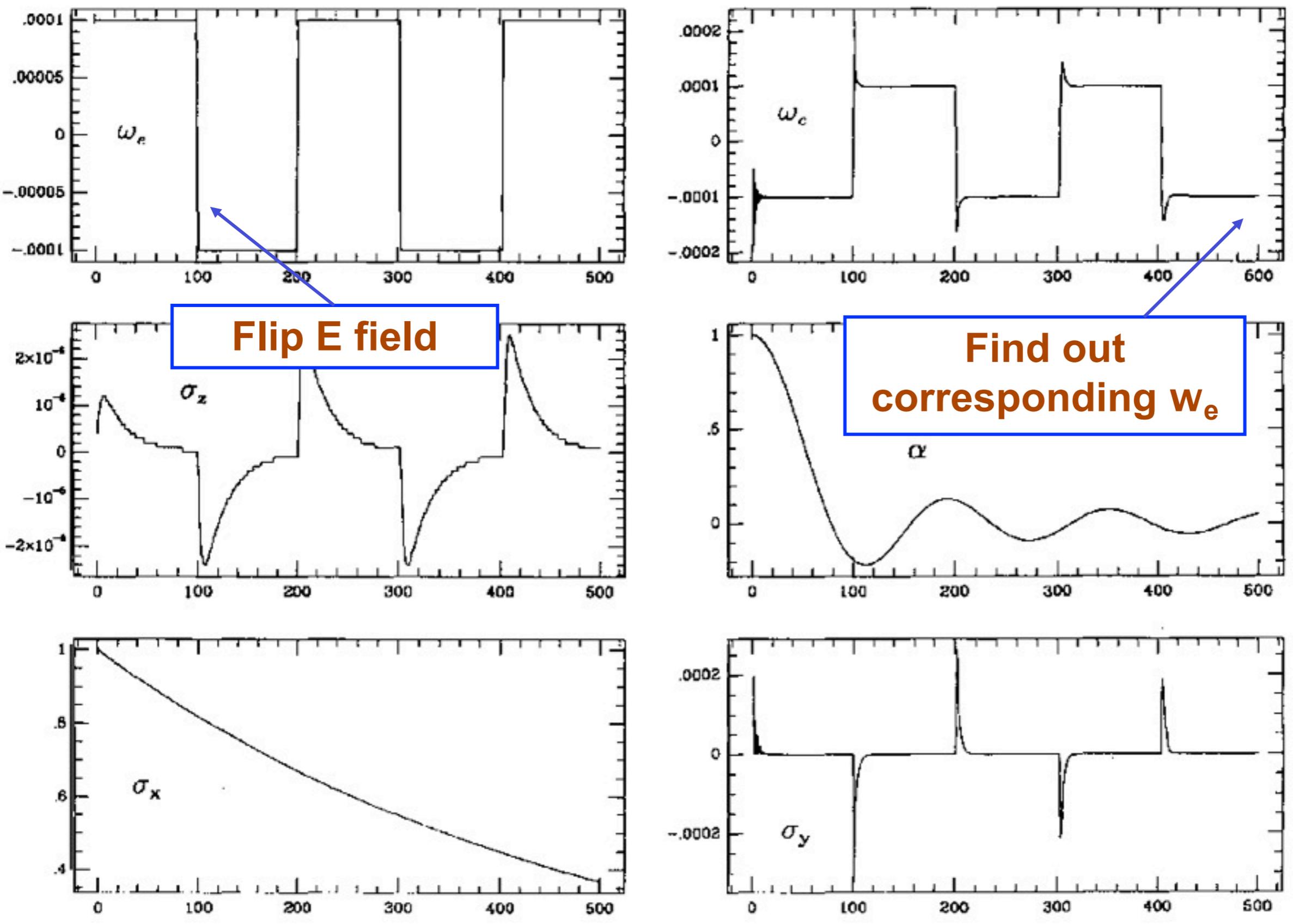
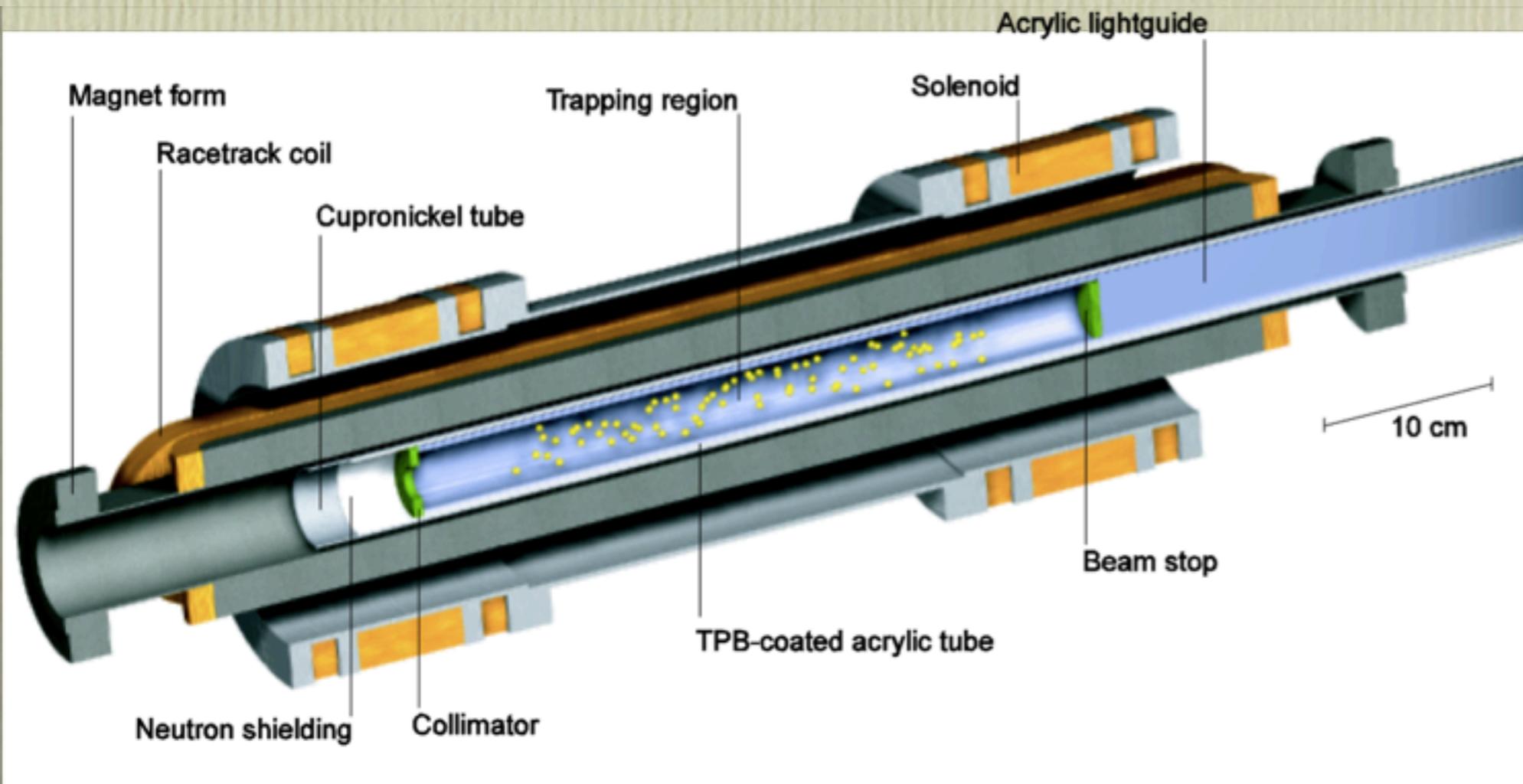


Fig. 10. Simulation including spin-dependent losses with  $\omega_s = +1 \times 10^{-4}$ , reversed every 50 s. The loop is initially underdamped but becomes overdamped due to the gain reduction from neutron losses. The  $\sin \pi/\alpha$  reduction factor is shown to indicate the loss of sensitivity expected when feedback is not used; such a reduction is absent from the correction signal  $\omega_c$ . Also, the component of  $\sigma_z$  due to the finite loop response time decays faster than  $\sigma_x$ ; this is due to spin-dependent losses.

# UCN Production in superfluid $^4\text{He}$

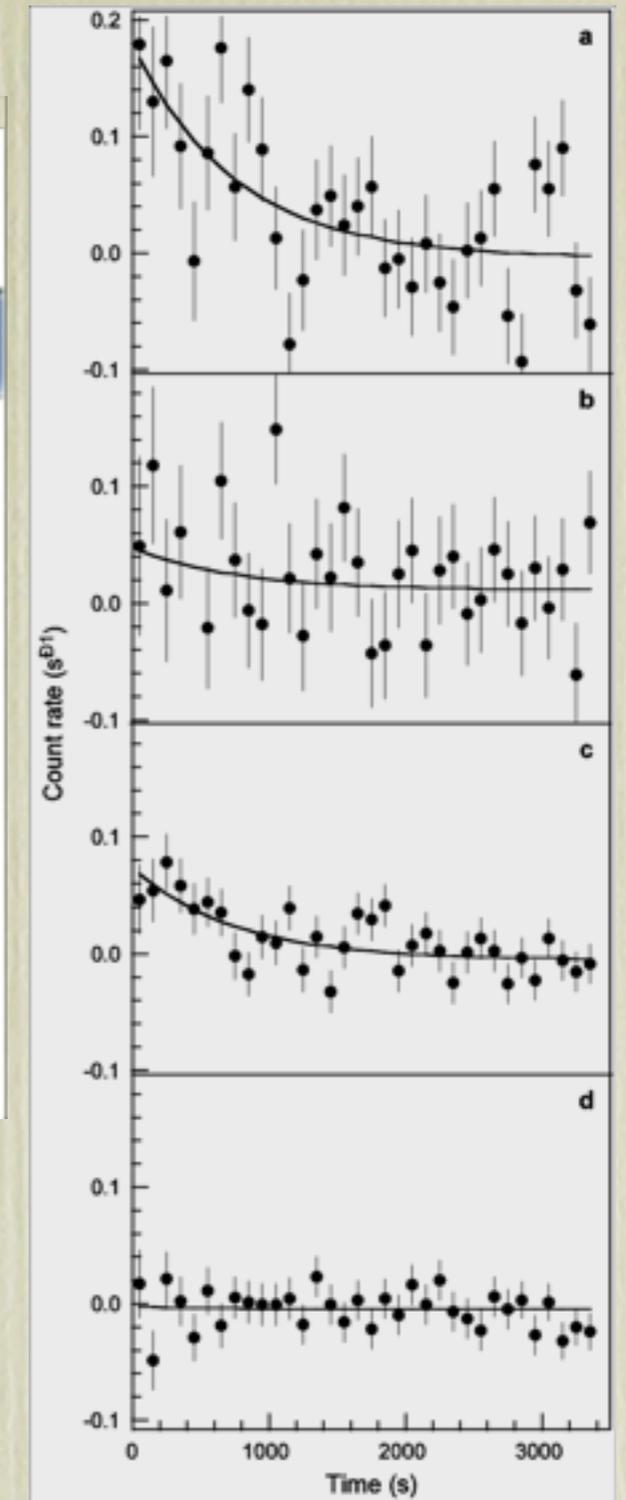
## Magnetic Trapping of UCN at NIST (Nature 403 (2000) 62)



$560 \pm 160$  UCNs trapped per cycle (observed)

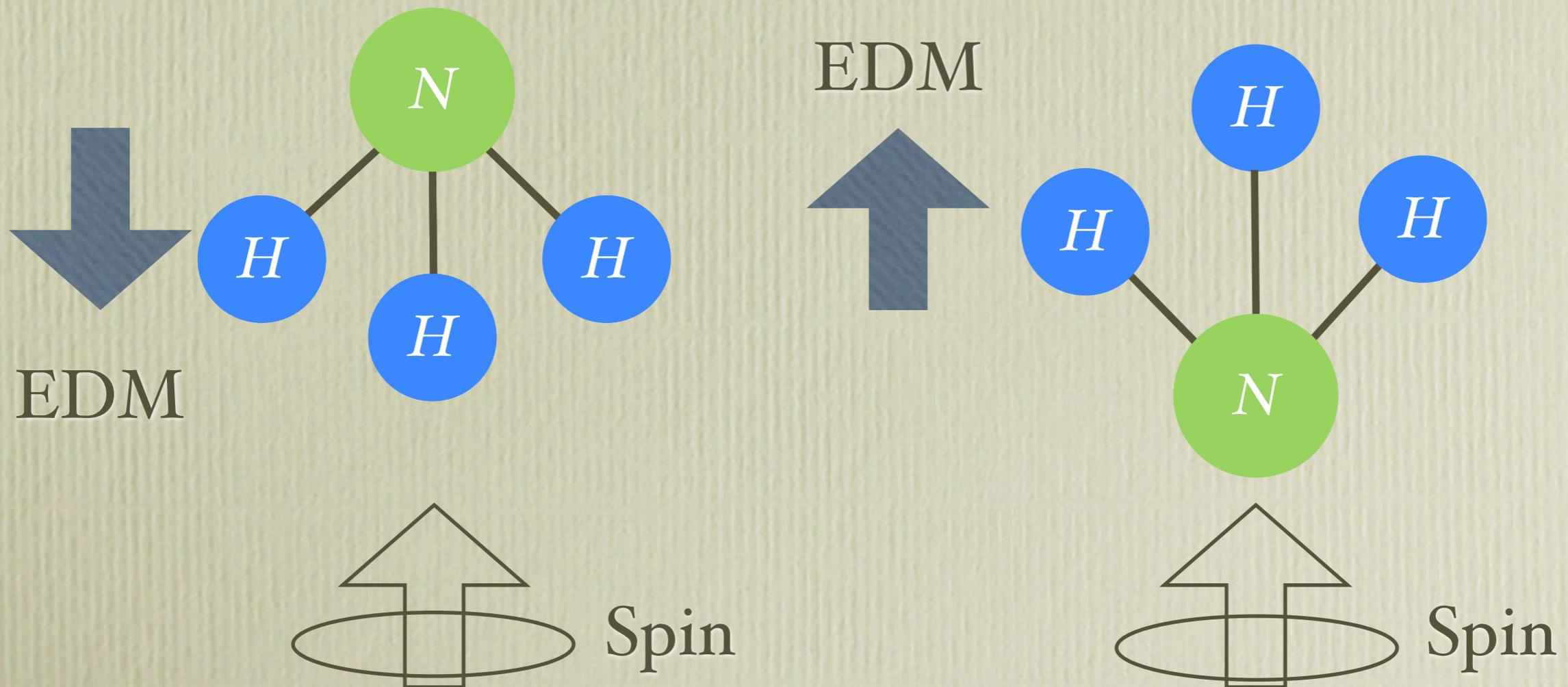
$480 \pm 100$  UCNs trapped per cycle (predicted)

The experiment helps to approve the neutron EDM proposal.



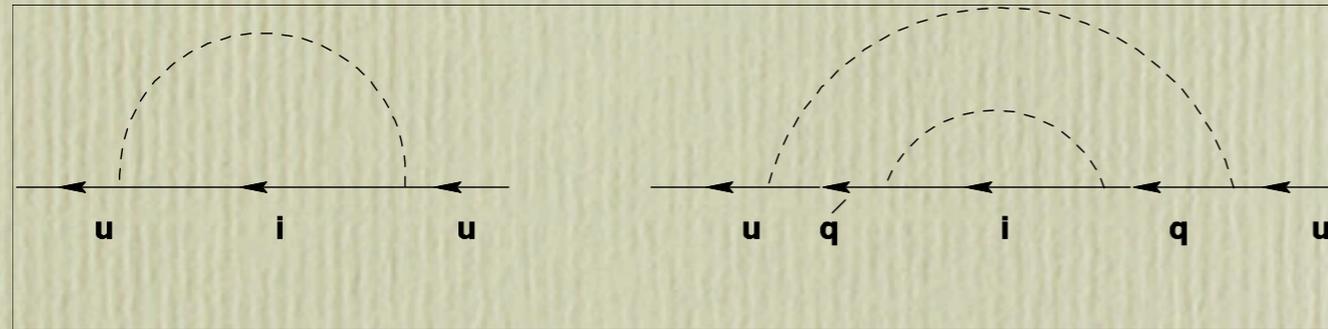
# Why permanent EDMs exist without violating P and T?

- Consider a diatomic polar molecule. The only possible orientation of the EDM is along the molecular axis, but the rotation (spin) is directed perpendicular to the axis.
- For polyatomic molecules (like  $\text{NH}_3$ ), the  $+k$  and  $-k$  ( $k$  is the spin projection) are degenerate states with opposite sign of EDM. The superposition of these two states would give zero EDM.



# Electroweak Process

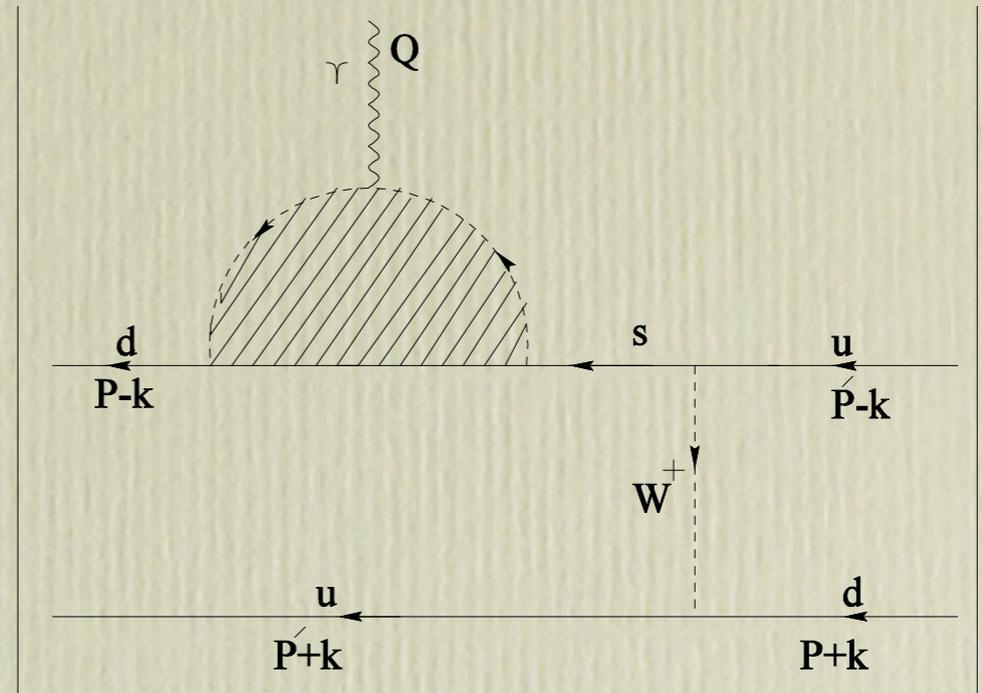
a) Contributions from single quark's EDM:



$$d_n \approx \frac{1}{3} d_u - \frac{4}{3} d_d$$

One and two-loop contributions are zero. Three-loop contribution is  $\sim 10^{-34} e \cdot cm$

b) Contributions from diquark interactions:



$$d_n = \frac{38}{9\pi^3} (G_F m_N^2)^2 \frac{m_t^2}{m_s^2} \frac{m_N^2}{m_W^2} \frac{\Lambda}{m_N^4} \frac{e}{m_N} (\text{Im} V)$$

$$\text{Im} V = c_1 s_1^2 c_2 s_2 c_3 s_3 \sin(\delta)$$

$$d_n \sim 10^{-32} e \cdot cm$$

(hep-ph/0008248)

# Strong Interaction

- $\Theta$  term in the QCD Lagrangian :

$$L_{\theta} = \frac{\theta g_s^2}{32\pi^2} G_{\mu\nu} \tilde{G}^{\mu\nu}$$

$$d_n = \frac{e}{m_p} \frac{g_{\pi NN} \bar{g}_{\pi NN}}{4\pi^2} \ln \frac{m_{\rho}}{m_{\pi}}$$

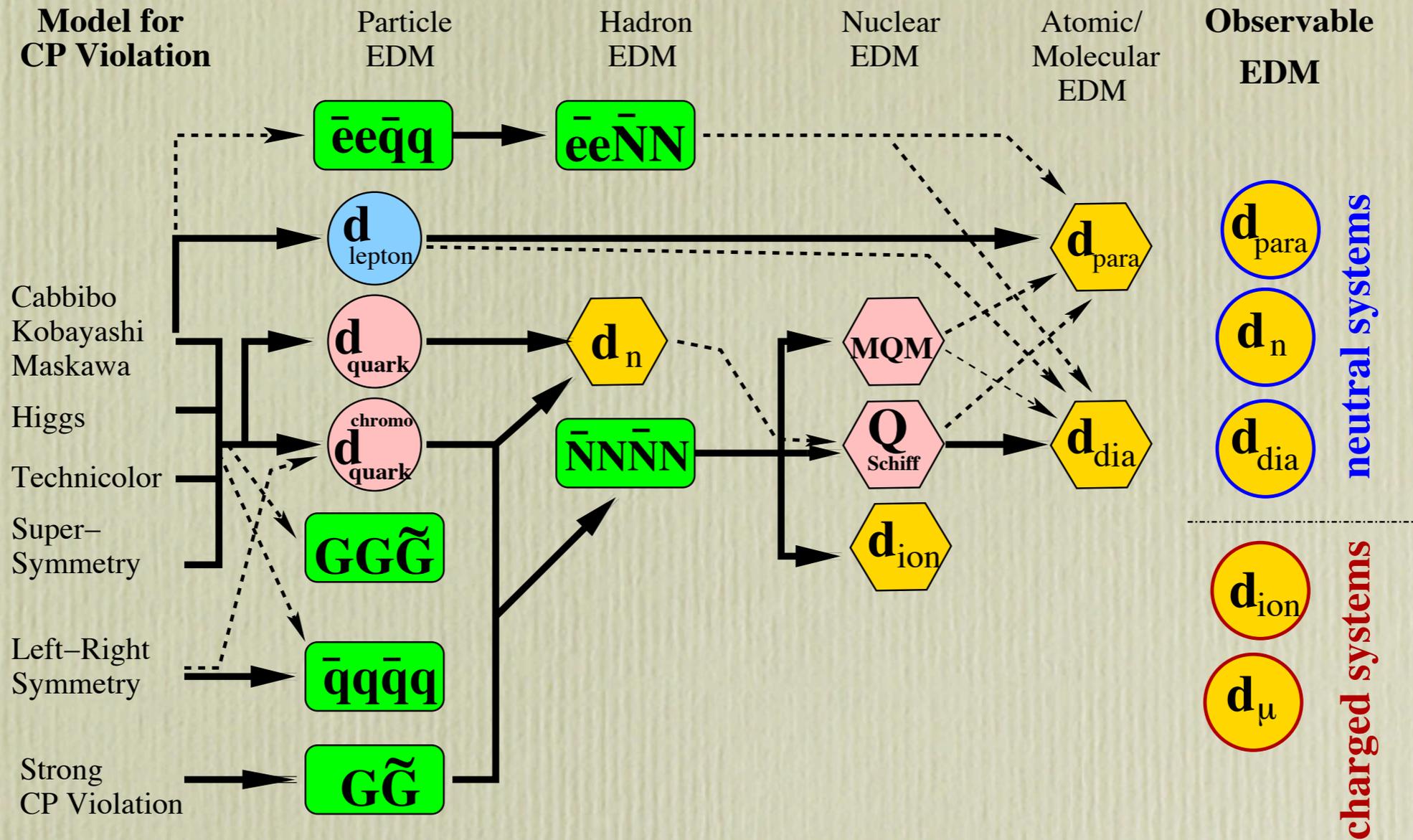
- $\Theta$  term's contribution to the neutron EDM :

$$\bar{g}_{\pi NN} = -\theta \frac{m_u m_d}{m_u + m_d} \frac{\sqrt{2}}{f_{\pi}} \frac{M_{\Xi} - M_{\Sigma}}{m_s}$$

$$d_n < 10^{-25} \text{ e}\cdot\text{cm} \rightarrow |\theta| < 3 \times 10^{-10}$$

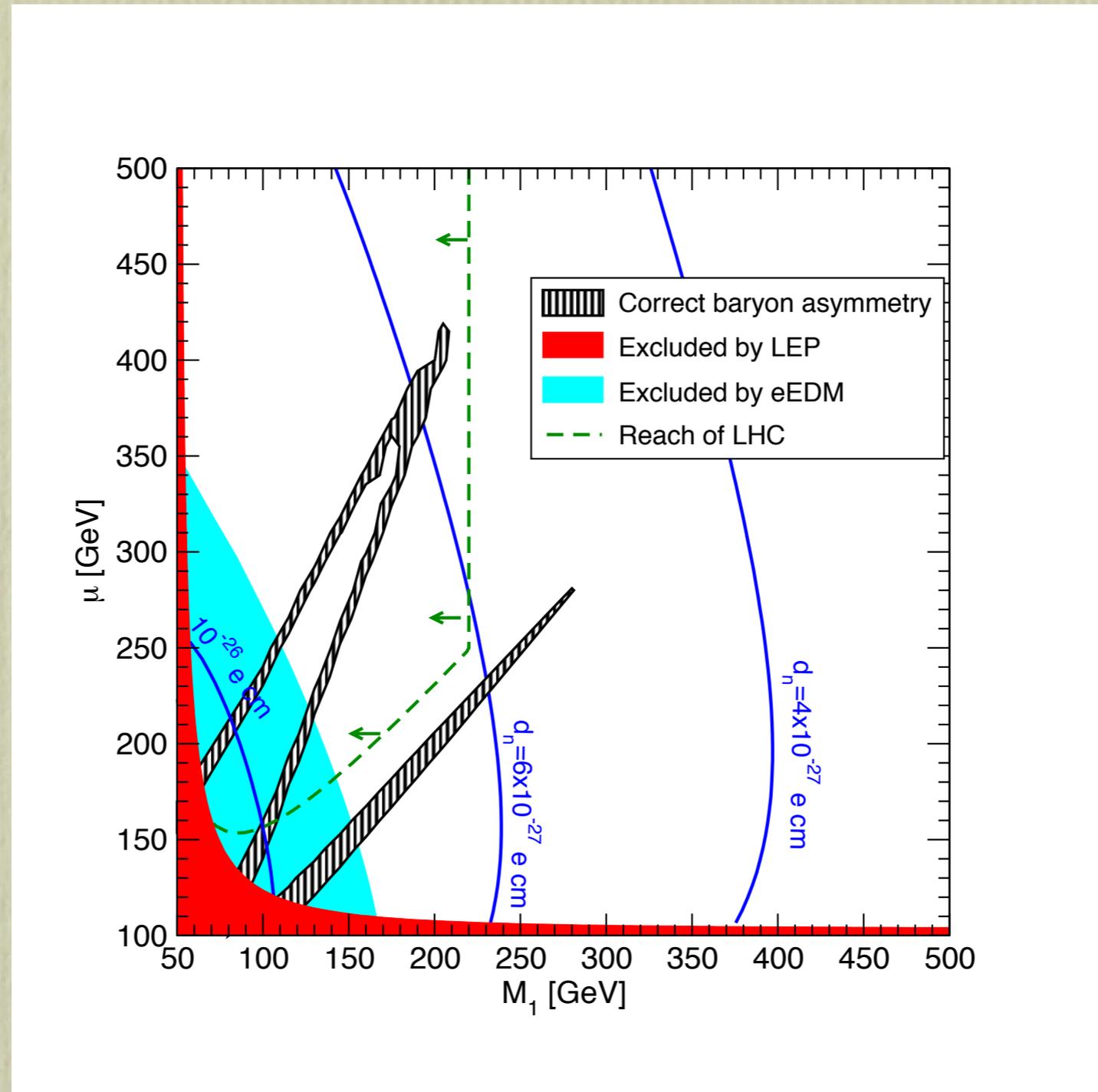
- Spontaneously broken Pecci-Quinn symmetry? No evidence of a pseudoscalar axion!

# Physics beyond SM



- There are many new CP sources generating observable EDMs.
- Observed EDMs are a combination of different CP-violating sources.
- To explain the strong CP violation or the new CP sources, it is needed to check the relation between different systems.

# One example of minimum supersymmetry model

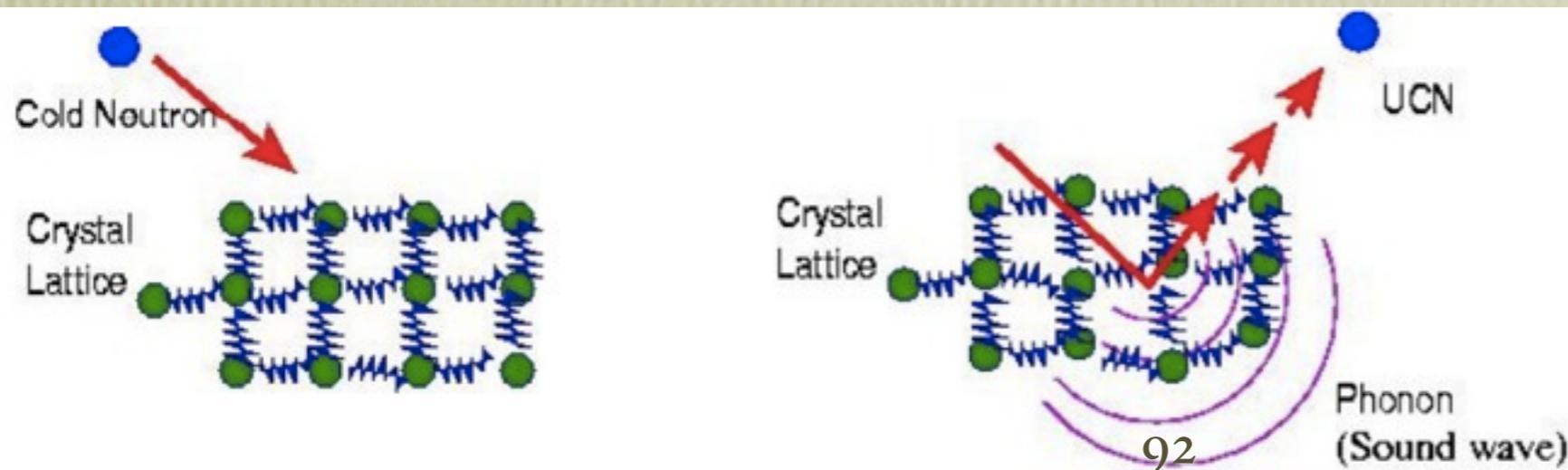
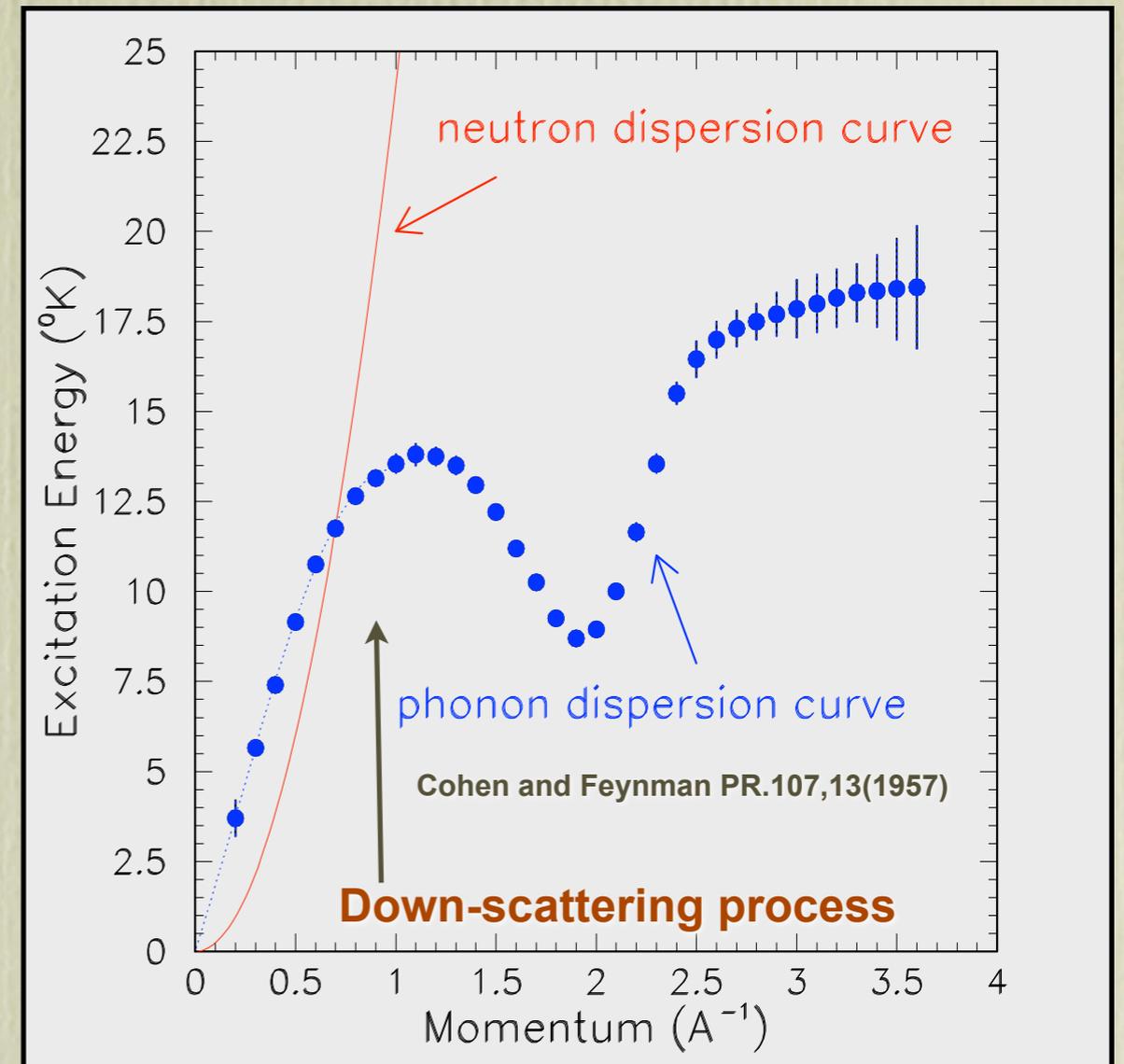


- LHC can only test one branch of parameter phase space of MSSM for the correct baryon asymmetry.
- Neutron EDM can be applied to exam the other region of the phase space.

# Superthermal Method--UCN production in superfluid $^4\text{He}$

- UCN was extracted from the **low-energy tail** of the Maxwell-Boltzmann distribution of cold neutrons ( $\sim 5 \text{ UCN/cm}^3$ ).
- A new method suggested by Golub and Pendlebury. Cold neutron with momentum of  $0.7 \text{ \AA}^{-1}$  ( $10^{-3} \text{ eV}$ ) can excite a phonon in  $^4\text{He}$  and become an UCN via **down-scattering process**.

**=>100 times larger UCN density than conventional UCN sources**

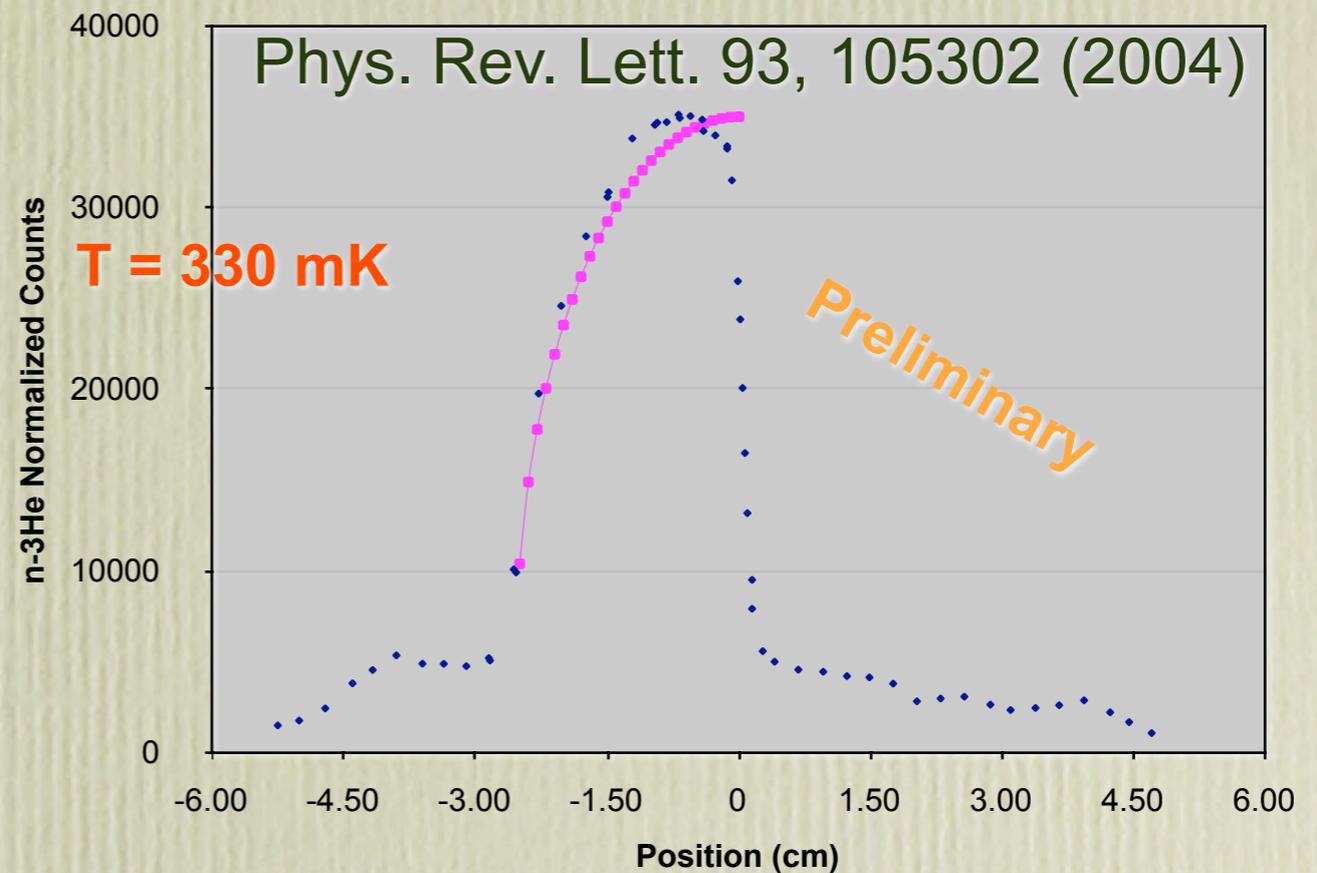
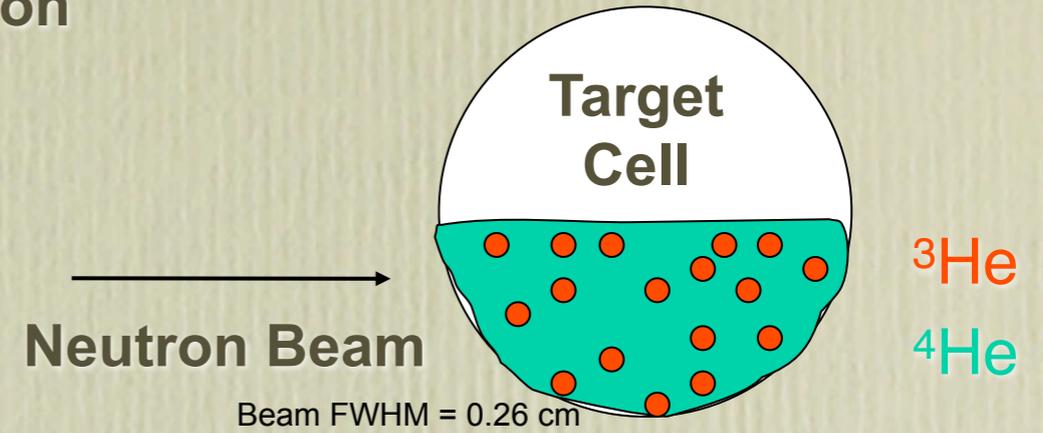


# $^3\text{He}$ Distributions in Superfluid $^4\text{He}$

Dilution Refrigerator at  
LANSCCE Flight Path 11a



Position



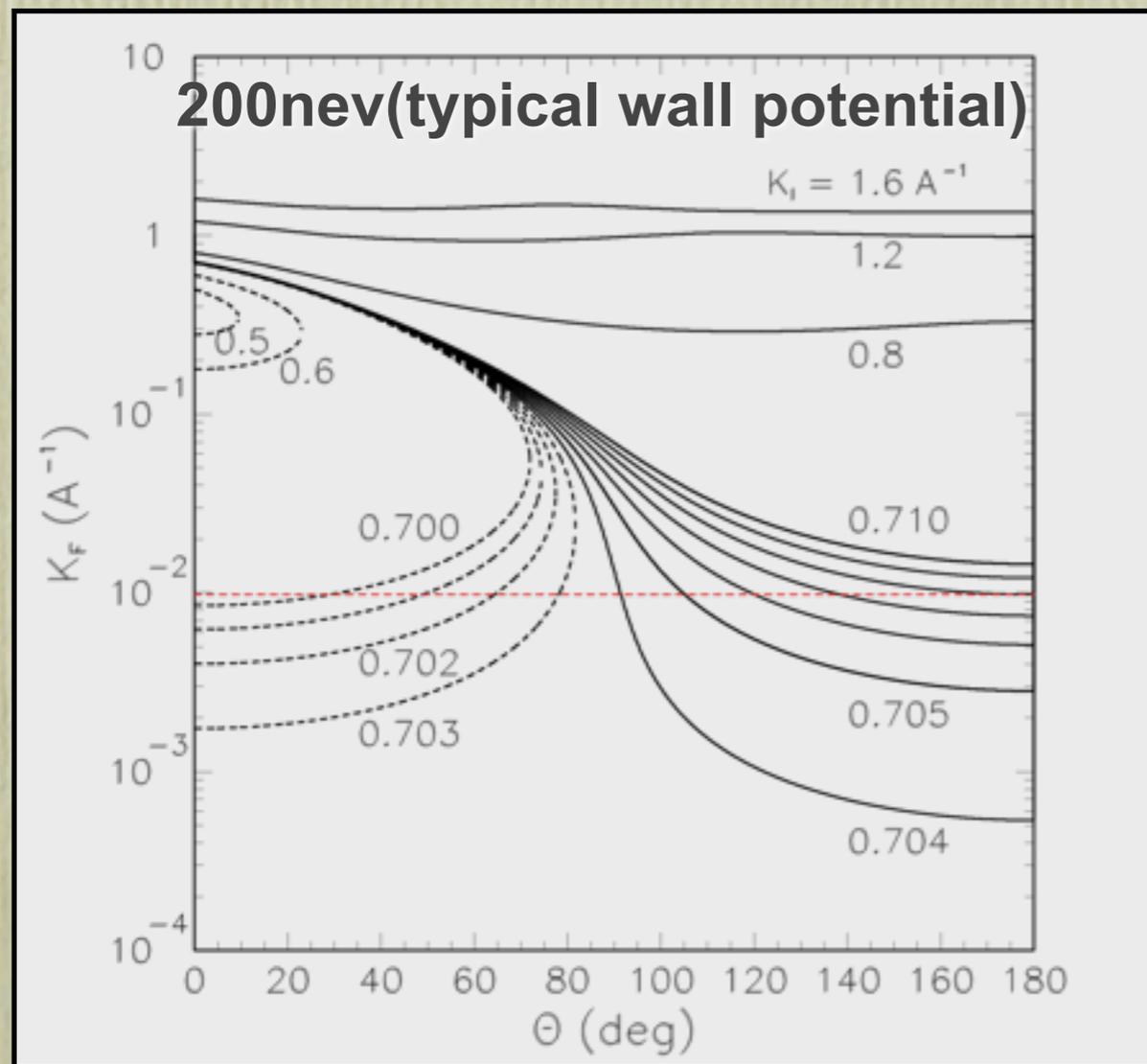
- The experiment shows neutrons distribute uniformly in the superfluid  $^4\text{He}$ . The result confirms the availability of  $^3\text{He}$  as a comagnetometer.

# Production of UCN in superfluid $^4\text{He}$

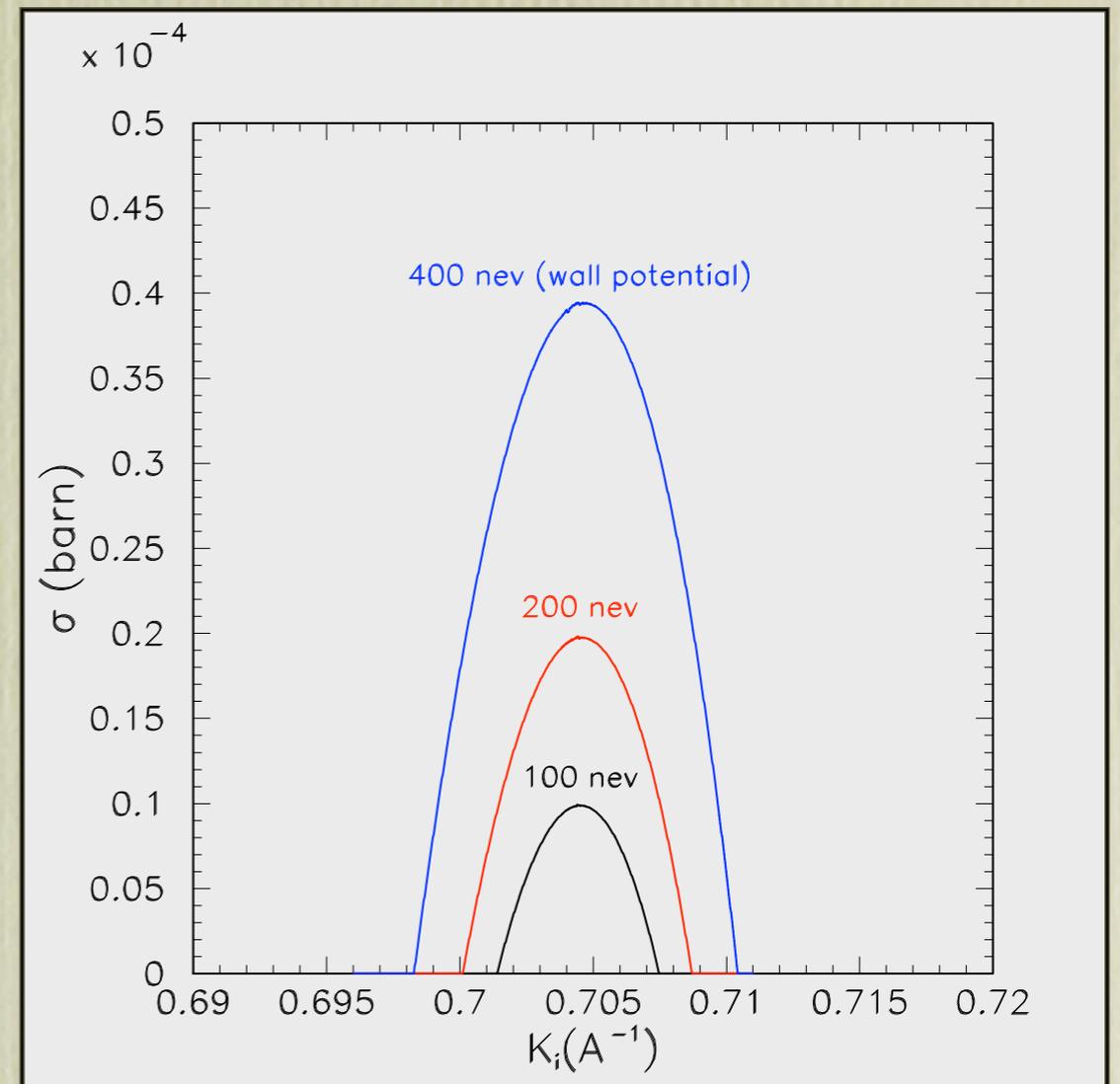
$$\vec{Q} = \vec{k}_i - \vec{k}_f,$$

$E(Q)$  is the phonon dispersion relation

$$\frac{\hbar^2 k_i^2}{2m} = \frac{\hbar^2 k_f^2}{2m} + E(Q),$$



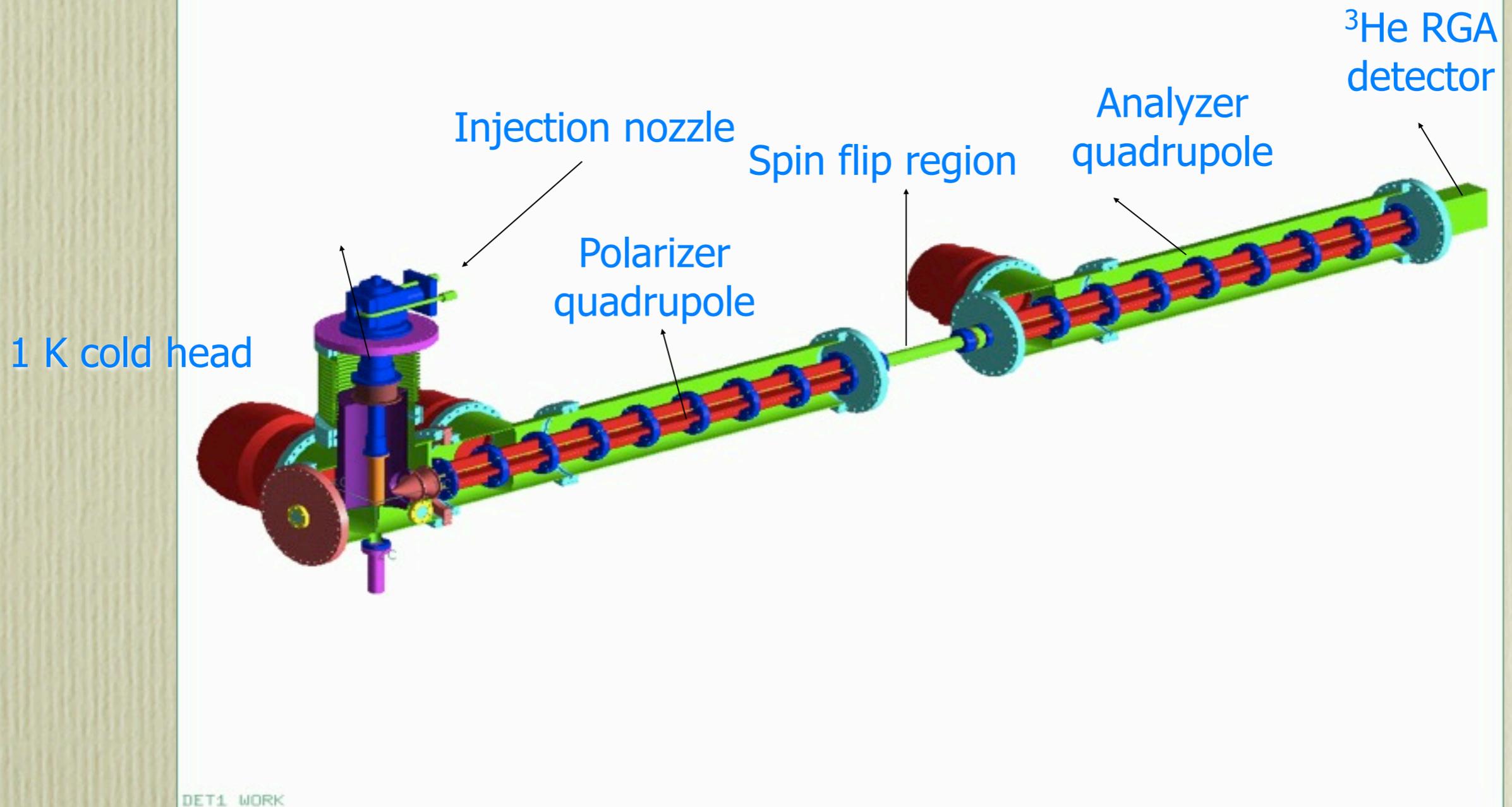
$\theta$  is neutron's scattering angle



For 1 meV neutron beam,  $\sigma(\text{UCN})/\sigma(\text{tot}) \sim 10^{-3}$  for 200 neV wall potential

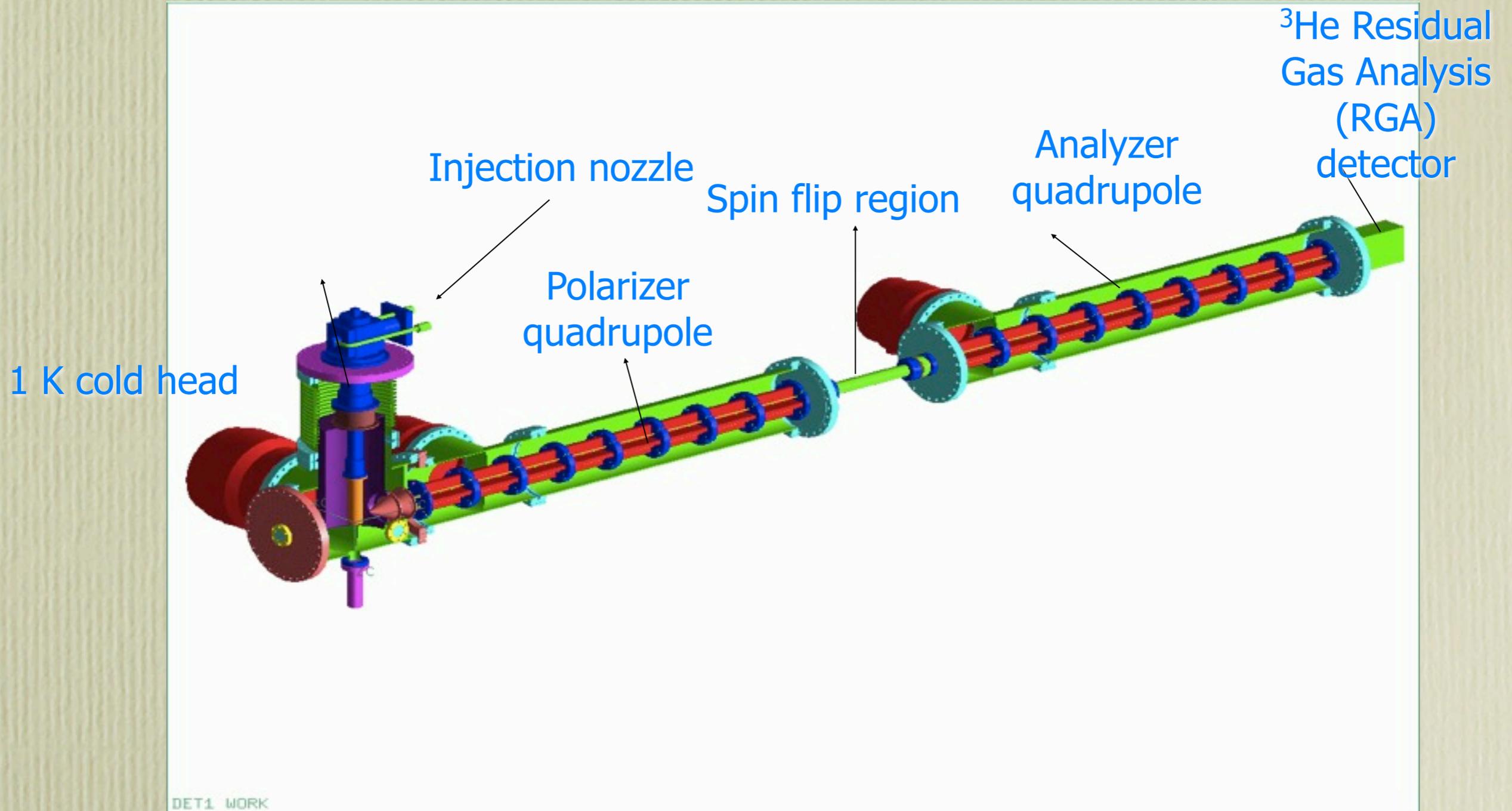
Mono-energetic cold neutron beam with  $\Delta K_i/K_i \sim 2\%$

# Polarized $^3\text{He}$ Atomic Beam Source

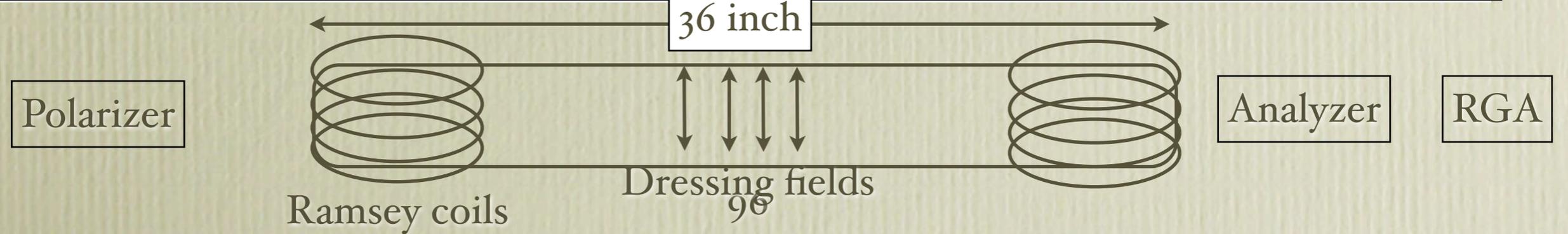


- Produce polarized  $^3\text{He}$  with 99.5% polarization at a flux of  $2 \times 10^{14}/\text{sec}$  and a mean velocity of 100 m/sec

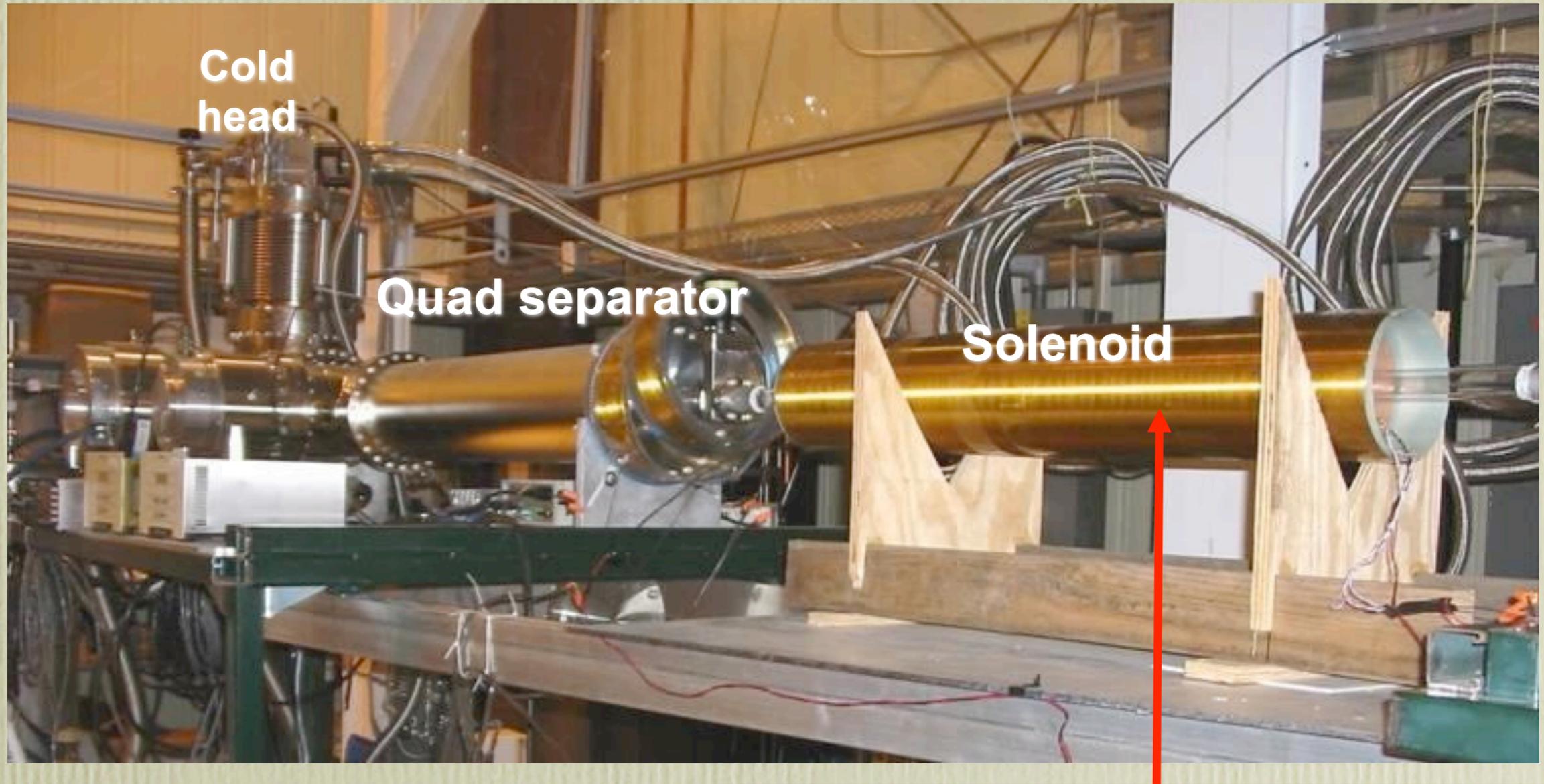
# Los Alamos Polarized $^3\text{He}$ Source



## • $^3\text{He}$ Spin dressing experiment

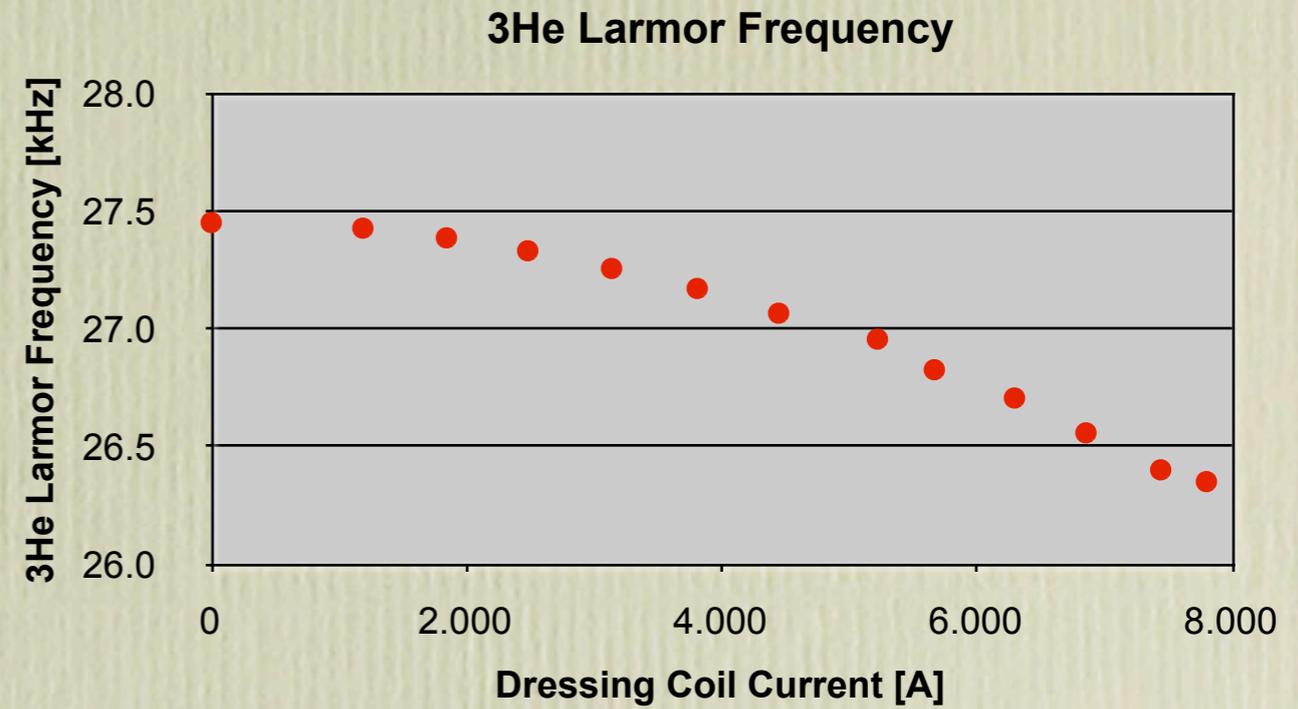
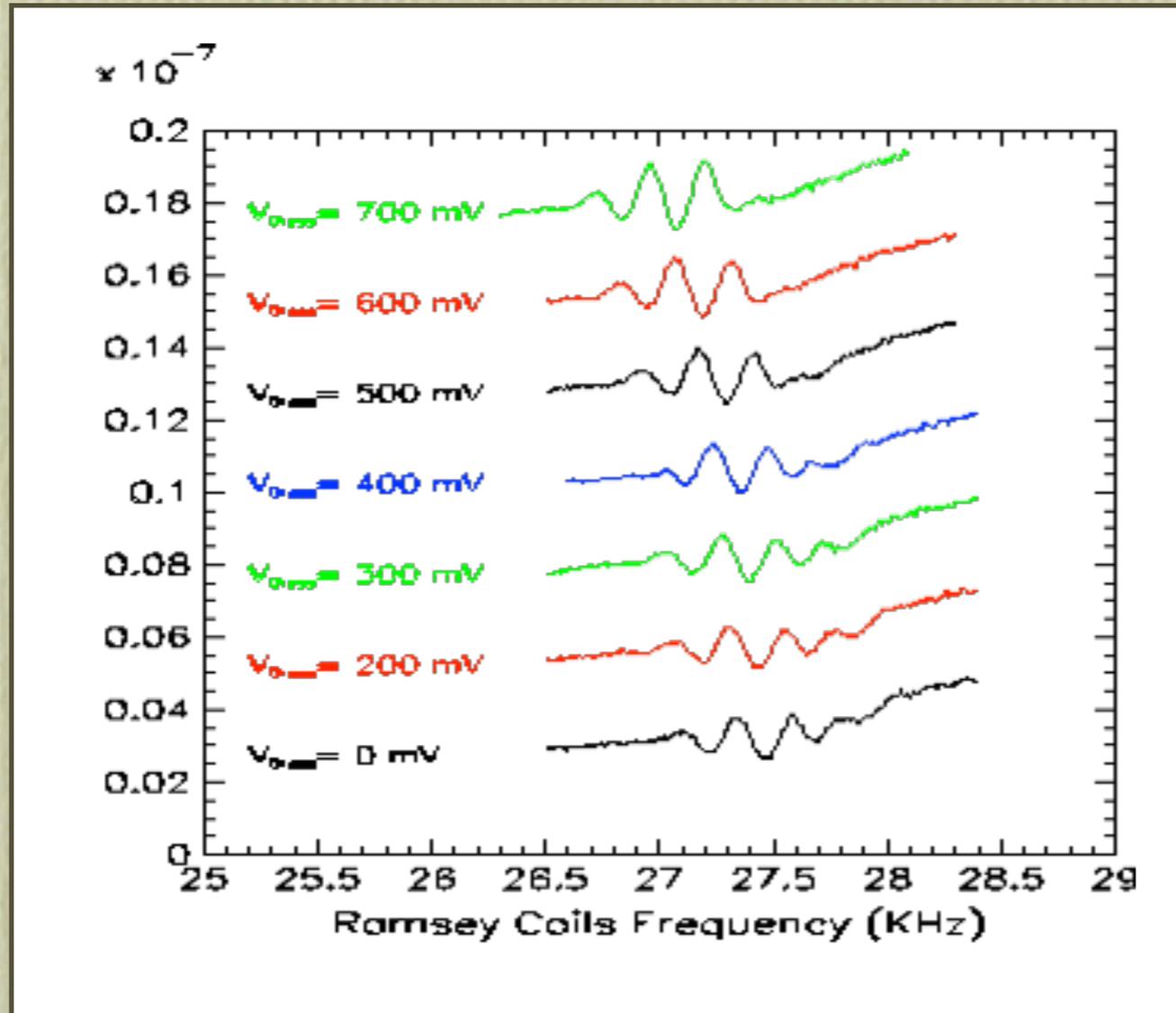


# Mapping the dressing field



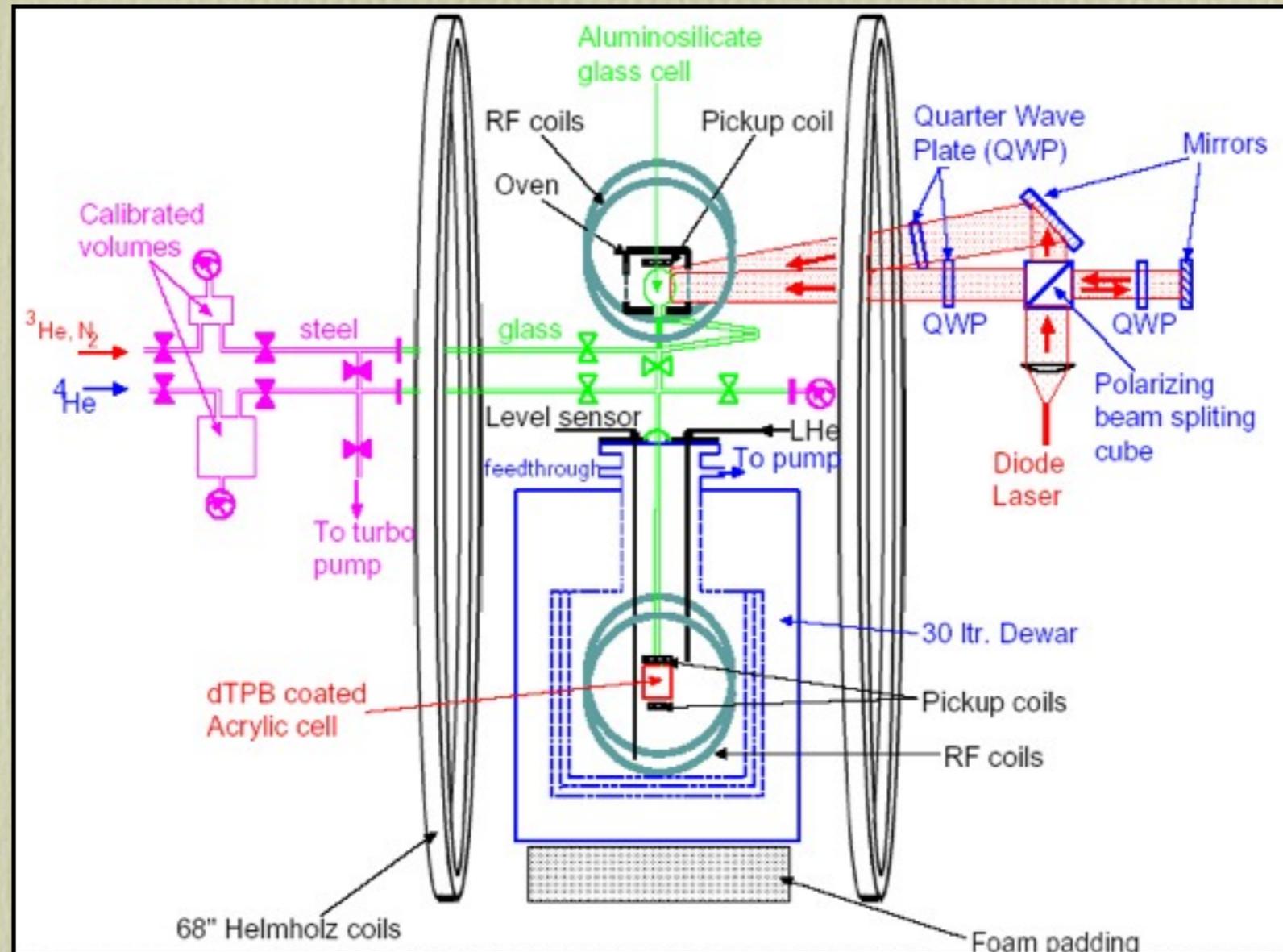
Spin-flip coils and dressing coils used inside the solenoid.

# Experiment result



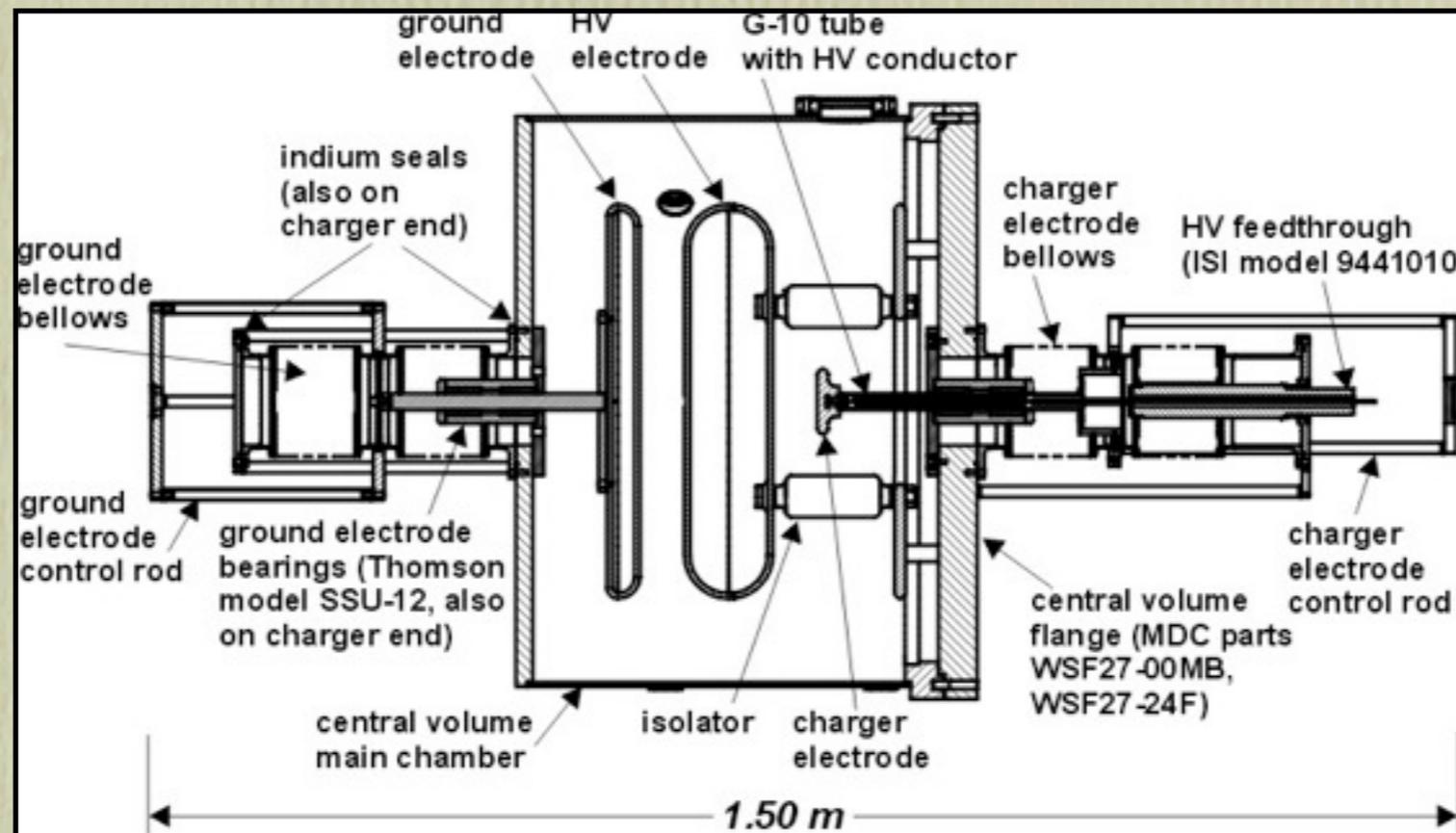
Esler, Peng, Lamoreaux, et al. Nucl-ex/0703029 (2007)

# $^3\text{He}$ relaxation test



- $T_1 > 3000$  seconds in 1.9K superfluid  $^4\text{He}$
- Acrylic cell coated with dTPB
- H. Gao, R. McKeown, et al, arXiv:Physics/0603176
- Test has also been done at 600 mK at UIUC

# High voltage test



- Goal is 50 kV/cm
- 200 liter LHe. Voltage is amplified with a variable capacitor
- 90 kV/cm is reached for normal state helium. 30 kV/cm is reached below the  $\lambda$ -point
- J. Long et al., arXiv:physics/0603231

# Heat flash

- The helium extracted from gas contains  ${}^3\text{He}/{}^4\text{He} = 10^{-7}$ .
- The heat flash technique can purify the helium to  ${}^3\text{He}/{}^4\text{He} = 10^{-12}$ .
- ${}^3\text{He}$  atoms in He II form part of the normal fluid component and tend to move to colder end of the apparatus.
- The normal fluid component, flowing away from the heater, will tend to carry with any  ${}^3\text{He}$  atoms and to prevent others from entering.
- The isotopically pure superfluid component can be drawn off in the opposite direction.

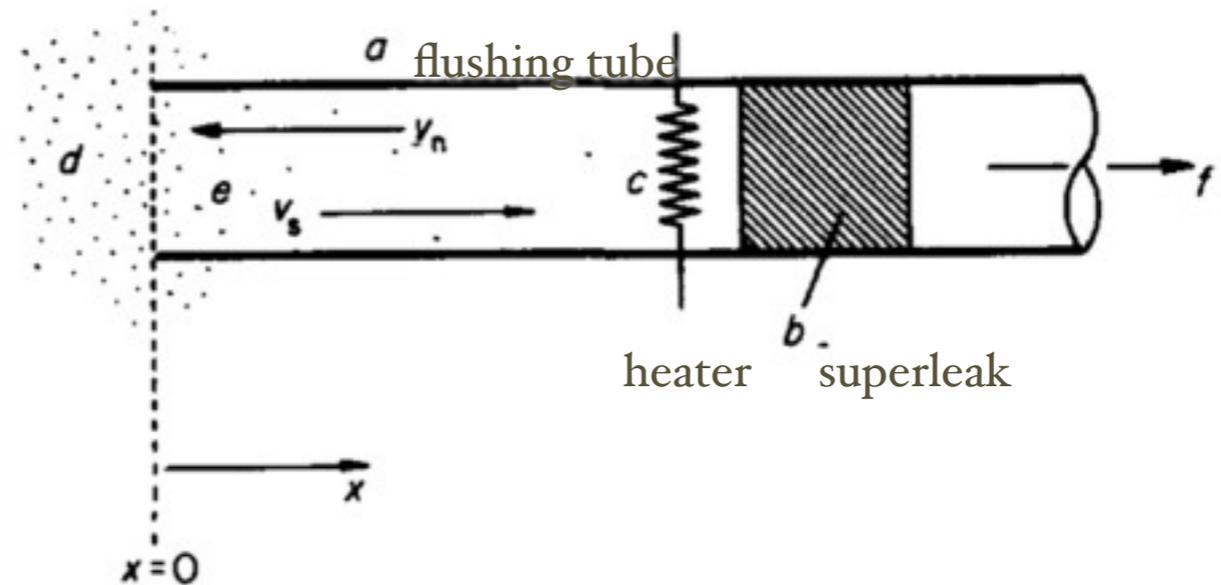
## Continuous flow apparatus for preparing isotopically pure ${}^4\text{He}$

P.C. Hendry and P.V.E. McClintock

Department of Physics, University of Lancaster, Lancaster LA1 4YB, UK

Received 20 November 1986

A  ${}^4\text{He}$  isotopic purification cryostat has been developed, capable of sustained operation in continuous flow. Starting from a feedstock of helium of the natural isotopic ratio,  ${}^3\text{He}/{}^4\text{He} = x_3 \approx 10^{-7}$ , it yields a purified product for which  $x_3 < 5 \times 10^{-13}$  at a production rate of  $3.3 \text{ STP m}^3 \text{ h}^{-1}$ . The isotopically purified  ${}^4\text{He}$  is being used for a variety of applications, including quantum evaporation experiments, studies of ion motion at the He II/vacuum interface, downscattering and containment of ultra-cold neutrons, and investigations of the breakdown of superfluidity in  ${}^4\text{He}$ .

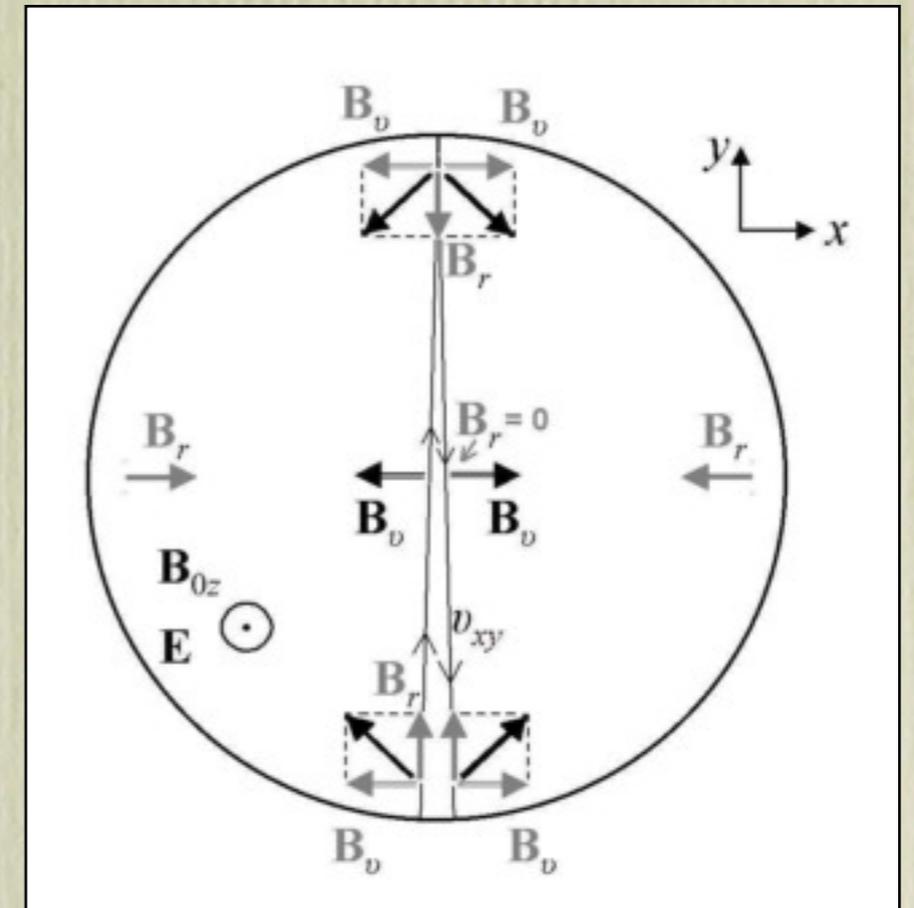


# Geometric phase

- The false EDM can arise from geometric phases.
- The effect between  $v \times E$  and a vertical gradient in the magnetic field.

- Gives a radial field 
$$B_r = -\frac{r}{2} \cdot \frac{\partial B}{\partial z}$$

- The radial field as well as to the sideways  $v \times E$  component, yielding a diagonal resultant.
- The net effect that the additional effective field continues to rotate in the same direction.
- The shift in frequency is proportional to  $E$ , mimicking an EDM signal.



# Neutron EDM collaboration

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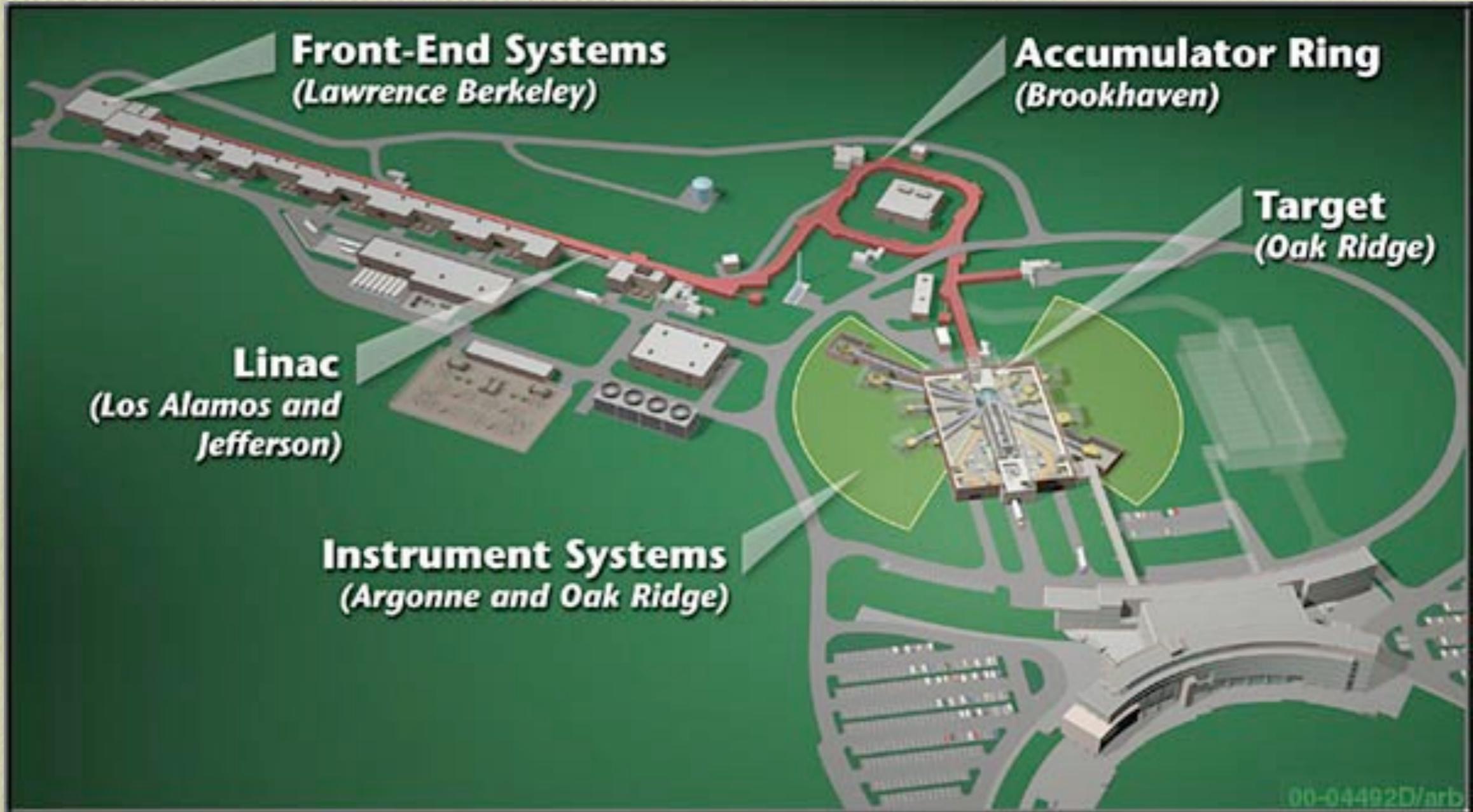
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**Engineers**

# 1.4 MW Spallation Source (1 GeV proton, 1.4mA)



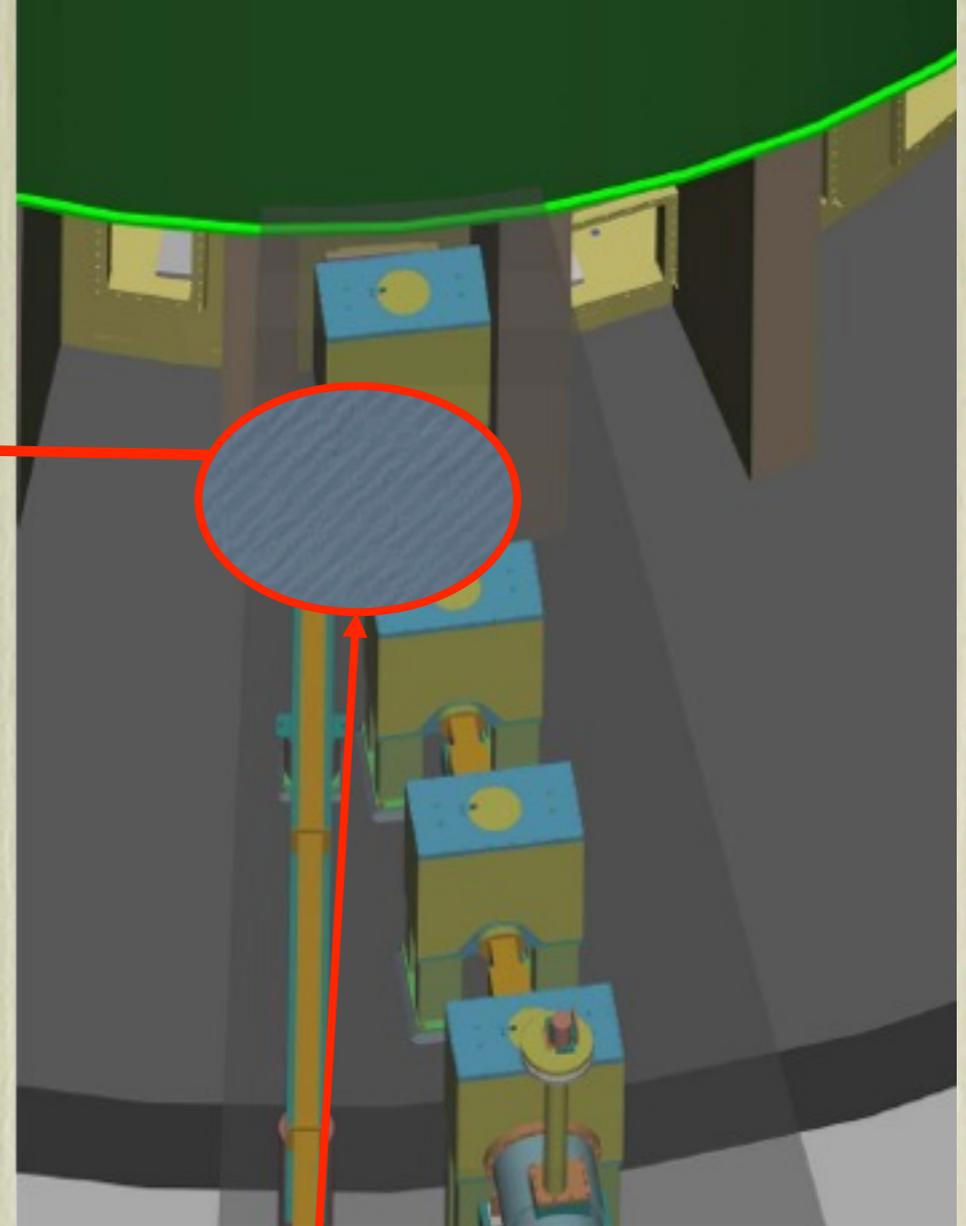
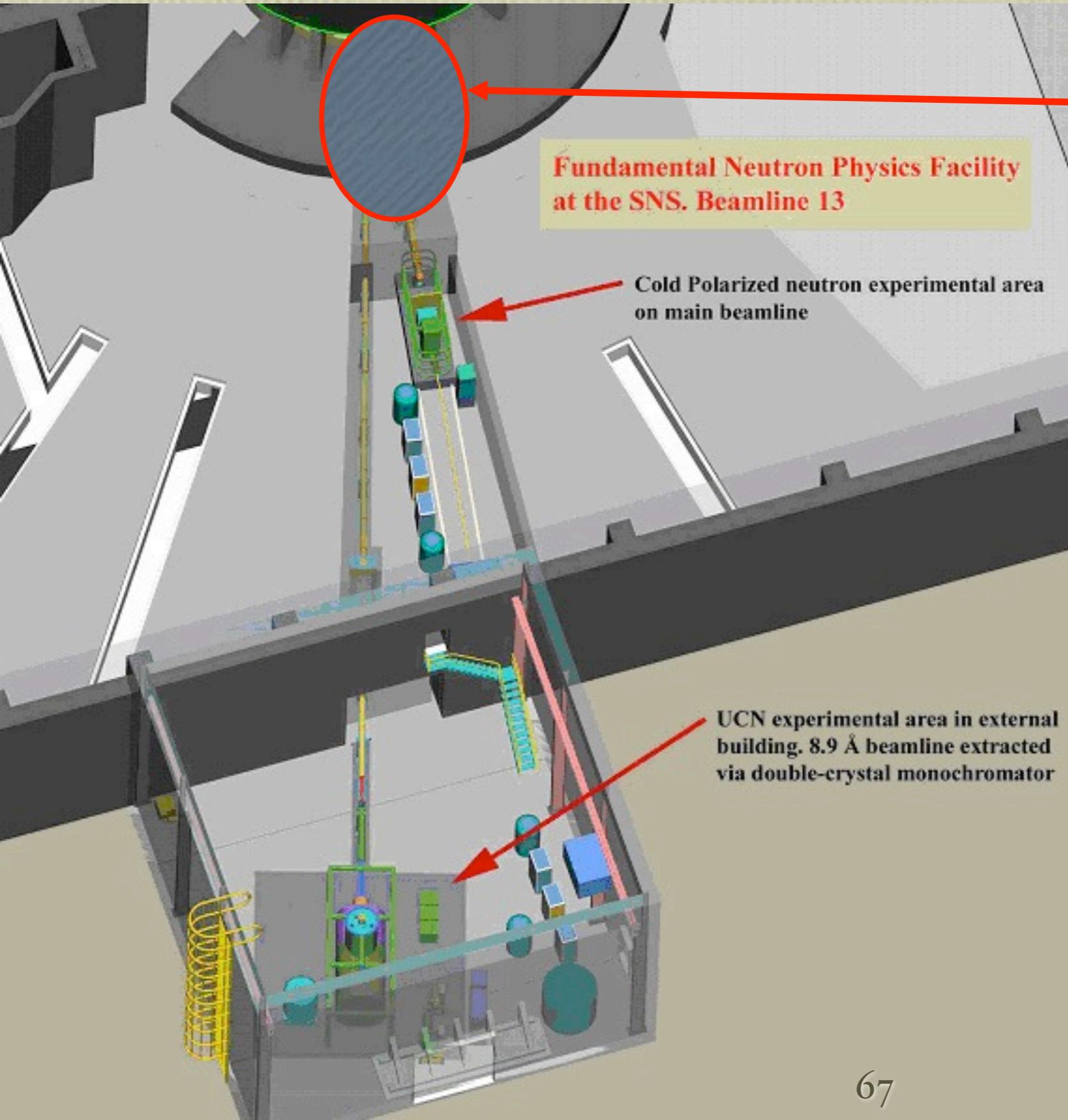
*p beam*

FNPB-Fundamental  
Neutron Physics Beamline

**FNPB  
construction  
underway**

**Cold beam  
available  
~2007**

**UCN line  
via LHe  
~2009**



Double  
monochrometer

Selects  $8.9 \text{ \AA}$   
neutrons  
for UCN via LHe

# History of neutron EDM experimetns

Ex. Type	$\langle v \rangle$ (m/cm)	E (kV/cm)	B (Gauss)	Coh. Time (s)	EDM (e.cm)	year
Scattering	2200	$10^{25}$	--	$10^{-20}$	$< 3 \times 10^{-18}$	1950
Beam Mag. Res.	2050	71.6	150	0.00077	$< 4 \times 10^{-20}$	1957
Beam Mag. Res.	60	140	9	0.014	$< 7 \times 10^{-22}$	1967
Bragg Reflection	2200	$10^9$	--	$10^{-7}$	$< 8 \times 10^{-22}$	1967
Beam Mag. Res.	130	140	9	0.00625	$< 3 \times 10^{-22}$	1968
Beam Mag. Res.	2200	50	1.5	0.0009	$< 1 \times 10^{-21}$	1969
Beam Mag. Res.	115	120	17	0.015	$< 5 \times 10^{-23}$	1969
Beam Mag. Res.	154	120	14	0.012	$< 1 \times 10^{-23}$	1973
Beam Mag. Res.	154	100	17	0.0125	$< 3 \times 10^{-24}$	1977
UCN Mag. Res.	$< 6.9$	25	0.028	5	$< 1.6 \times 10^{-24}$	1980
UCN Mag. Res.	$< 6.9$	20	0.025	5	$< 6 \times 10^{-25}$	1981
UCN Mag. Res.	$< 6.9$	10	0.01	60-80	$< 8 \times 10^{-25}$	1984
UCN Mag. Res.	$< 6.9$	12-15	0.025	50-55	$< 2.6 \times 10^{-25}$	1986
UCN Mag. Res.	$< 6.9$	16	0.01	70	$< 12 \times 10^{-26}$	1990
UCN Mag. Res.	$< 6.9$	12-15	0.018	70-100	$< 9.7 \times 10^{-26}$	1992
UCN Mag. Res.	$< 6.9$	4.5	0.01	120-150	$< 6.3 \times 10^{-26}$	1999

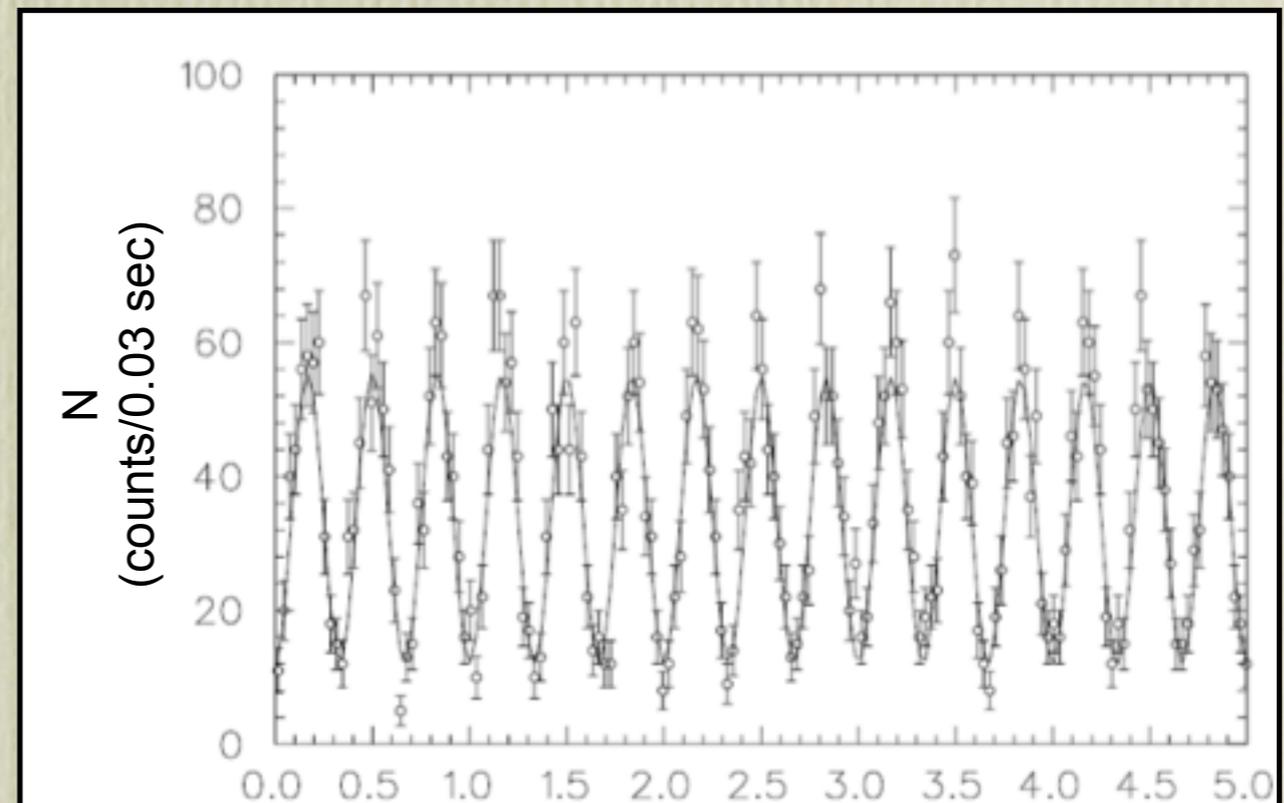
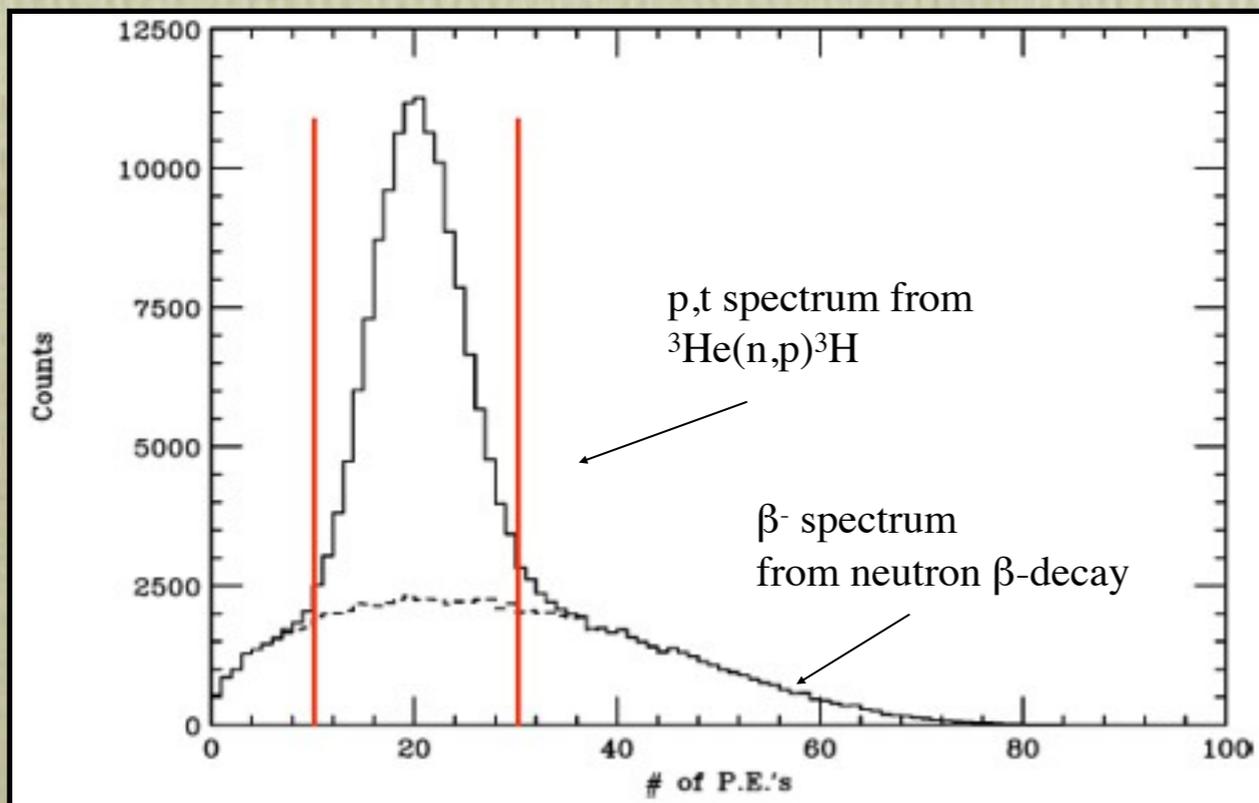
•  $B = 1mG \Rightarrow 3 \text{ Hz}$  neutron precession freq.

•  $d = 10^{-26} \text{ e}\cdot\text{cm}$ ,  $E = 10 \text{ KV/cm} \Rightarrow 10^{-7} \text{ Hz}$  shift in precession freq.

# nEDM statistical sensitivity

- 300 live days over 3 years (due to accelerator/experiment uptime)
- Optimal projected sensitivity (@ 90% CL) :  $d = 7.8 \times 10^{-28} \text{ e cm}$
- Width of neutron capture signal given by number of photoelectrons
- Capture light is partially quenched compared to  $\beta$ -decay electrons
- $\sigma_d$  depends on  $\sigma_f$

$$\sigma_{d_n} = \hbar \frac{1.64 \sigma_f}{4E_0} \sqrt{2}$$



# nEDM systematic uncertainty

- Pseudomagnetic field (Brad Filippone)
  - Due to spin-dependence of n-<sup>3</sup>He scattering length – gives frequency shift as  $\sigma_n \cdot \sigma_3$  varies
  - Gives frequency noise if  $\pi/2$  pulse varies
  - Precision spin flip needed anyway if we want to fix the phase
  - $10^{-3}$  reproducibility with both cells < 5% different is sufficient for  $10^{-28}$  e cm
- Gravitational effects
  - $10^{-29}$  e cm if leakage ~ 1 nA for ~ 10 cm cell
  - Thermal offsets could give larger effects
- Quadratic vxE effect
  - <  $10^{-28}$  e cm if E-field reversal is good to 1%
- Geometric Phase – linear vxE effect
  - From Golub, Swank & Lamoreaux
  - Probably biggest potential systematic issue

# nEDM systematic uncertainty

(Brad Filippone)

- Significantly different effects for neutron vs  $^3\text{He}$ 
  - Neutron has  $\omega_0 \gg \omega_L$  ( $\omega_L$  is cell traversal frequency) and is largely independent of cell geometry.
    - Can use previous analysis of geometric phase
  - $^3\text{He}$  has  $\omega_0 \ll \omega_L$  and is sensitive to cell geometry
    - Depends on diffusion time to walls (geometry & temperature)
    - False EDM in rectangular geometry: Golub, Swank & Lamoreaux  
arXiv:0810.5378
- Effect depends on Magnetic Field gradients ( $B_0$  along x-direction)

# nEDM systematic uncertainty

(Brad Filippone)

<b>Error Source</b>	<b>Systematic</b>	<b>Comments</b>
<b>Linear vxE (geometric phase)</b>	<b><math>&lt; 2 \times 10^{-28}</math></b>	<b>Uniformity of B0 field</b>
<b>Quadratic vxE</b>	<b><math>&lt; 0.5 \times 10^{-28}</math></b>	<b>E-field reversal to &lt;1%</b>
<b>Pseudomagnetic Field Effects</b>	<b><math>&lt; 1 \times 10^{-28}</math></b>	<b>pi/2 pulse, comparing 2 cells</b>
<b>Gravitational offset</b>	<b><math>&lt; 0.1 \times 10^{-28}</math></b>	<b>With 1 nA leakage currents</b>
<b>Leakage currents</b>	<b><math>&lt; 1 \times 10^{-28}</math></b>	<b>&lt; 1 nA</b>
<b>vxE rotational n flow</b>	<b><math>&lt; 1 \times 10^{-28}</math></b>	<b>E-field uniformity &lt; 0.5%</b>
<b>E-field stability</b>	<b><math>&lt; 1 \times 10^{-28}</math></b>	<b><math>\Delta E/E &lt; 0.1\%</math></b>
<b>Miscellaneous</b>	<b><math>&lt; 1 \times 10^{-28}</math></b>	<b>Other vxE, wall losses</b>

# Possible upgrade paths

(Brad Filippone)

Once experiment demonstrates that it's sensitivity is limited by neutron flux (first physics result) ...

- Could “move“ experiment to cold beam at FNPB (or vice versa)
  - Choppers instead of monochromator could increase 8.9 Å flux by ~ 6x ( $d_n < 4 \times 10^{-28}$  e-cm)
- Could “move“ experiment to planned 2<sup>nd</sup> target station at SNS
  - 1 MW, optimized for long wavelength neutrons
  - Could increase 8.9 Å flux by > 20 ( $d_n < 2 \times 10^{-28}$  e-cm)



**CD0 – 1/09**

Also NIST or PULSTAR  
possible

# Active worldwide effort to improve neutron EDM sensitivity

(Brad Filippone)

<b>Exp</b>	<b>UCN source</b>	<b>cell</b>	<b>Measurement techniques</b>	$\sigma_d$ ( $10^{-28}$ e-cm)
ILL CryoEDM	Superfluid $^4\text{He}$	$^4\text{He}$	Ramsey technique for $\omega$ External SQUID magnetometers	Phase1 ~ 50 Phase2 < 5
PNPI – ILL	ILL turbine PNPI/Solid $\text{D}_2$	Vac.	Ramsey technique for $\omega$ E=0 cell for magnetometer	Phase1 < 100 < 10
ILL Crystal	Cold n Beam		Crystal Diffraction	< 100
PSI EDM	Solid $\text{D}_2$	Vac.	Ramsey technique for $\omega$ External Cs & $^3\text{He}$ magnetometers Hg co-mag for P1, Xe for P2?	Phase1 ~ 50 Phase2 ~ 5
SNS EDM	Superfluid $^4\text{He}$	$^4\text{He}$	$^3\text{He}$ capture for $\omega$ $^3\text{He}$ comagnetometer SQUIDS & Dressed spins	~ 8
TRIUMF/JPARC	Superfluid $^4\text{He}$	Vac.	Under Development	?

# Comparison of worldwide

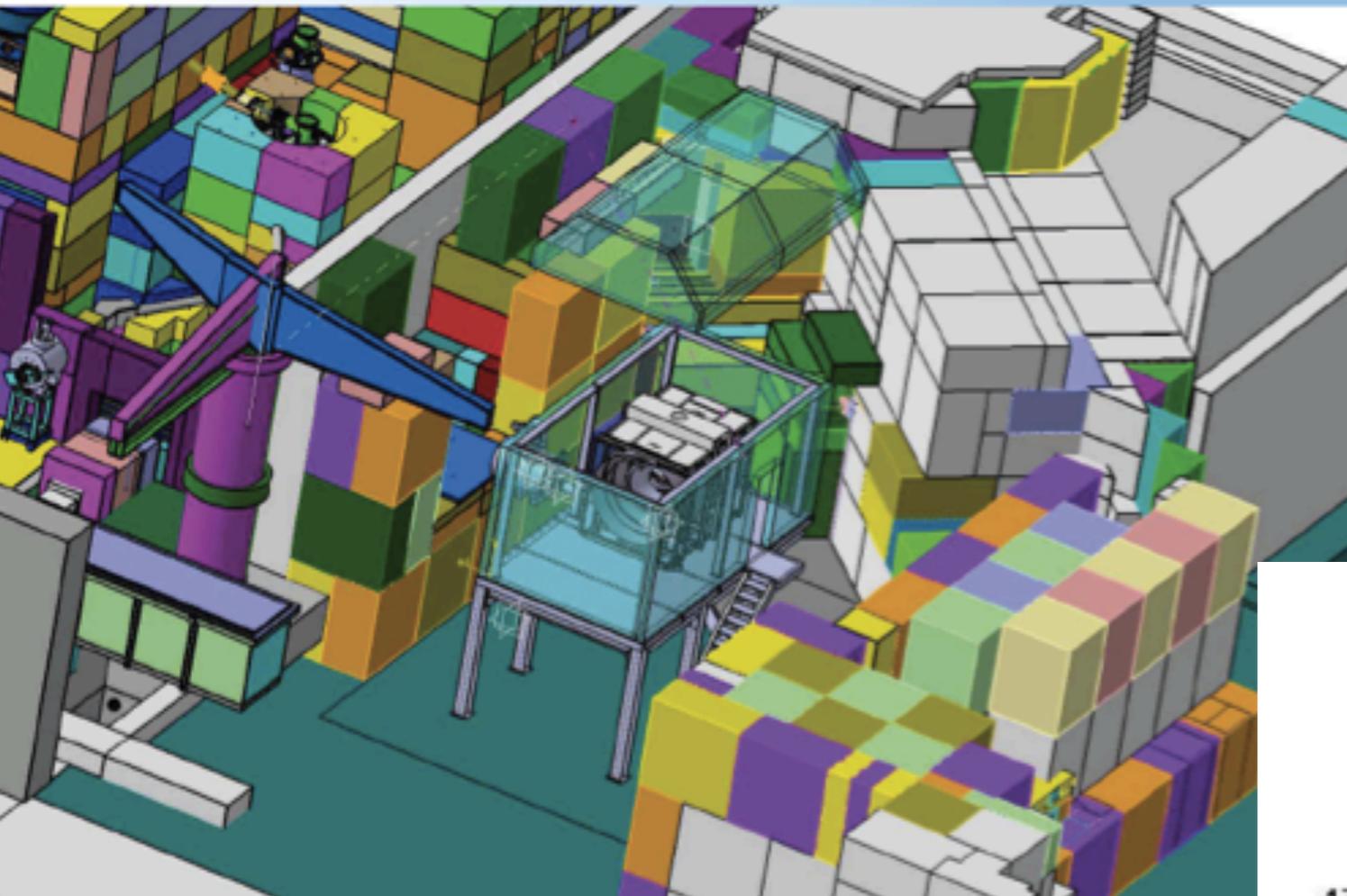
(Brad Filippone)

- Comparing sensitivities from different experiments is somewhat qualitative (depends on many assumptions)
- At present, ILL CryoEDM and PSI-nEDM appear to be the most competitive with SNS nEDM
- Both ILL-CryoEDM and PSI-nEDM have 2 phases of measurement with some construction between the data periods

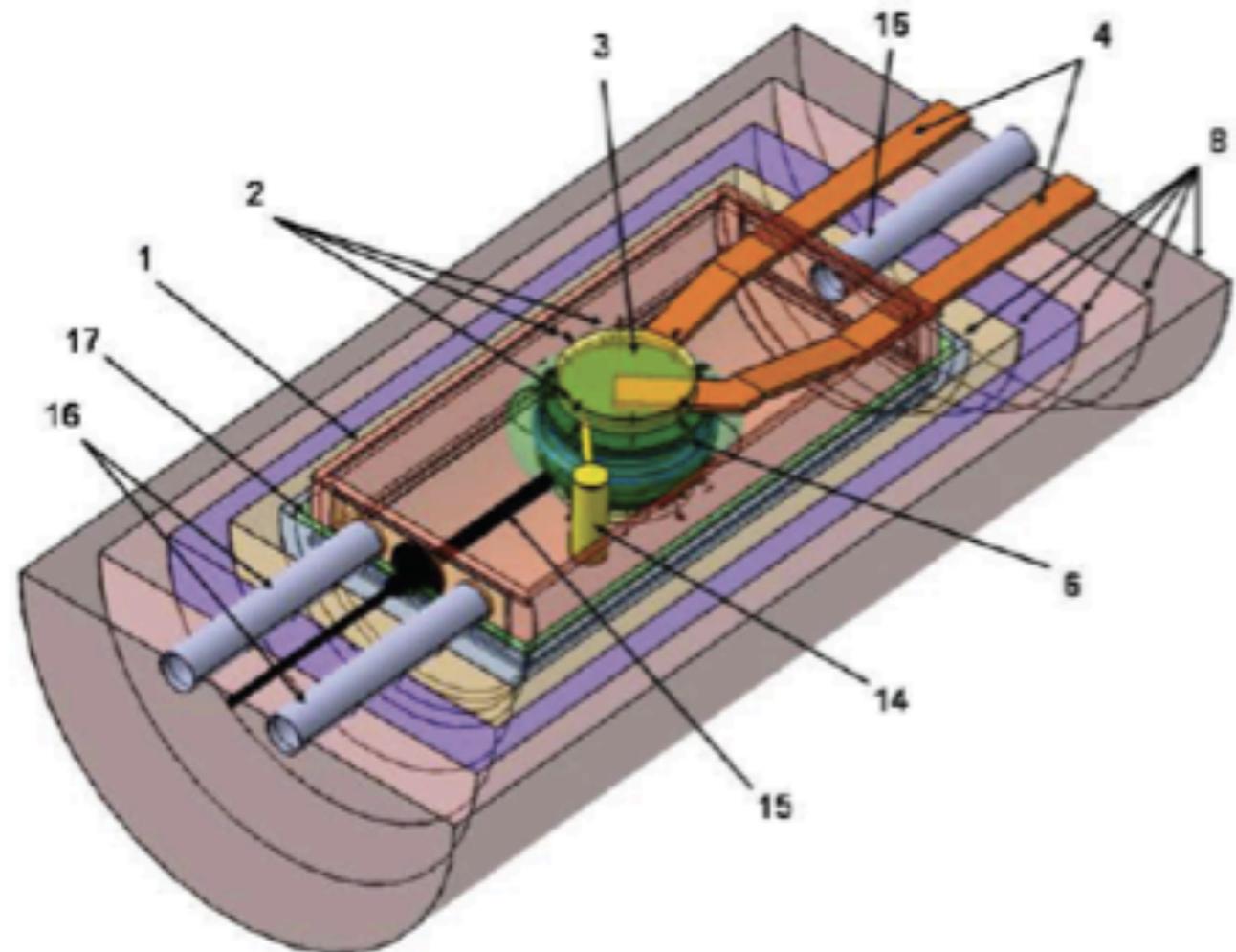
# PSI high flux UCN source

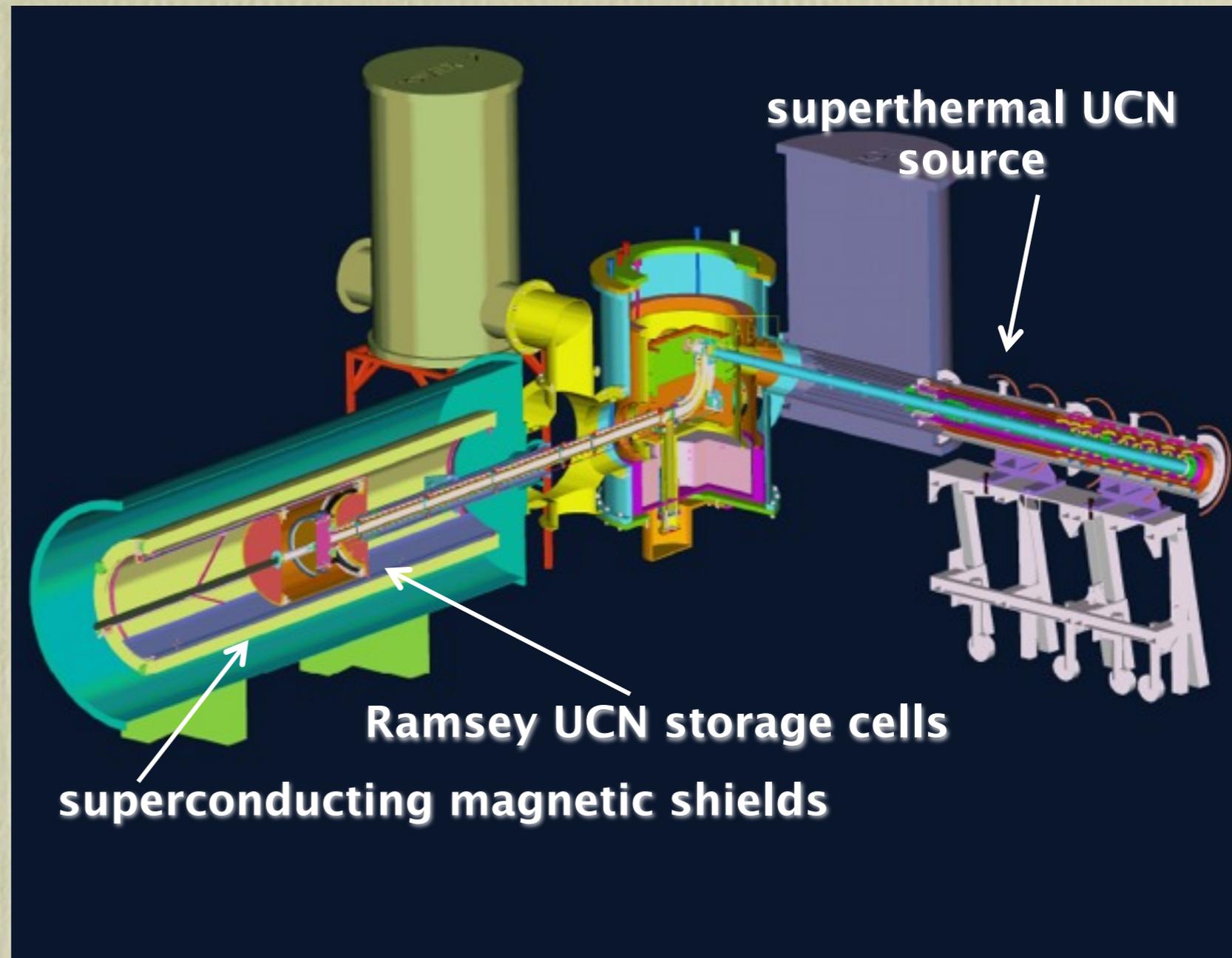
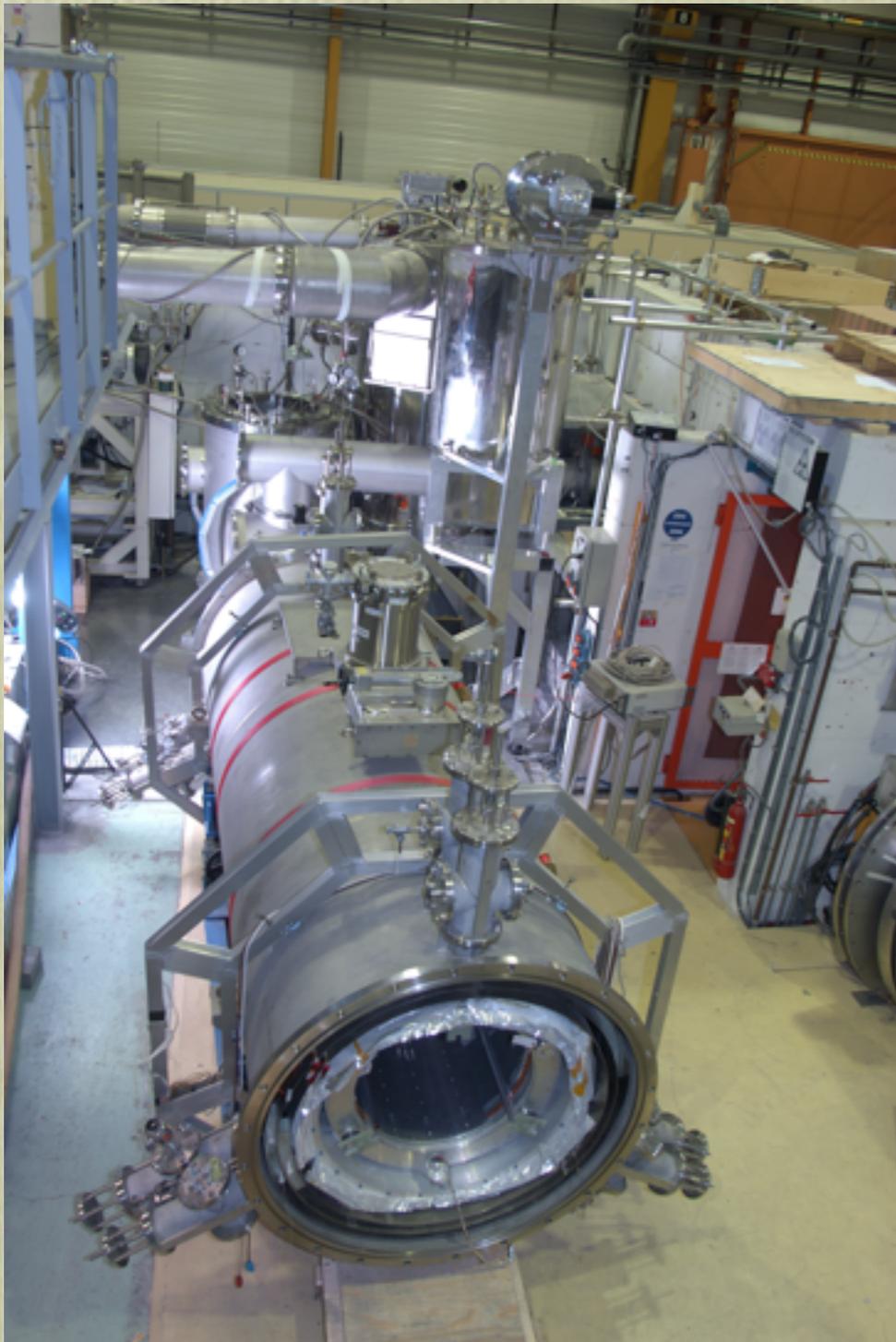
(Brad Filippone)

## PSI UCN area south



- Initial data will use original apparatus from ILL with magnetic upgrades
- New apparatus being designed for higher sensitivity





**whole experiment in superfluid He at 0.5 K**

- production of UCN
- storage & Larmor precession of UCN
- SQUID magnetometry
- detection of UCN

# Ongoing nEDM experiments schedules and sensitivities

(Brad Filippone)

Exp	Status	Schedule	Claimed Sensitivity (e-cm)
ILL CryoEDM	Phase 1 – underway Phase 2 – new beamline	2010-12 2012-15	$< 5 \times 10^{-27}$ $< 5 \times 10^{-28}$
PNPI- EDM	PNPI @ ILL Move to PNPI UCN	2010 ?	$\sim 10^{-26}$ $< 10^{-27}$
PSI EDM	Initial phase underway (using old ILL apparatus) New exp.	2010-13 2015	$\sim 5 \times 10^{-27}$ $\sim 5 \times 10^{-28}$
SNS EDM	Preparing Baseline	2016 2018	Commissioning $\sim 8 \times 10^{-28}$

# Other factors

(Brad Filippone)

- The "known" systematic effects are part of the experimental design
- Tackling the unknown effects requires unique handles in the experiment that can be varied
- The significance of a non-zero result requires multiple approaches to unforeseen systematics
- nEDM @ SNS is unique in its use of a polarized  $^3\text{He}$  co-magnetometer, characterization of geometric phase effects via temperature variation, as well as the dressed spin capability

# Comparison of capabilities

(Brad Filippone)



= included



= not included

	C R Y O E D M 1	C R Y O E D M 2	P S I E D M 1	P S I E D M 2	S N S E D M
$\Delta\omega$ via accumulated phase in n polarization	Green	Green	Green	Green	Red
$\Delta\omega$ via light oscillation in $^3\text{He}$ capture	Red	Red	Red	Red	Green
Co-magnetometer	Red	Red	Green	?	Green
Superconducting B-shield	Green	Green	Red	Red	Green
Dressed Spin Technique	Red	Red	Red	Red	Green
Horizontal B-field	Green	Green	Red	Red	Green
Multiple EDM cells	Red	Green	Red	Green	Green

Note that red vs green does not necessarily signify good vs bad. But understanding systematics requires mix of red & green.